

# Introduction to accelerators

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## Acronyms

- RF – radiofrequency
- MW – microwave
- HV – high voltage
- SC – superconducting

## Links

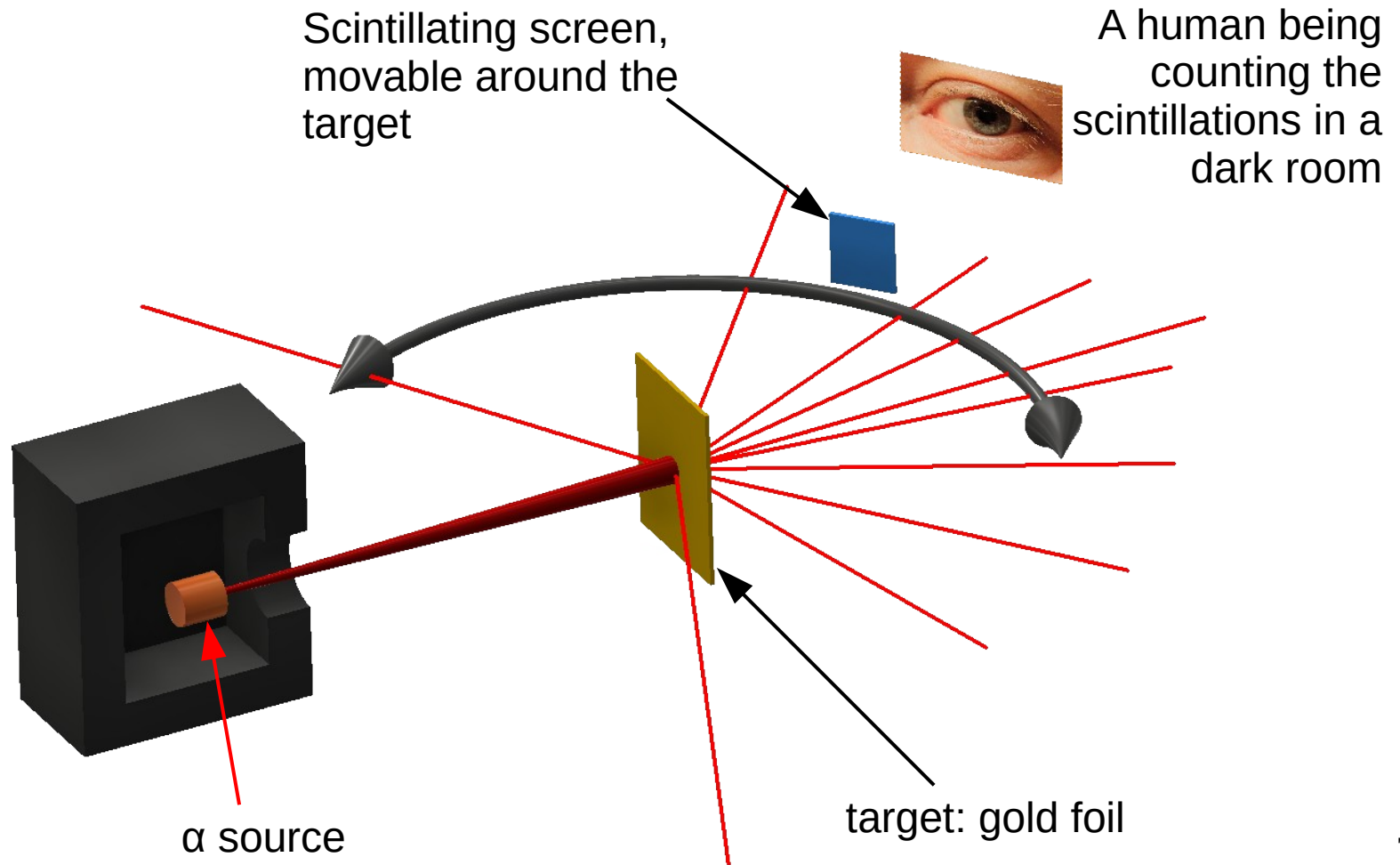
- <http://indico.cern.ch/event/532397/timetable/>  
(CERN Accelerator School 2016, Budapest, videorecordings!)

# TODO

- Introduce luminosity

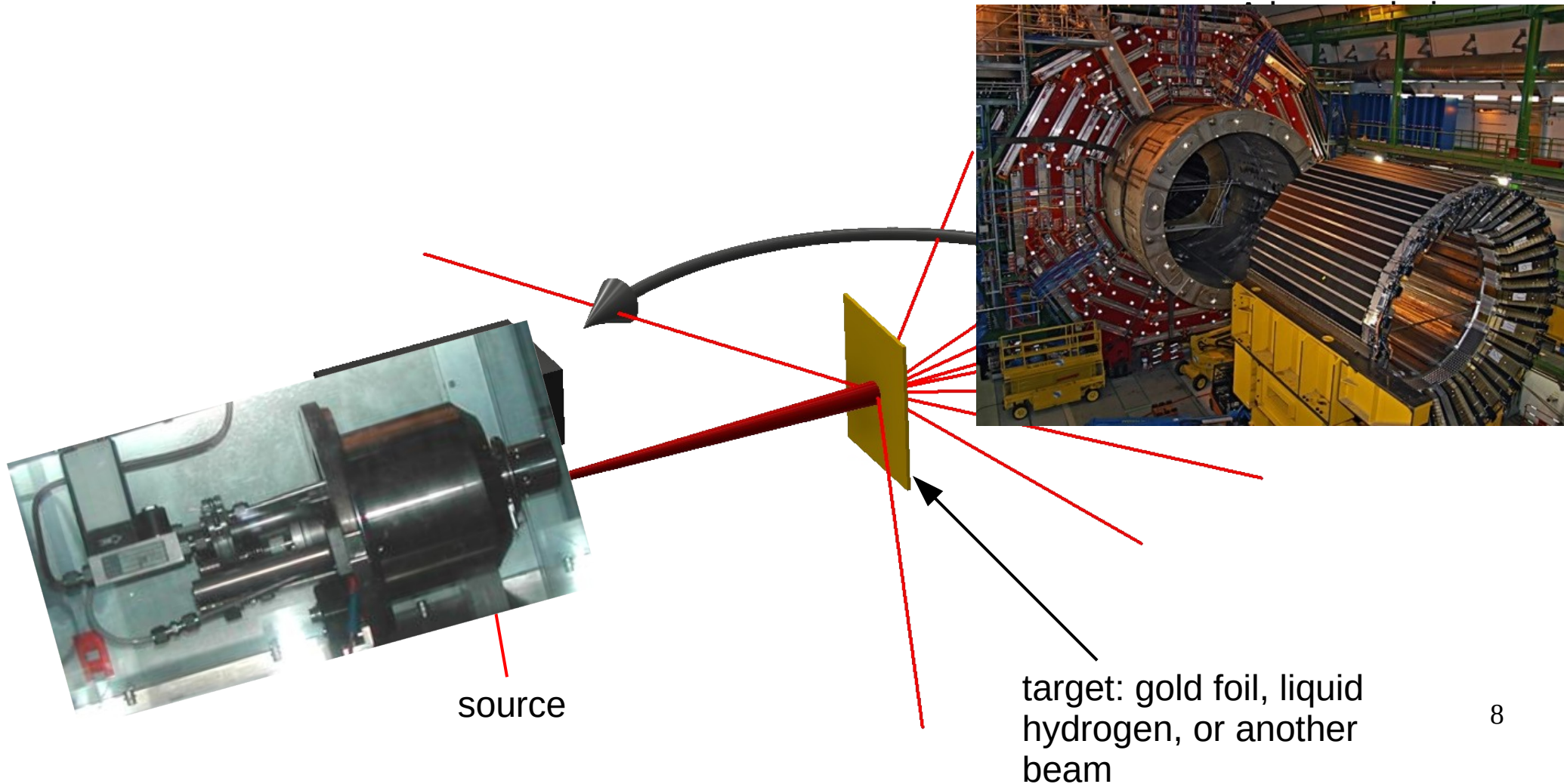
# The beginning...

- Rutherford experiment (1908-1913): radioactive ( $\alpha$ ) radon source – “natural accelerator” (outcome: discovery of the nucleus)



# The beginning...

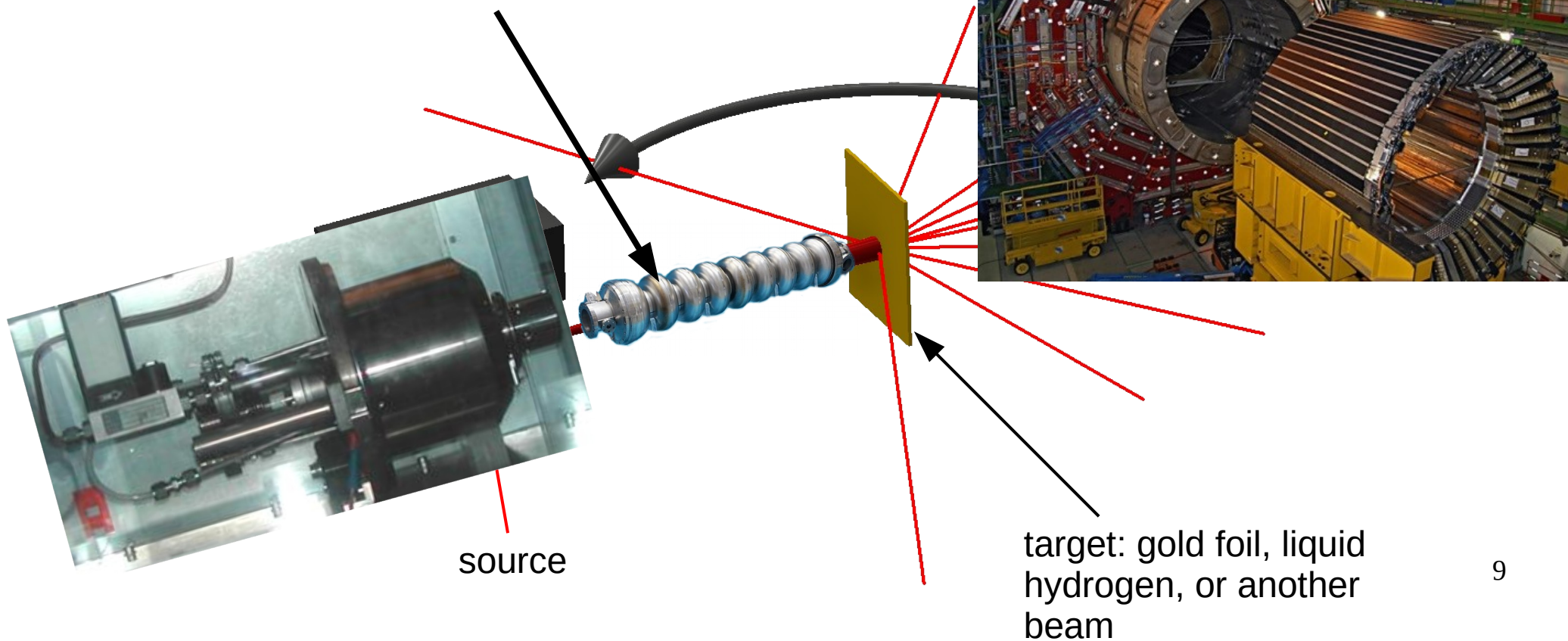
We are repeating the bloody same experiment ever since...



# The beginning...

We are repeating the bloody same experiment ever since...

**But: we have now  
ACCELERATORS!**



# The beginning...

- Rutherford (1927): *“What we require is an apparatus to give us a potential of the order of 10 million volts which can be safely accomodated in a reasonably sized room and operated by a few kilowatts of power. We require too an exhausted tube capable of withstanding this voltage. [...] I see no reason why such a requirement cannot be made practicable by the use of oil or air under high pressure, but these are problems for the future”*

# Particle sources



# Particle sources: classification

- Primary beams: produced directly
    - Protons
    - Electrons
    - Ions
      - positive
      - negative
- constituents of ordinary matter
- Secondary beams: produced by another beam hitting a target
    - Pions
    - Muons
    - Antiprotons
    - Positrons

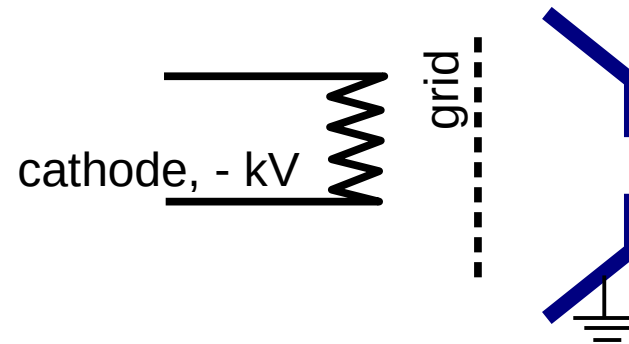
# Electron sources

- Electrons must receive sufficient energy to overcome the work function
  - Temperature (heated or thermic cathodes)
  - Laser (photocathodes)

# Electron sources: thermic cathodes

- Current: number of electrons above work function

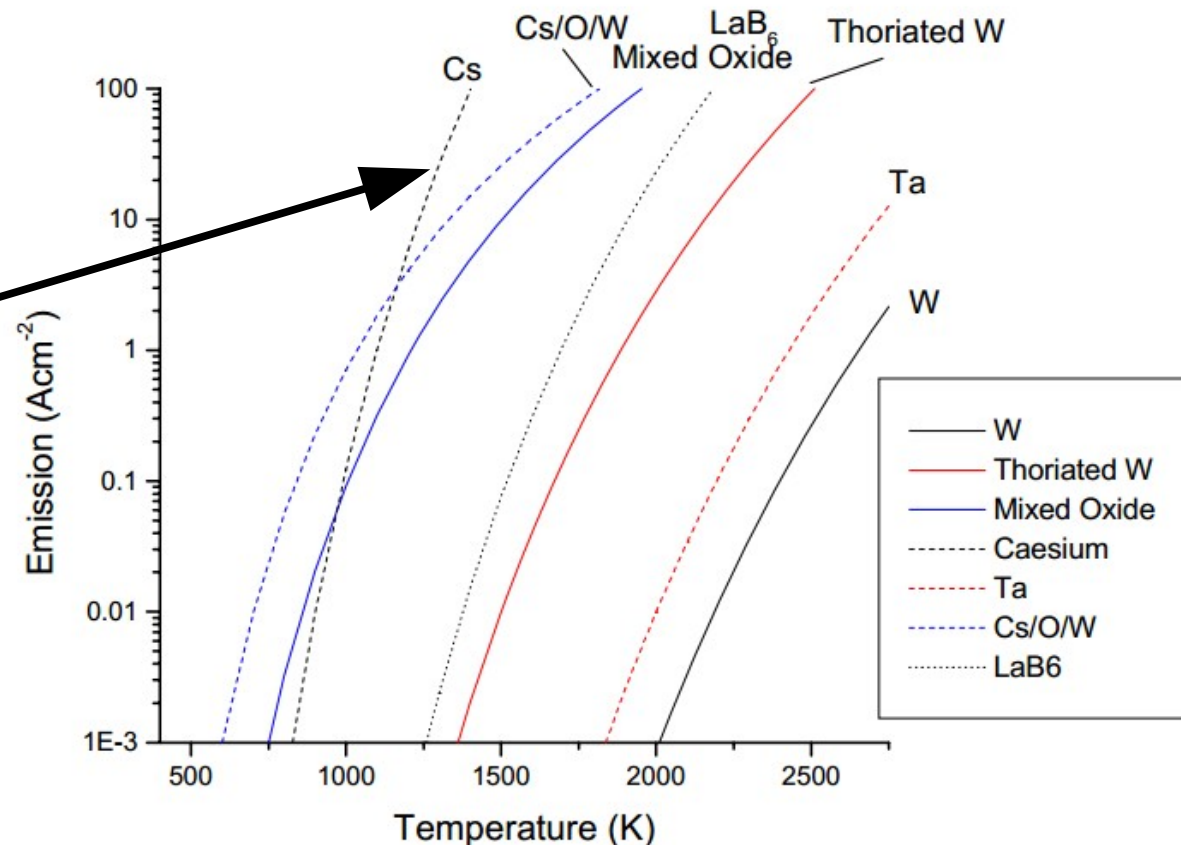
$$J = A T^2 \exp\left(\frac{-e \Phi_{work}}{kT}\right)$$



time structure of electron beam can be manipulated by voltage on the grid

- Good cathode materials:
  - Survives high temperatures
  - Low work function

(Cs melts above 300K, curve is for info only)



- Old televisions used this technique (CRT–cathode ray tube)

# Electron sources: photocathodes

- Same principle like photomultiplier: photon with energy above work function  $E=h\nu > \Phi_{\text{work}}$ , can liberate an electron
- Surplus energy above work function goes to kinetic energy
- **Quantum efficiency ( $Q_e$ )**: average # of electrons for 1 photon.
- Metals: work function in UV. Reflection  $\rightarrow$  low  $Q_e$  (copper:  $\sim 10^{-4}$ )
- Semiconductors are better
- Fast, short and well timed laser pulses can deliver a bunch train with required microstructure (needed for RF acceleration, see later)

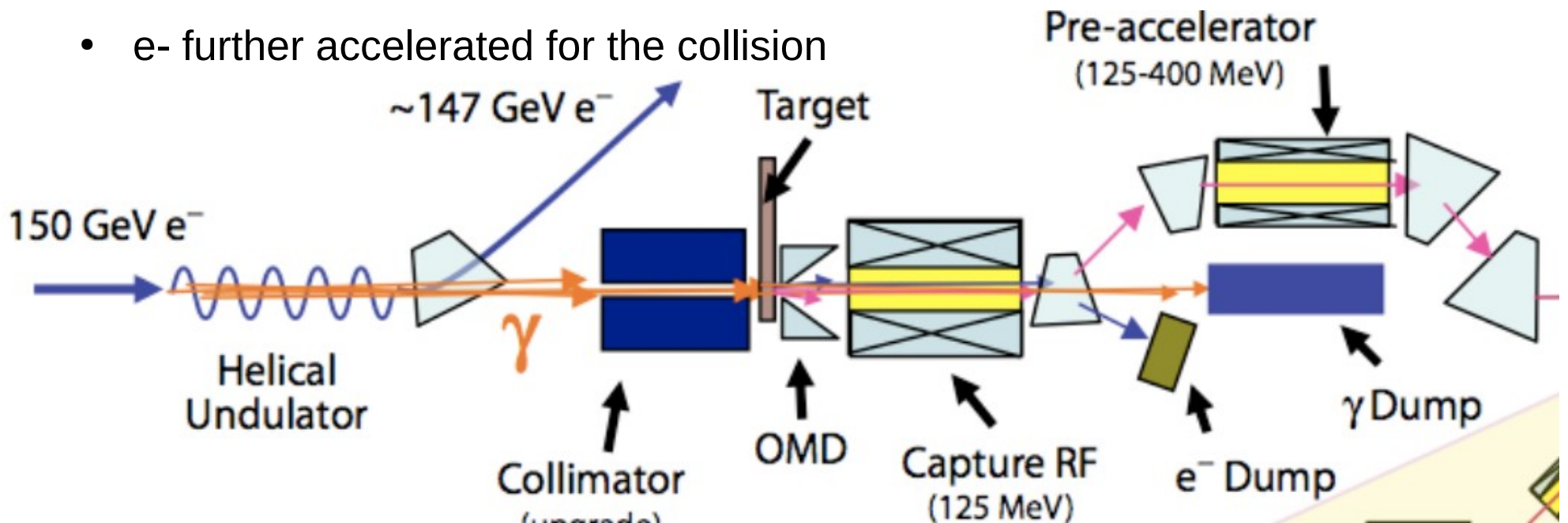
	$Q_e$ [%]	$\lambda$ [nm]
Cu	0.01	267
$K_2CsSb$	29	590
$Cs_2Te$	12.4	$\sim 350$
GaAs:Cs	17	225

# Electron sources in general

- Electrons have small (negligible) kinetic energy
- Initially accelerated by the static or RF field of carefully designed electrodes (puller or extraction electrode)
- Child-Langmuir limit: electron cloud at the surface of the cathode shields the puller electrode's field, this limits achievable current.

# Positron-sources (secondary beam)

- Standard solution:
  - intensive electron-beam (few GeV – 20 GeV) on target. Positron intensity  $\sim$  total energy of e- beam
  - thick, large-Z target. (production- or conversion-target). Beam energy is converted into electromagnetic shower: e<sup>+</sup>/e<sup>-</sup> particles + others
- ILC (International Linear Collider – planned) [250+250 GeV]
  - Main electron beam at 150 GeV passes an undulator
  - produces 30 MeV-es photons (like in a Free Electron Laser)
  - Photons hitting a thin production target: e<sup>±</sup> pair production
  - e- further accelerated for the collision



# Ion sources

- Ionization of a low-pressure gas - plasma

- Typically electrons used for ionization

- Electrons must have:  
 $E_{\text{kin}} > I_n$  (ionization energy)  
 optimum:  $E_{\text{kin}} \sim 2-3 \times I_n$

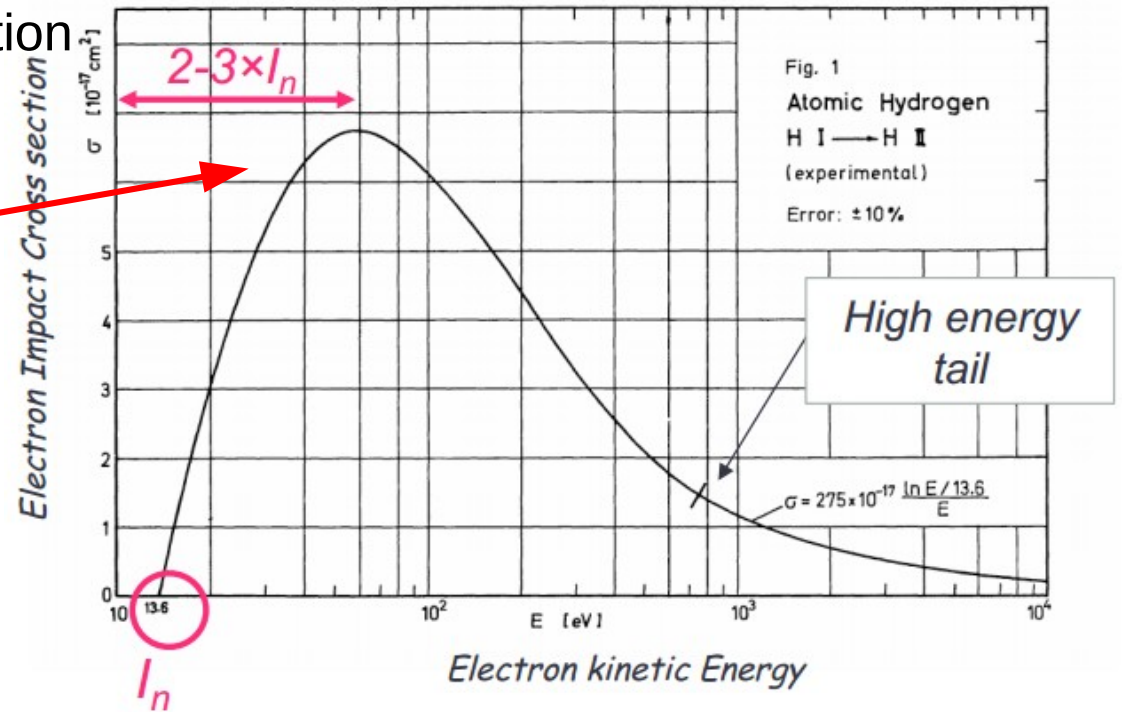
- Phenomena in a plasma:

- Electron impact ionization:  
 $e^- + A^{n+} \rightarrow A^{(n+1)+} + 2e^-$
- Charge exchange:  
 $A^{n+} + B^0 \rightarrow A^{(n-1)+} + B^+$
- Elastic collisions

- Plasma needs to be confined for long term with stable parameters
- Need several collisions for multiply ionized ions – keeping for long time

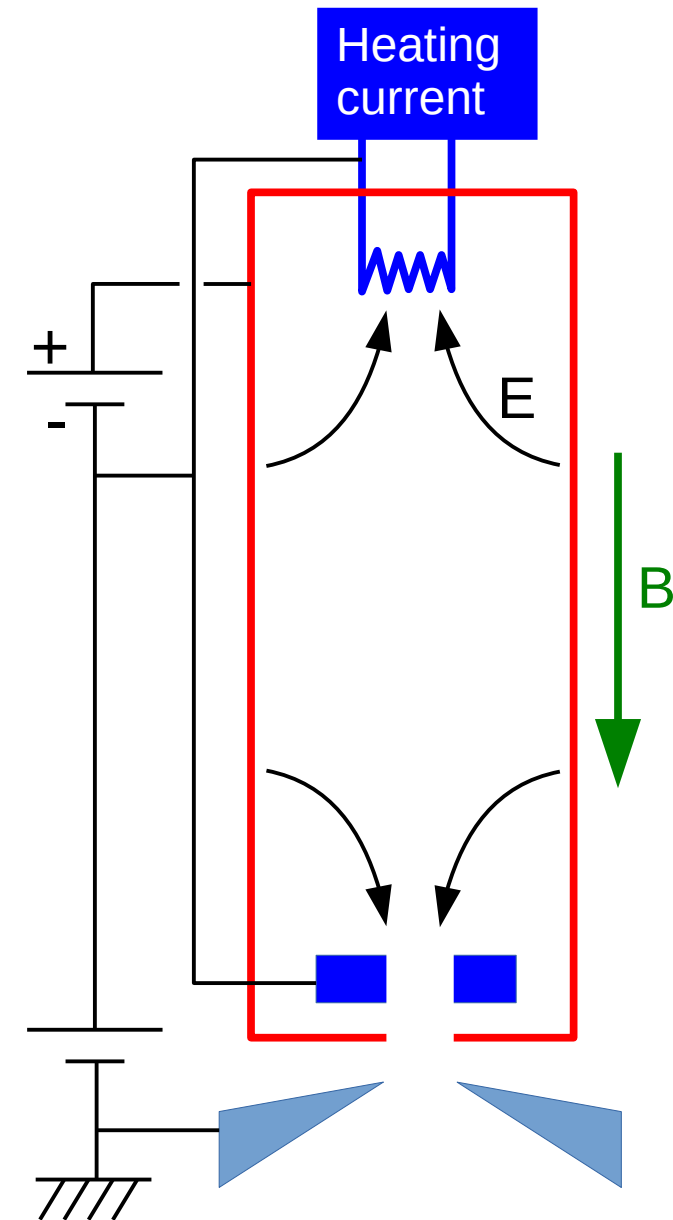
Electrons can come from:

- External source – electron gun
- From the plasma itself



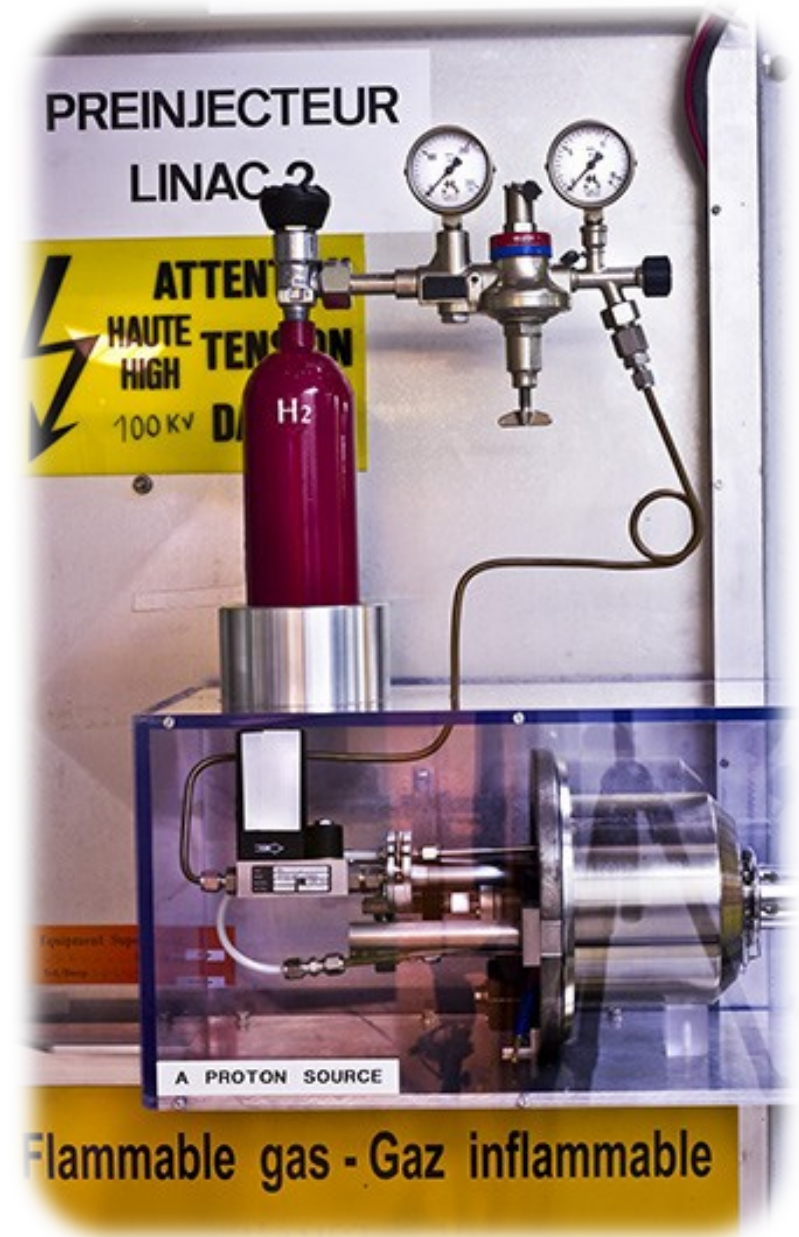
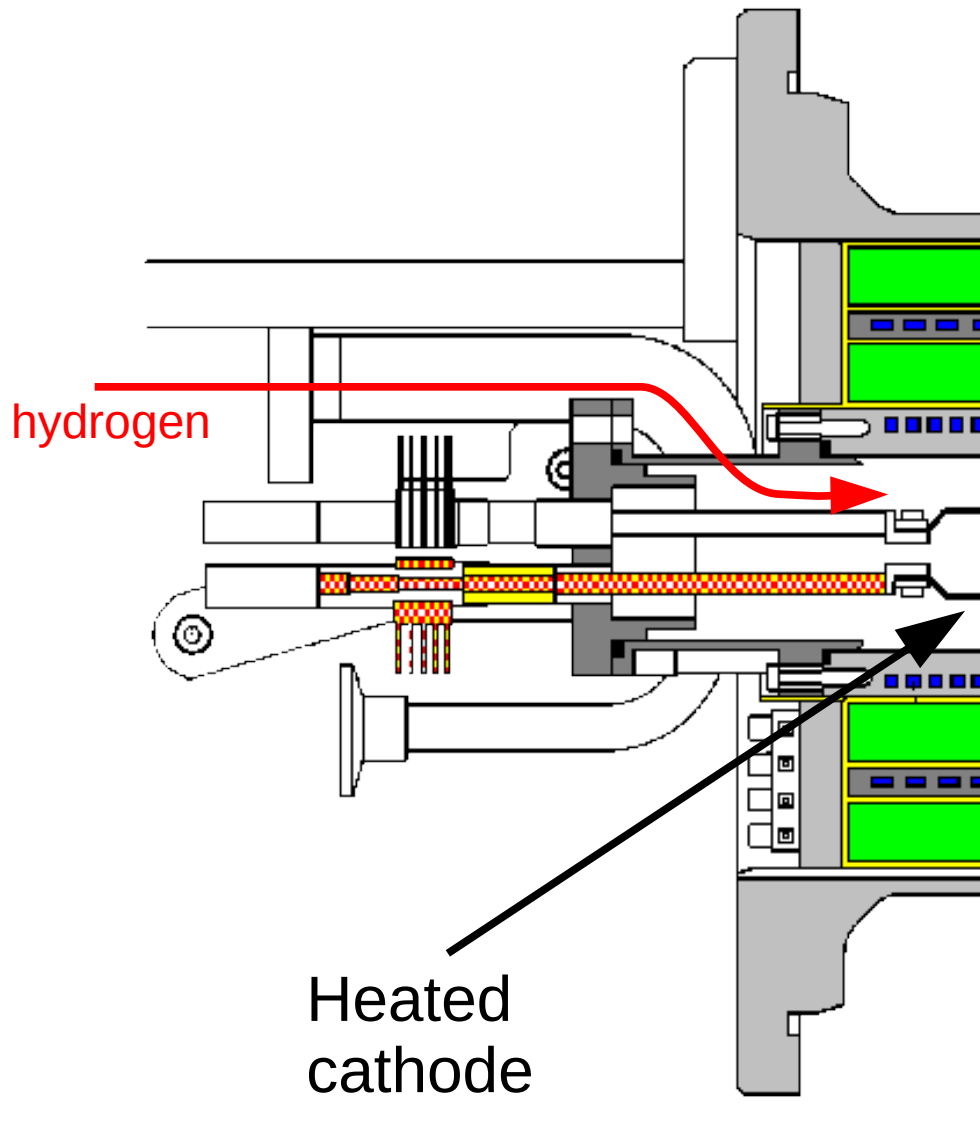
# Penning ionization gauge (PIG) ion source

- Heated cathode provides electrons
- Penning trap: electrons confined by B field in the transverse, E field in the longitudinal direction
  - cf Penning vacuum gauge
- Electrons gain energy from E field, and ionize the low-pressure gas
- Gas pressure typically  $10^{-3} - 1$  mbar:
  - If pressure too large, electrons collide before gaining sufficient energy
  - If pressure too low, not enough output current
- Whole unit on positive voltage. Ions extracted by grounded puller/extraction electrodes

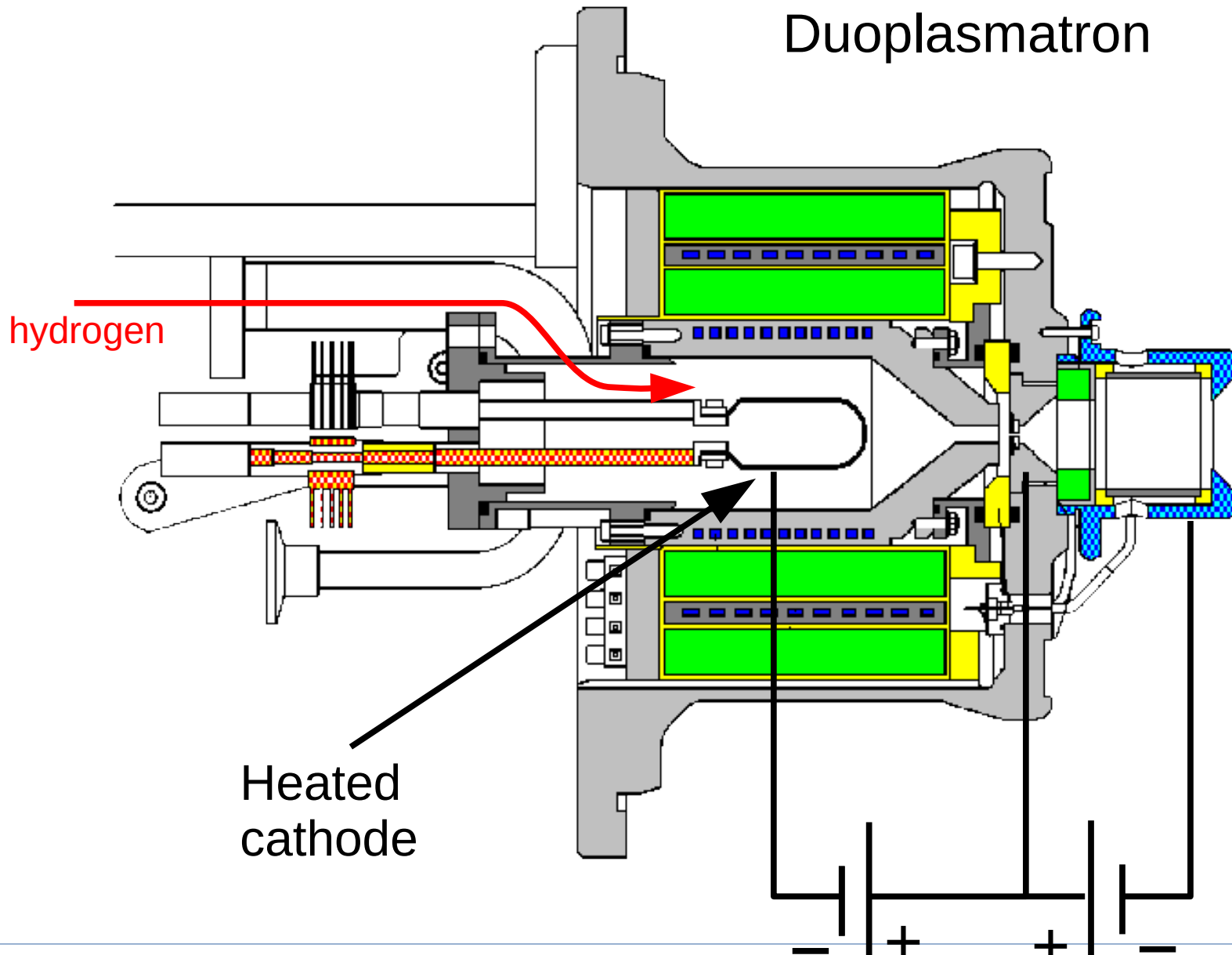




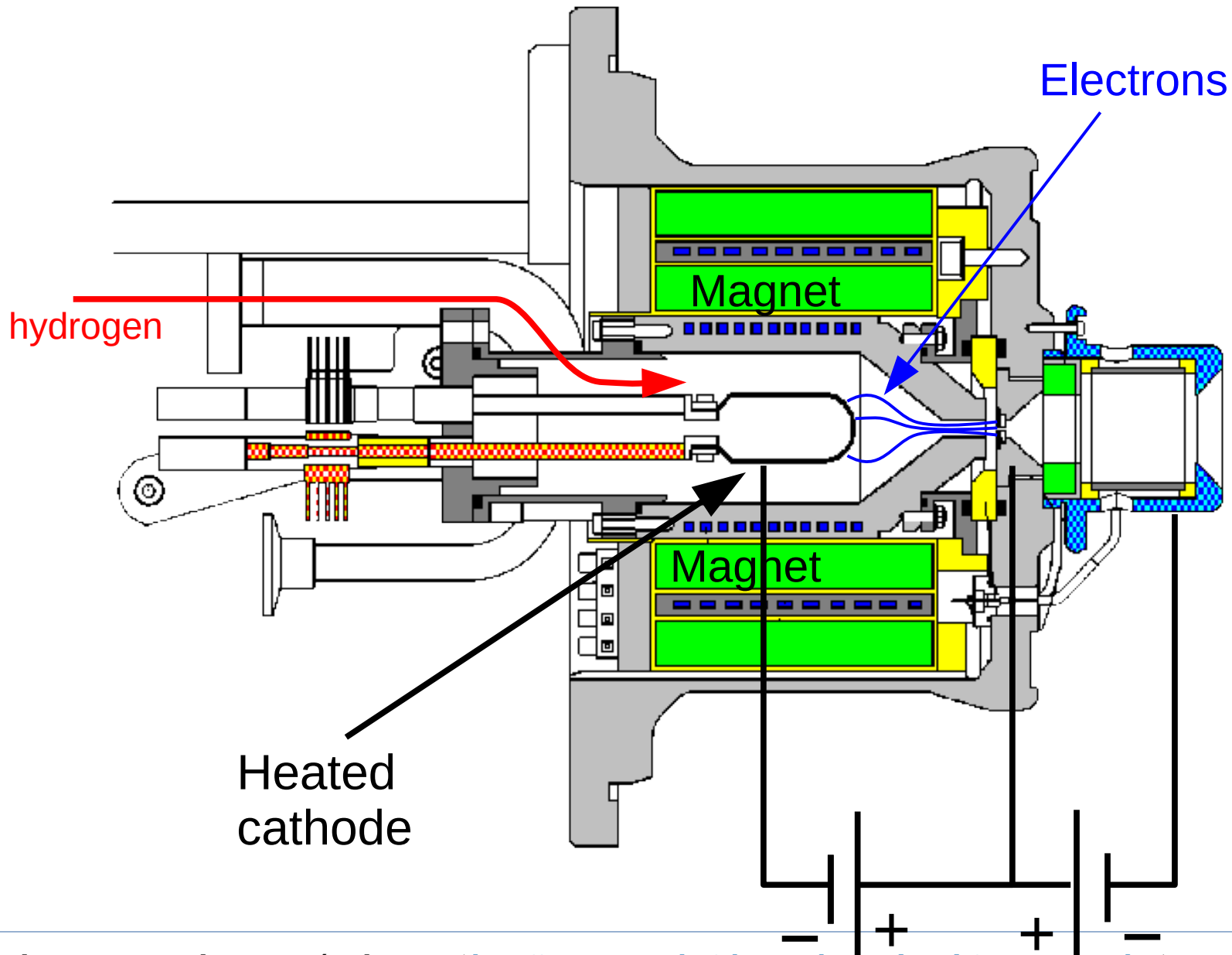
# Duoplasmatron



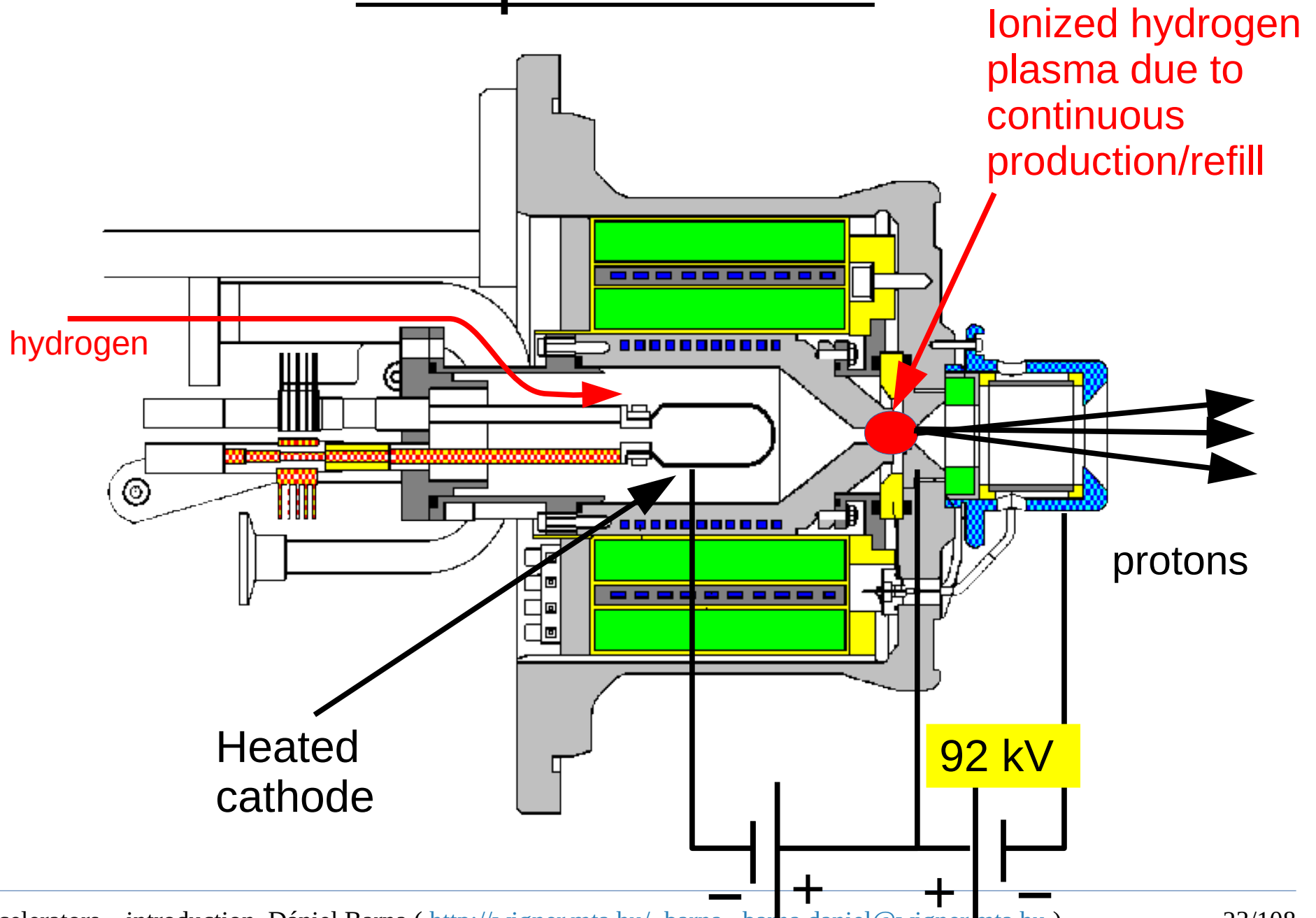
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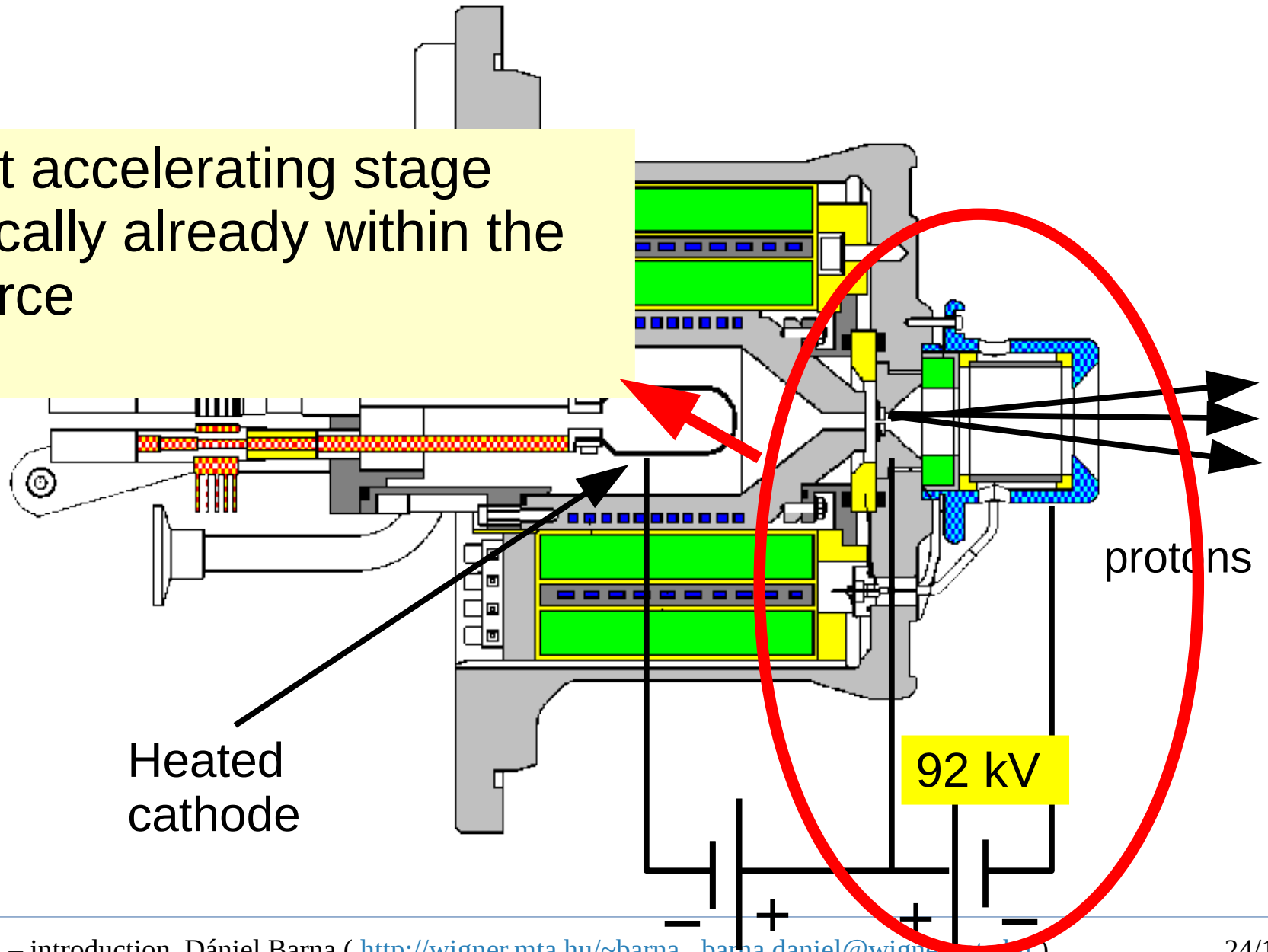


# Duoplasmatron



# Duoplasmatron

- First accelerating stage typically already within the source



# Electron Cyclotron Resonance Ion Source (ECRIS)

- More: <http://cas.web.cern.ch/cas/Slovakia-2012/Lectures/ThuillierI.pdf>

- **Electron cyclotron resonance:**

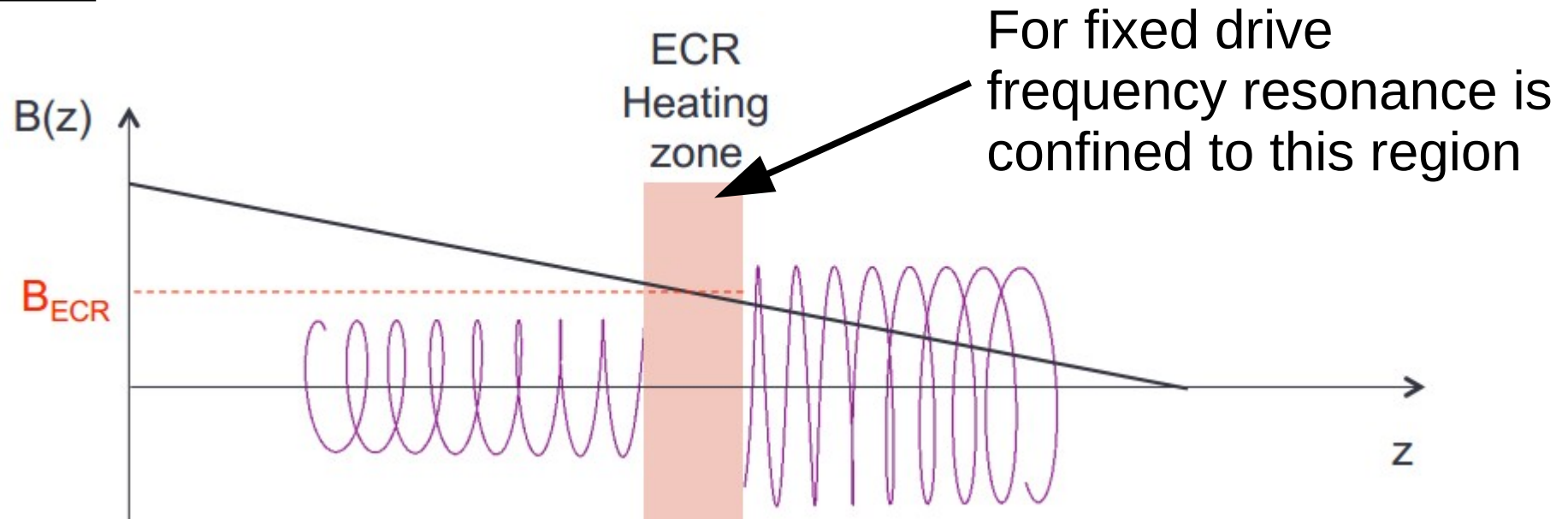
- In B field the (nonrelativistic) revolution frequency of electrons (cyclotron frequency) is constant:

$$\omega = \frac{q B}{m} \quad f = \frac{q B}{2 \pi m}$$

- Typically in the MW regime:  
f=28 GHz (B=1T); f=2.8 GHz (B=0.1T)
- Resonance: E field with same frequency will excite cyclotron motion, electrons gain energy for ionization

# Electron Cyclotron Resonance Ion Source (ECRIS)

- Electron cyclotron resonance in inhomogeneous B field:



- Size of ECR zone correlates with gradient of B
- In ECRIS, the ECR zone is typically a confined surface

# Electron Cyclotron Resonance Ion Source (ECRIS)

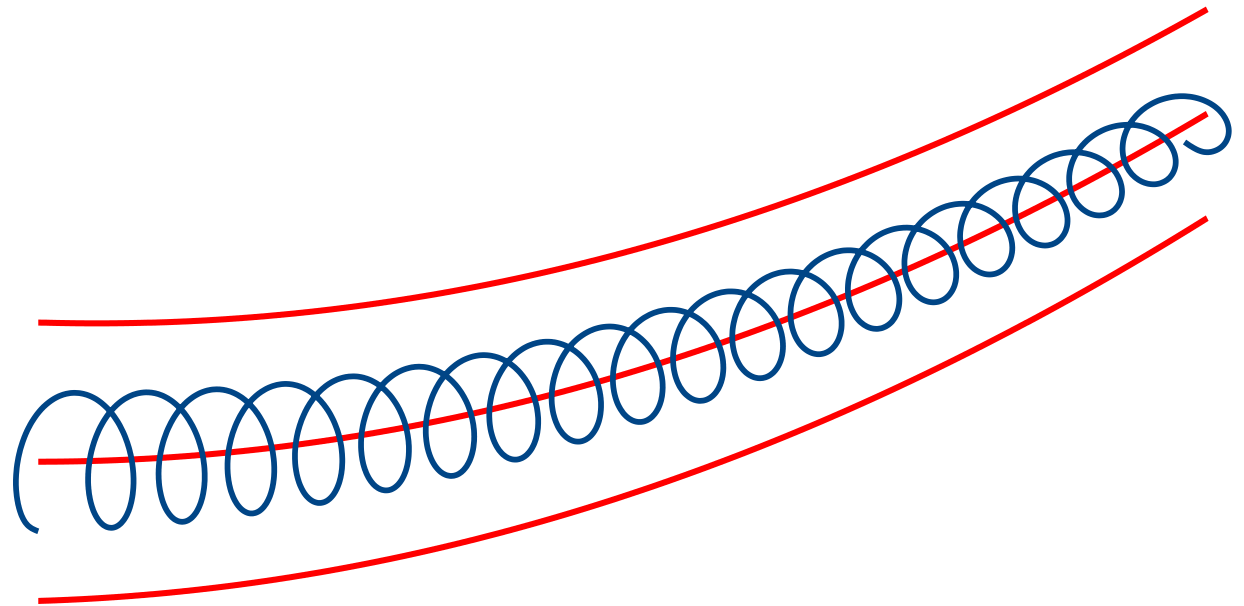
- **Charged particles in a magnetic field**

- $E_{\text{kin}} = \text{const}$ , since  $\vec{F} = q \vec{v} \times \vec{B} \perp \vec{v}$

- Low-energy particles spiral around induction lines

- if their energy  $\ll$  inhomogeneity of field

- more specifically if:  $\delta B/B \ll 1$  over one cyclotron turn





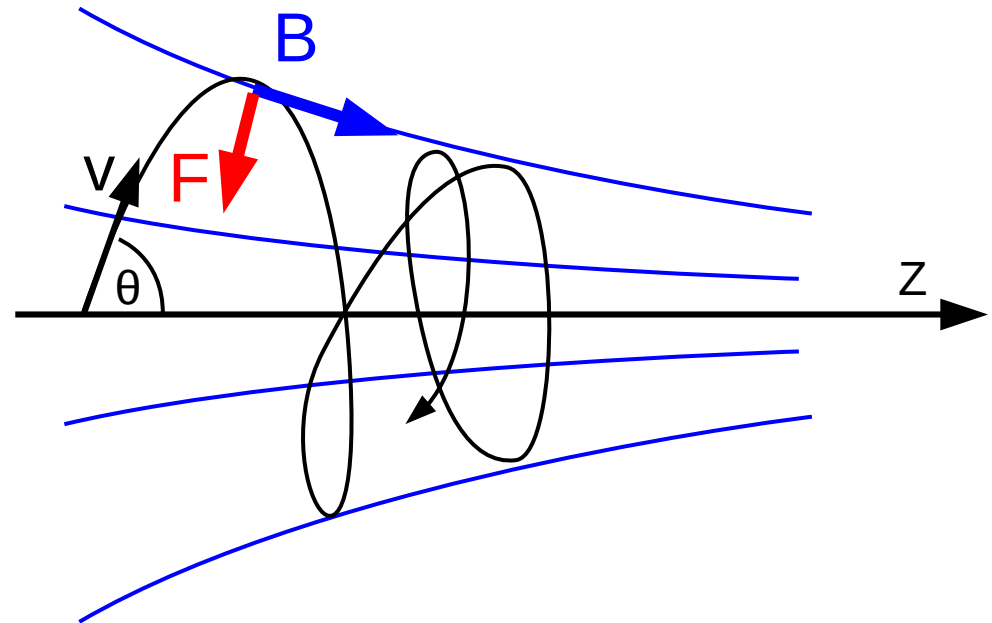
# Electron Cyclotron Resonance Ion Source (ECRIS)

Magnetic mirror, magnetic bottle

- Stronger magnetic field → converging induction lines

- Force has z component

- If angle is over a threshold  $\theta > \theta_{\min}$  (depending on B), particle bounces back



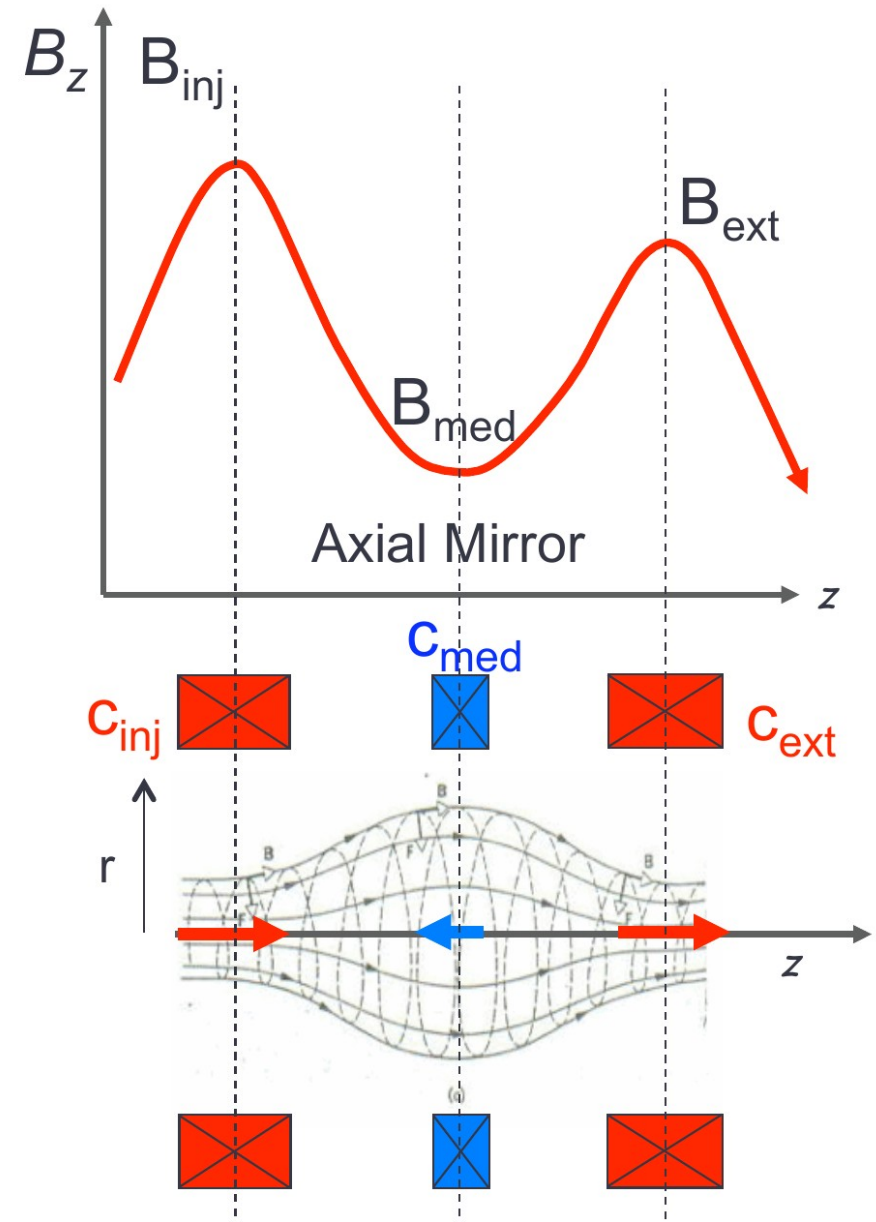
- $\theta < \theta_{\min}$  - “loss cone”, particles escape the bottle. Collisions always refill this zone.

- Loss cone is used to outcouple the ions

# Electron Cyclotron Resonance Ion Source (ECRIS)

Trapping along the z axis: using a magnetic bottle

Confines both electrons and ions



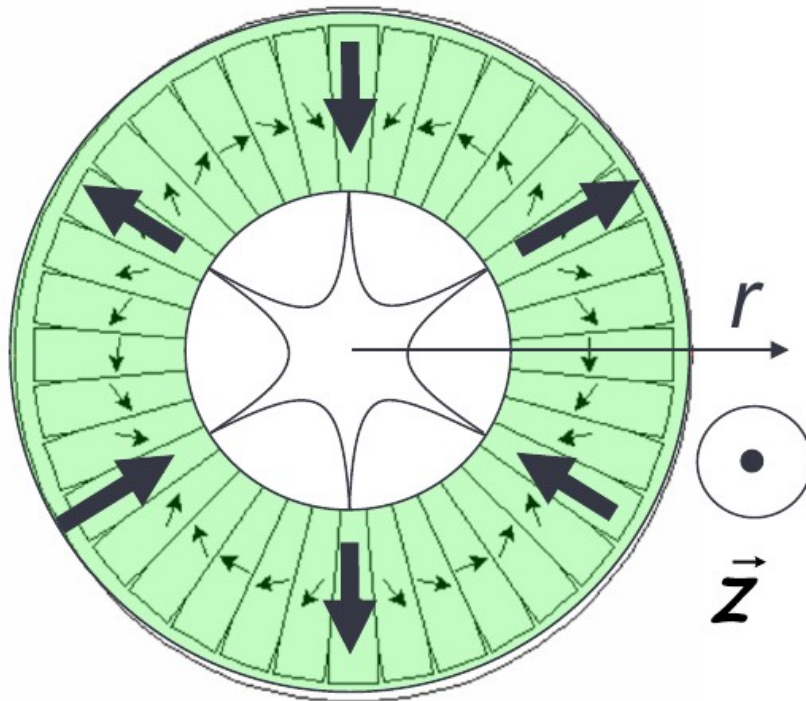
# Electron Cyclotron Resonance Ion Source (ECRIS)

Trapping radially: sextupole field

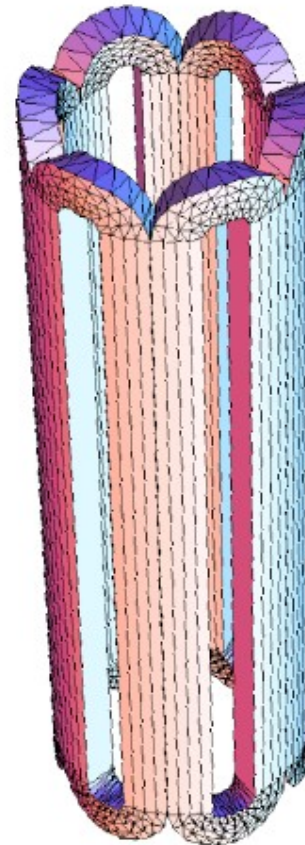
Using permanent magnets...

or

electromagnets



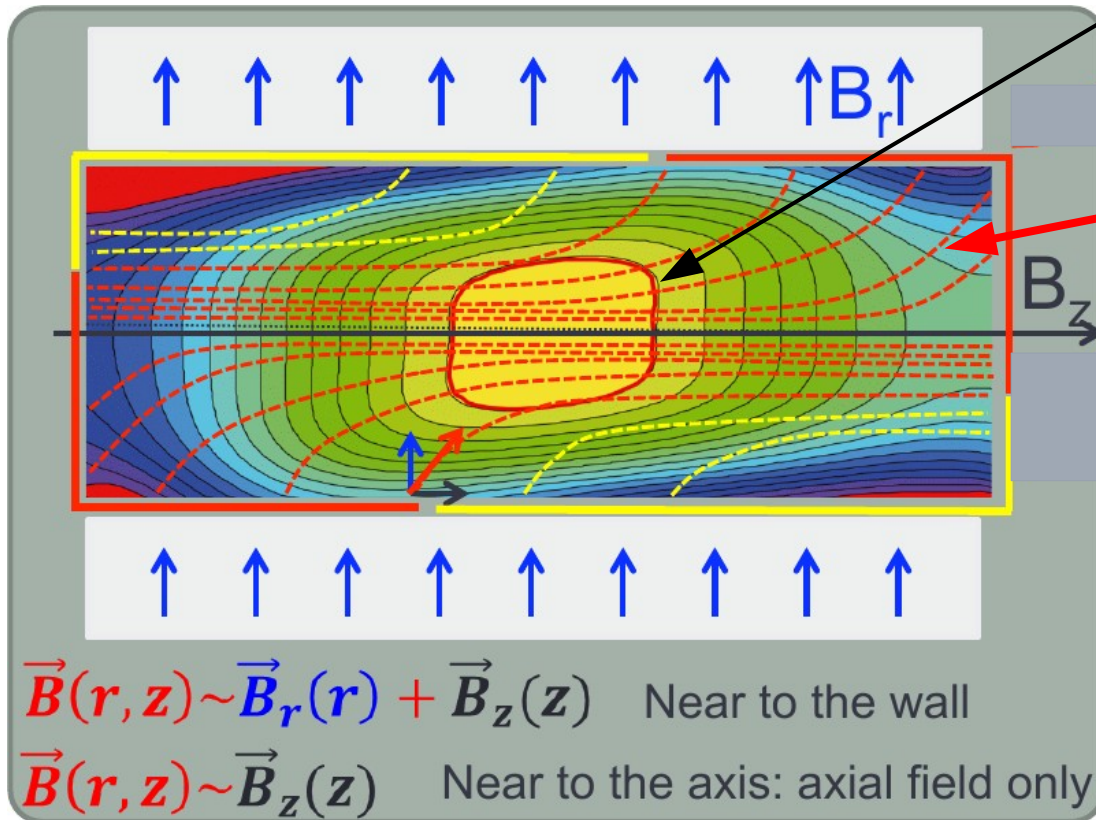
(HallBach Hexapole  
With 36 permanent magnets  
30° rotation/magnet)



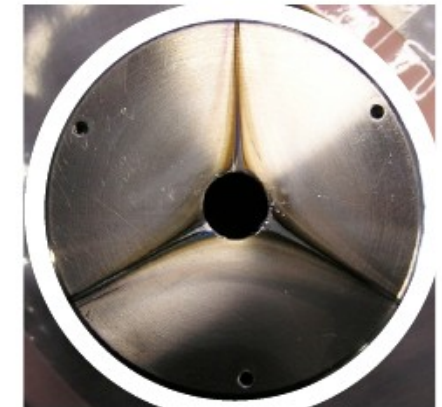
# Electron Cyclotron Resonance Ion Source (ECRIS)

Resulting magnetic field is not easy to understand

Color:  $|B|$



Resonance surface. Electrons following red induction lines passing through this surface gain energy from MW field and ionize on their path



Plasma shape at injection (L) and Extraction (R)

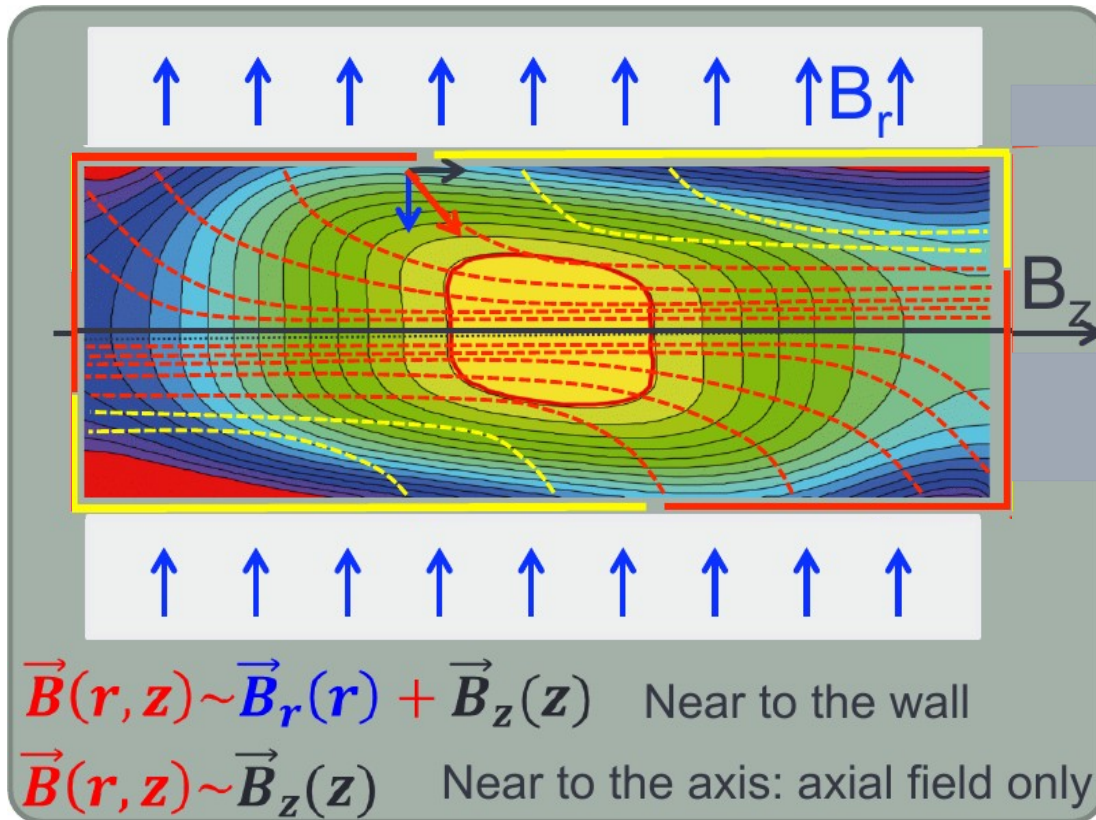
Source: Thuillieri CAS lecture

# Electron Cyclotron Resonance Ion Source (ECRIS)

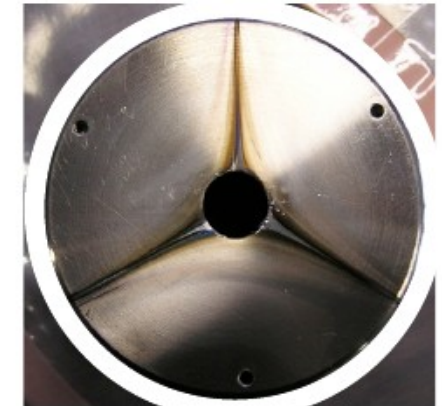
Resulting magnetic field is not easy to understand

Rotated by 60° around z axis

Color: |B|



Forrás: Thuillieri CAS előadás



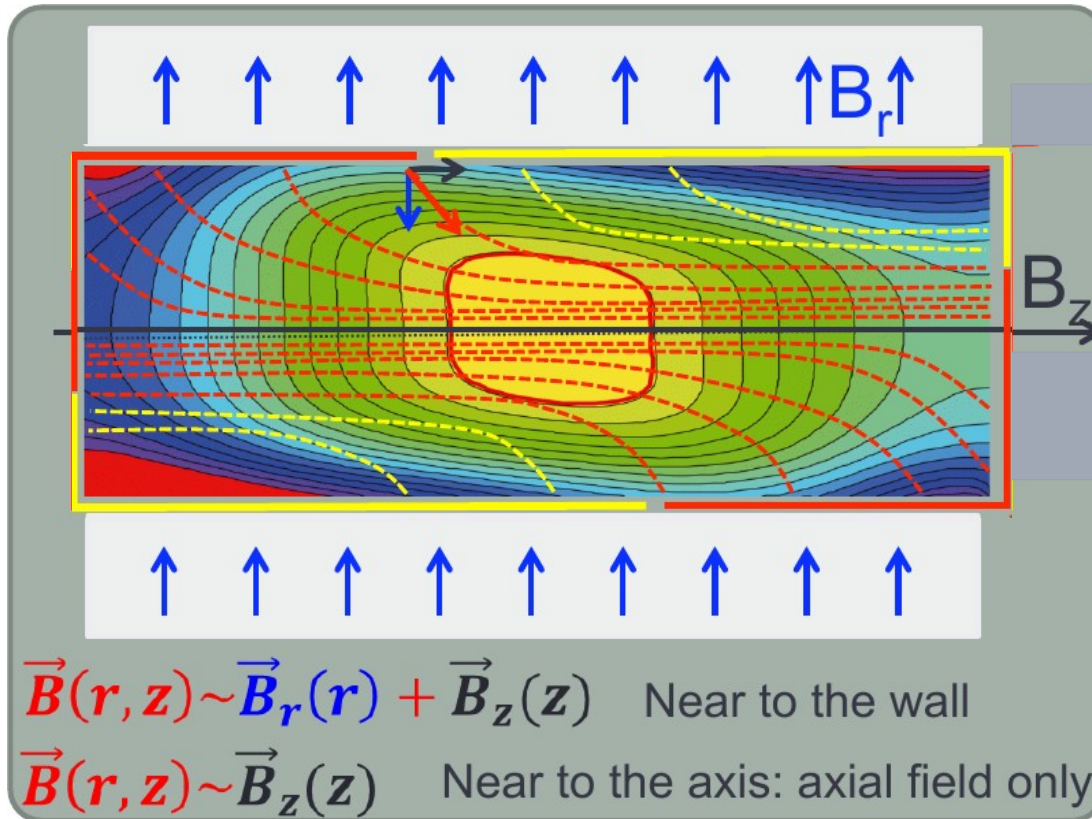
Plasma shape at injection (L) and Extraction (R)

# Electron Cyclotron Resonance Ion Source (ECRIS)

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Color:  $|B|$



Question: on the  $|B| = \text{const}$  resonance surface, why is the induction line density non-constant, whereas  $|B|$  is?



Plasma shape at injection (L) and Extraction (R)

Forrás: Thuillieri CAS előadás

## Pion beam

- Secondary beam
- For example a proton beam hitting a target

## Muon beam

- From the decay of a pion beam in a straight beampipe

# Charged particles in electromagnetic fields

Electromagnetic force:

$$F = q E + \underbrace{q \cdot v \times B}$$

$\perp v$ , does not make work

- Acceleration:
  - **Electric field (always!!!)**
  - **But:** electric field can be produced by induction:  $\nabla \times E = -\frac{\partial B}{\partial t}$   
and not only by charges:  $\nabla \cdot E = \rho / \epsilon_0$
- Bending, focusing (i.e. transverse manipulation):
  - Magnetic field: proportional to velocity  $\rightarrow$  automatically increases with energy, without increasing B.  
(we still need to increase B if we need same orbit:  
 $F = m \cdot a = m \cdot v^2 / R$ ,  $B \cdot R = p / q$  )  
**Always use B at high energies**
  - Electric field
    - Useful at low energies ( $E_{\text{kin}} \sim 100$  keV): 1-10 kV for beam manipulation
    - Simple electrodes, cheap voltage sources
    - Electrostatic beamlines typically used for atomic physics experiments, radioactive beams, etc
    - The RFQ (see later) also uses electric field



# Charged particles in electromagnetic fields

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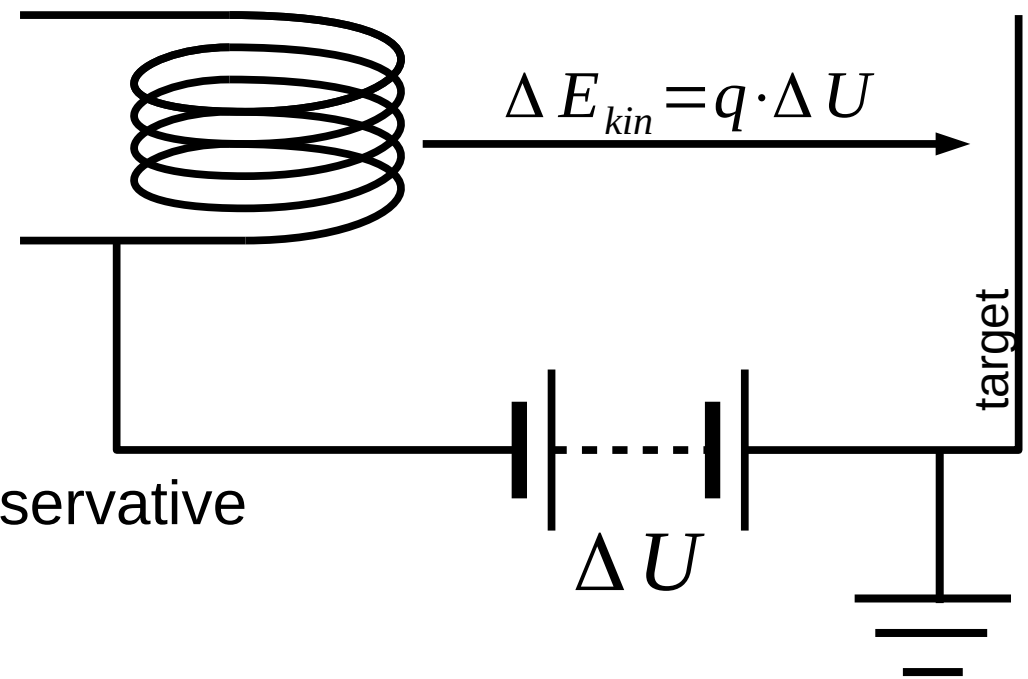
Useful conversion (E = 100 kV) : 1 T  $\leftrightarrow$  300 MV/m

- Magnets for bending, focusing
- Electric field for acceleration

# Electrostatic acceleration

# Electrostatic acceleration

- Target or source at high voltage (MV), other one typically grounded (exception: tandem...)
- Single-pass (can not reuse same electric field by guiding the beam through it again), since electro**static** field is conservative



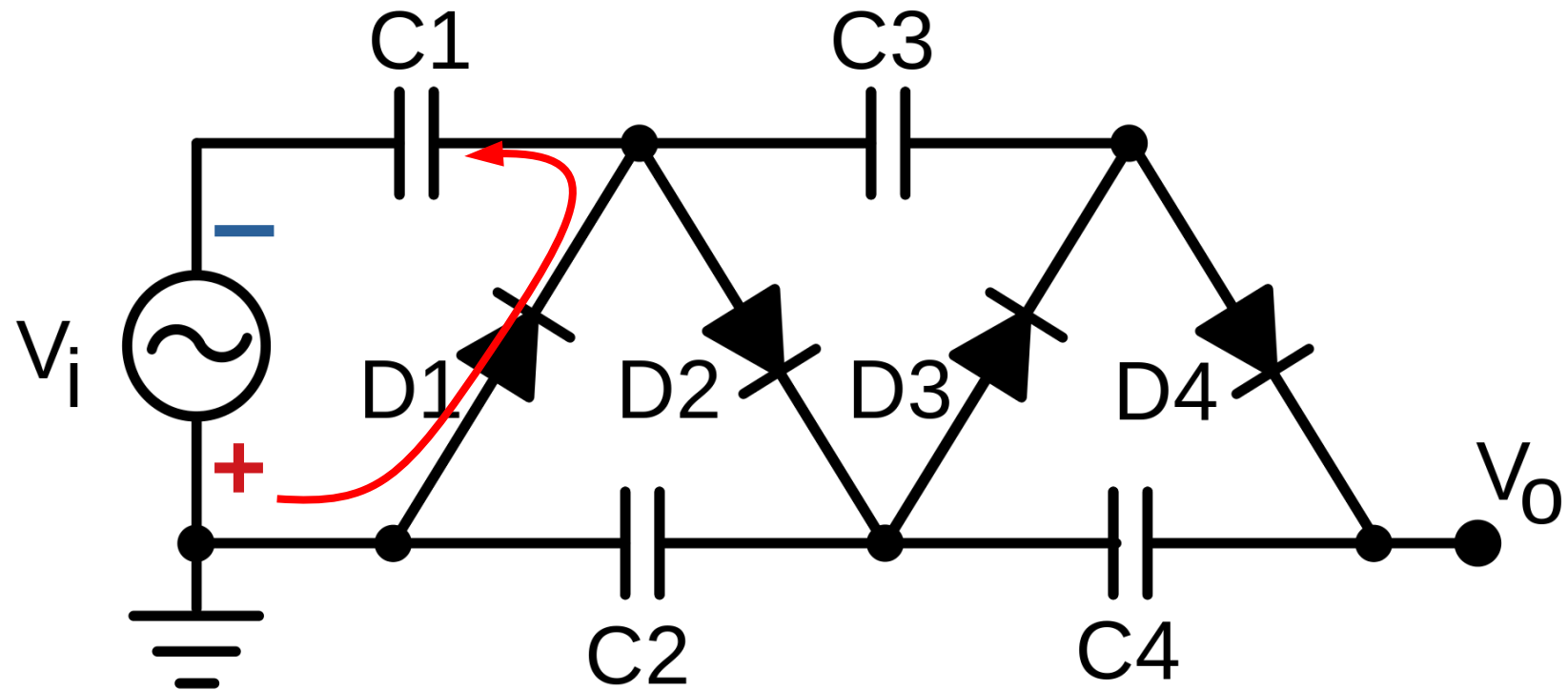
$$\oint E \, ds = 0$$

- HV generators
  - Cockroft-Walton (~MeV)
  - Van de Graaff (~10 MeV)
- Limit: electric breakdown, sparking, size of insulation

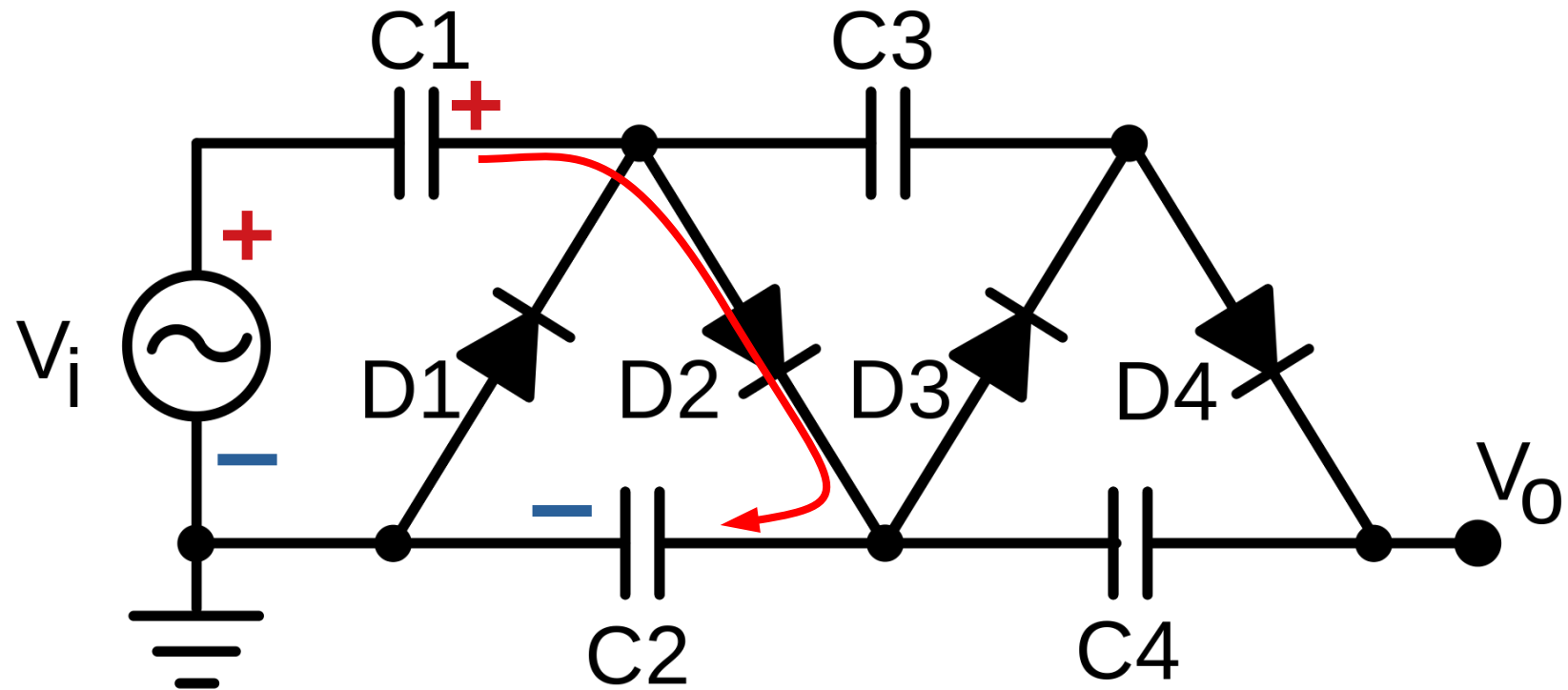
# Cockroft-Walton accelerator



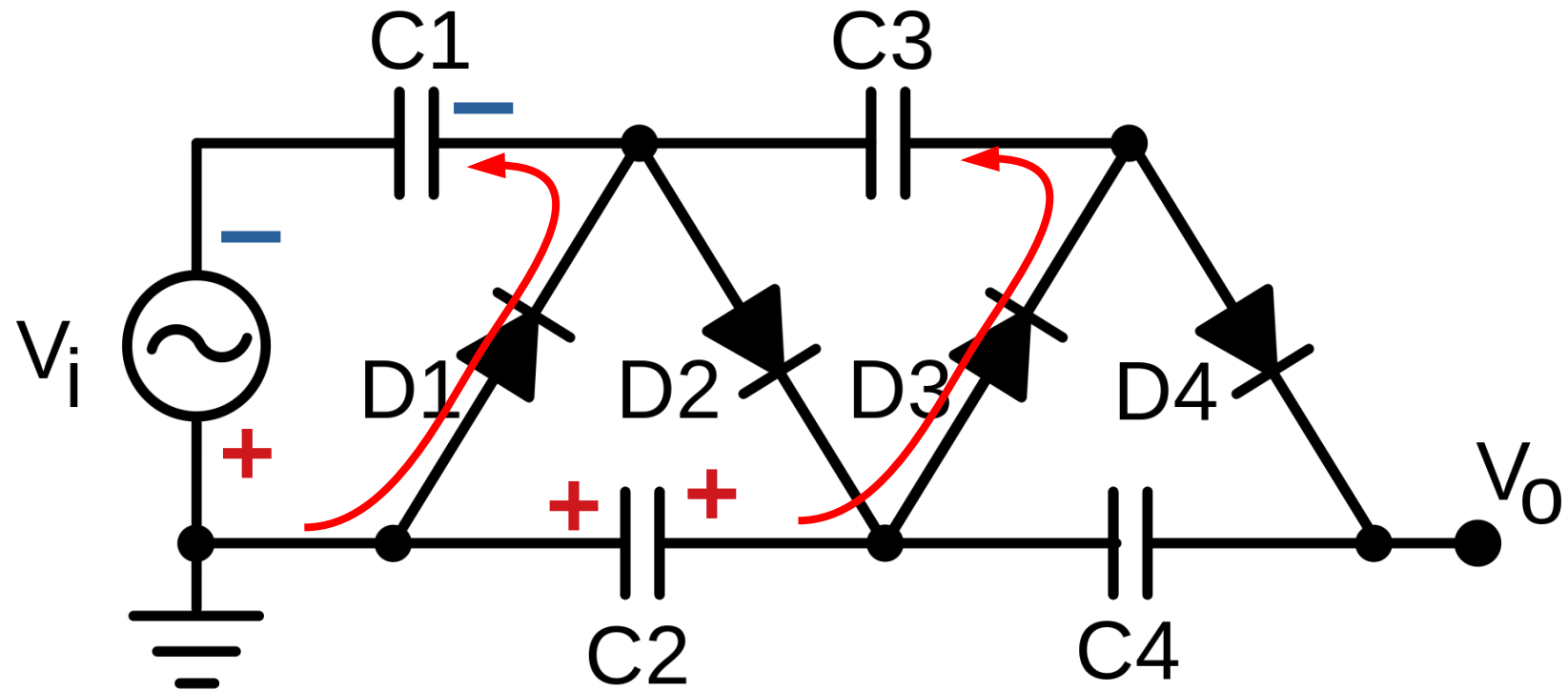
# Cockroft-Walton accelerator



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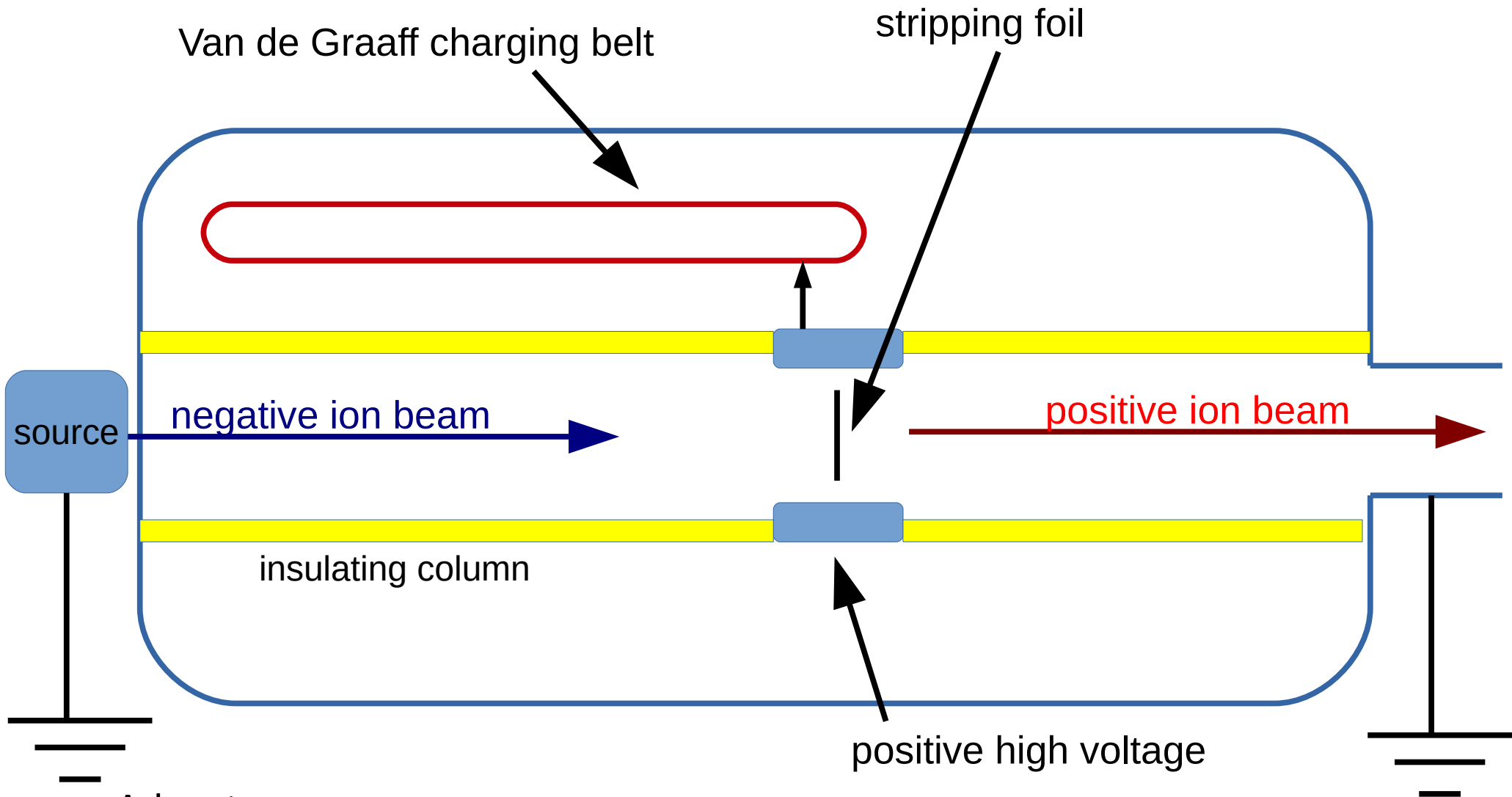
# Van de Graaff accelerator



Often times vertical (unlike this) to avoid gravitational load on long insulating column



# Tandem Van de Graaff



Advantages:

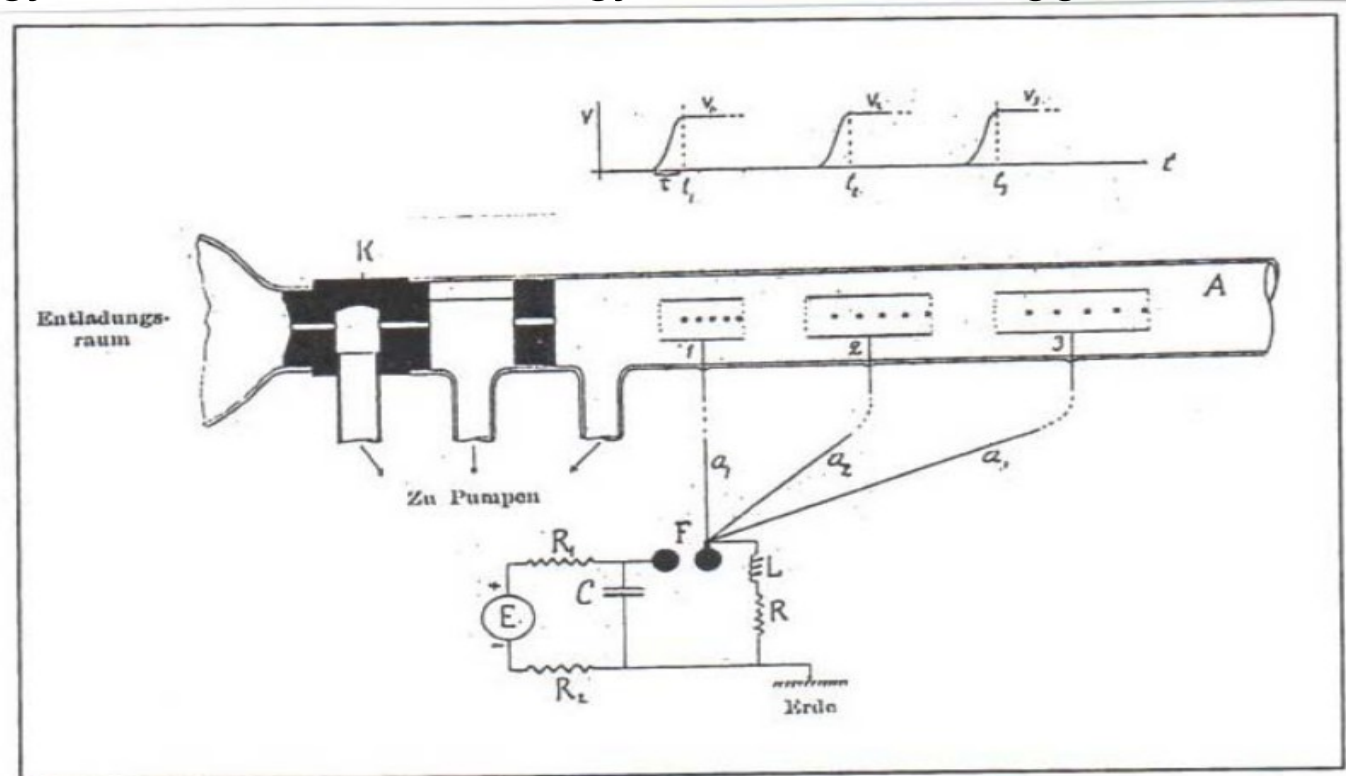
- Double output energy for same high voltage
- Source and target can be grounded

Changing electromagnetic fields:  
1) Linear accelerators (LINAC)

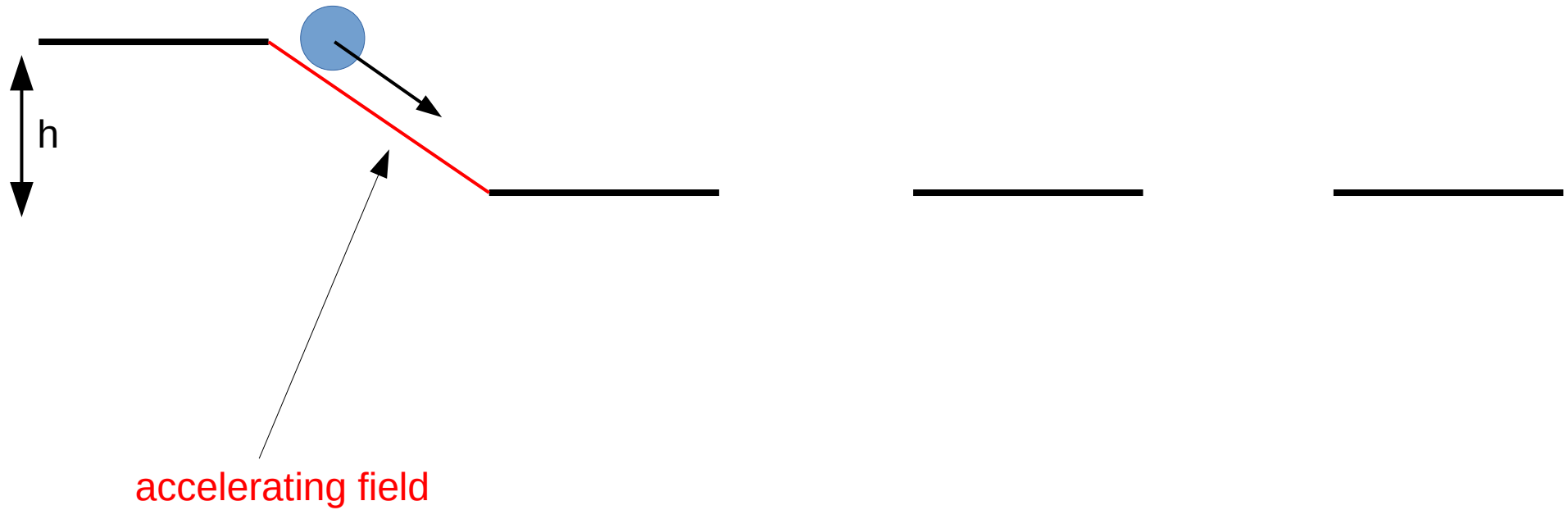
# Pulsed drift tube linac

Ising, 1924 – koncepció

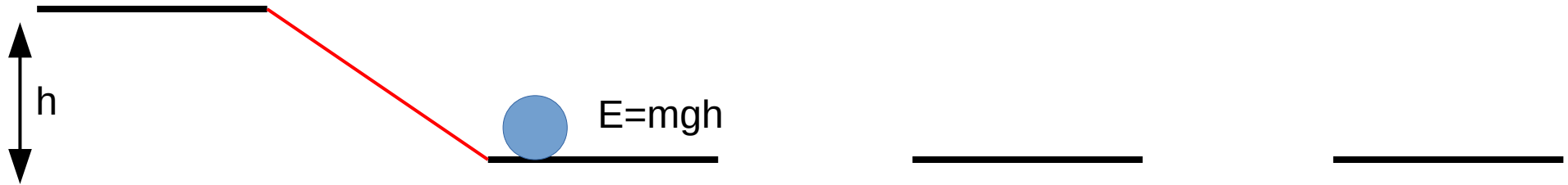
- Nem szükséges, hogy a teljes gyorsító tér egyidőben rendelkezésre álljon (átütés veszélye...), elég épp ott, ahol a részecske van (az elektromos tér gyorsít, nem a “potenciál”...)
- (Váltakozó EM térben nincs definiálva a potenciál!)
- Egyetlen fokozat helyett sok kisebb fokozat
- Jól időzített pulzusokkal (amíg a részecske a csövön belül van)
- csövek közötti rés gyorsít, csövek hossza egyre nő a sebességgel



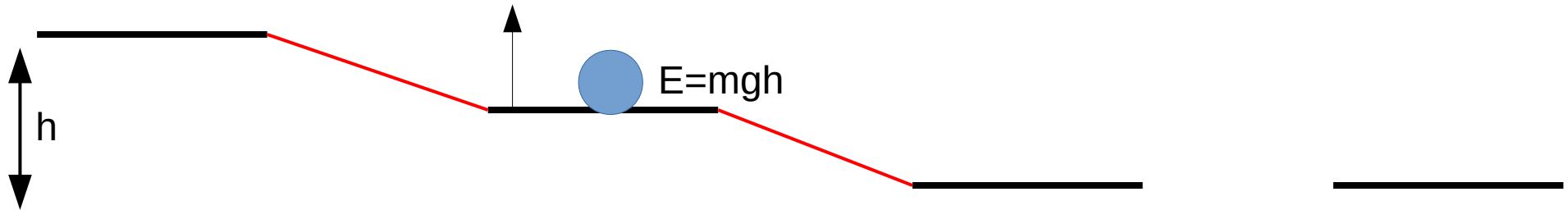
# Pulsed drift tube linac



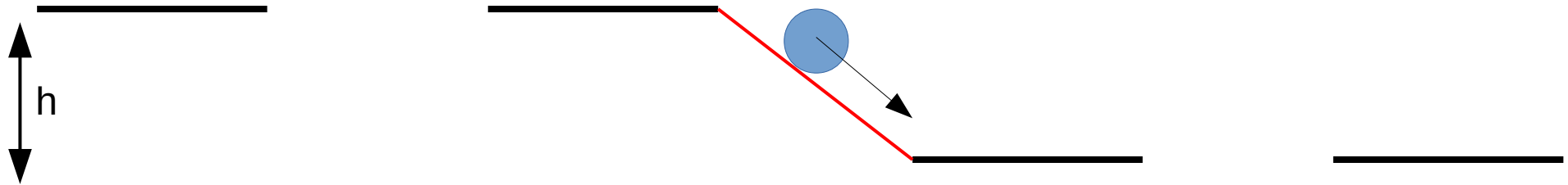
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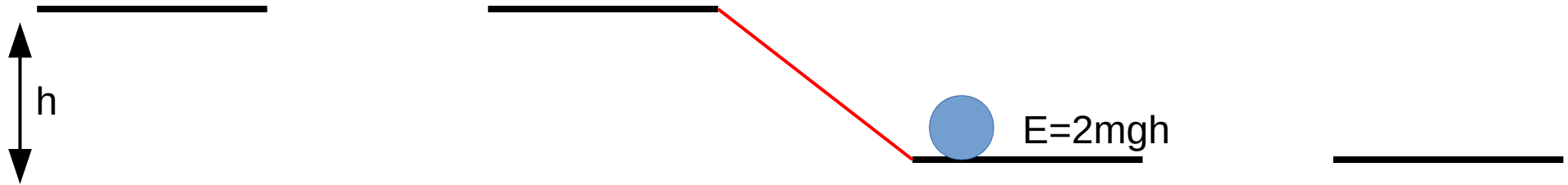
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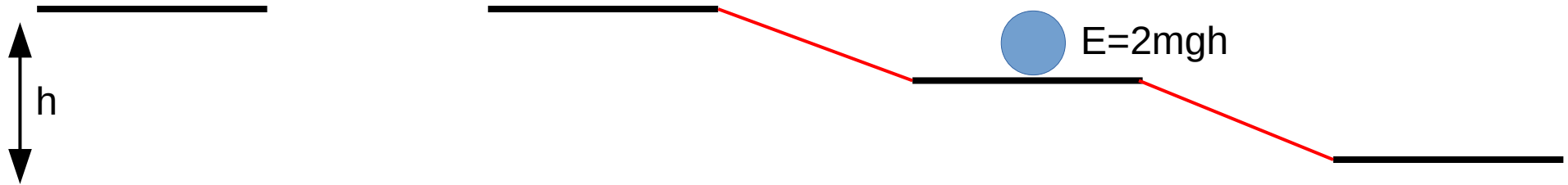


# Pulsed drift tube linac





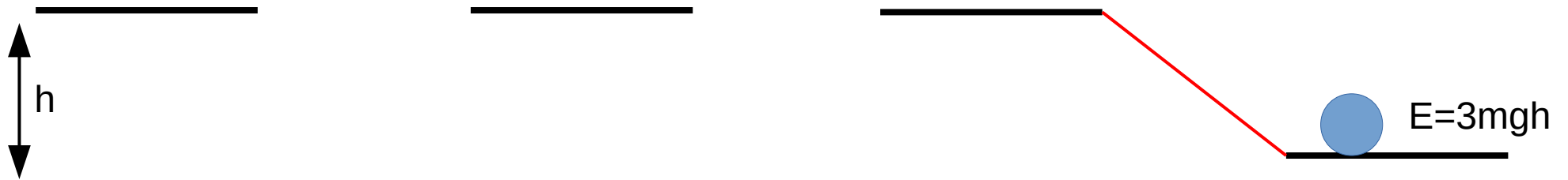
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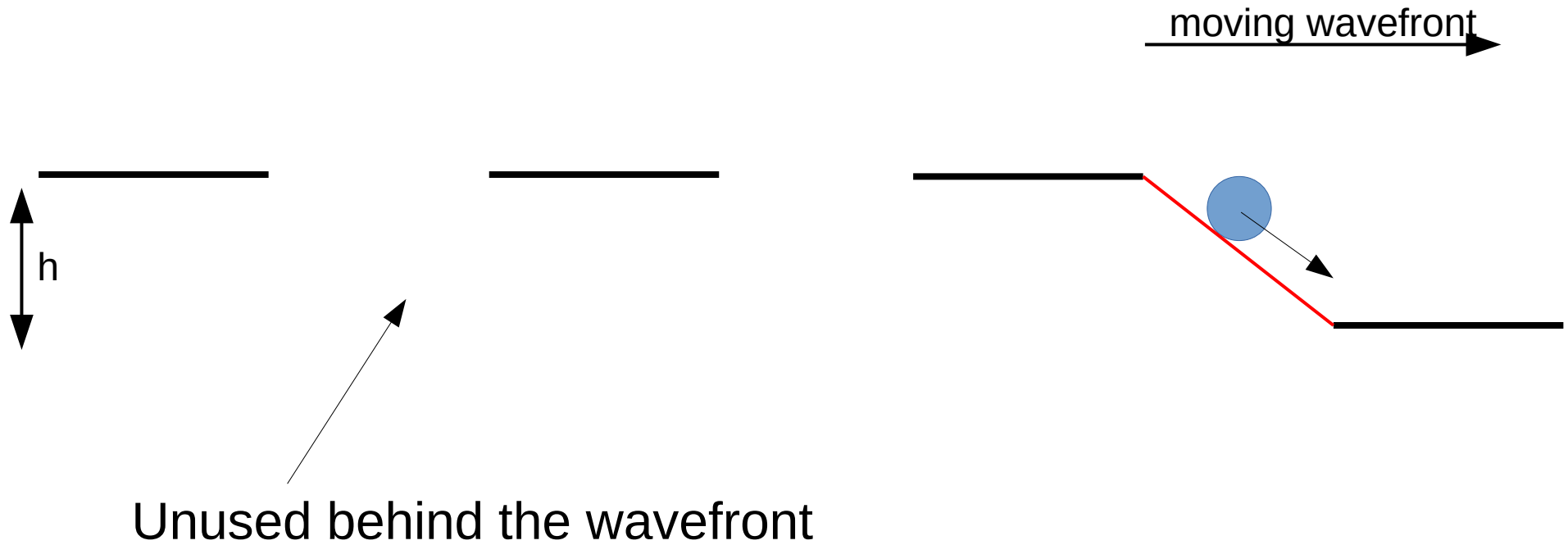
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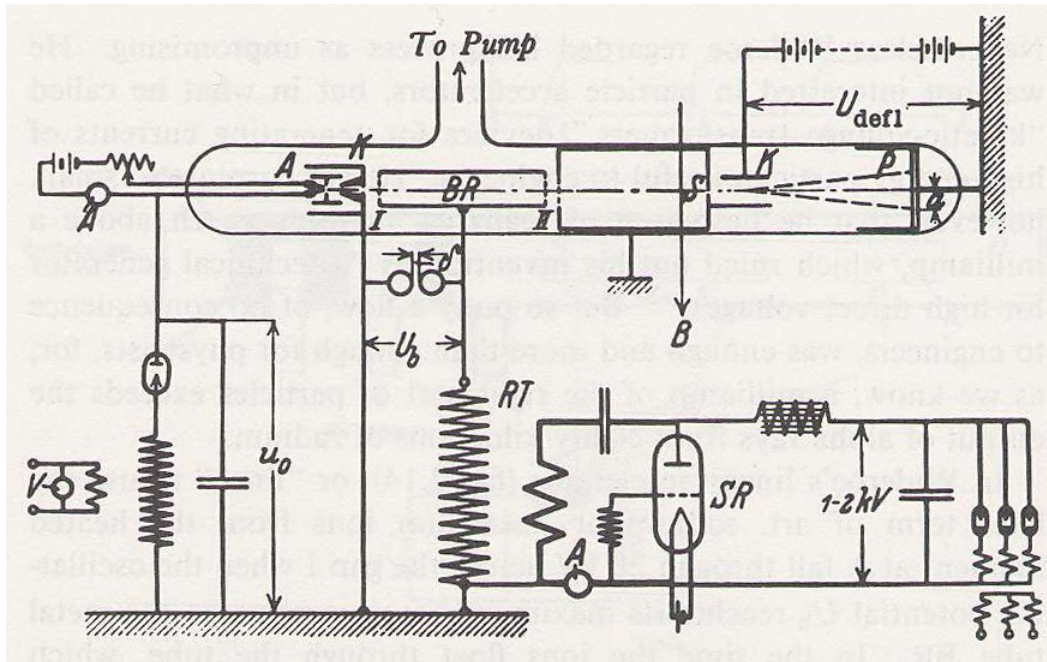
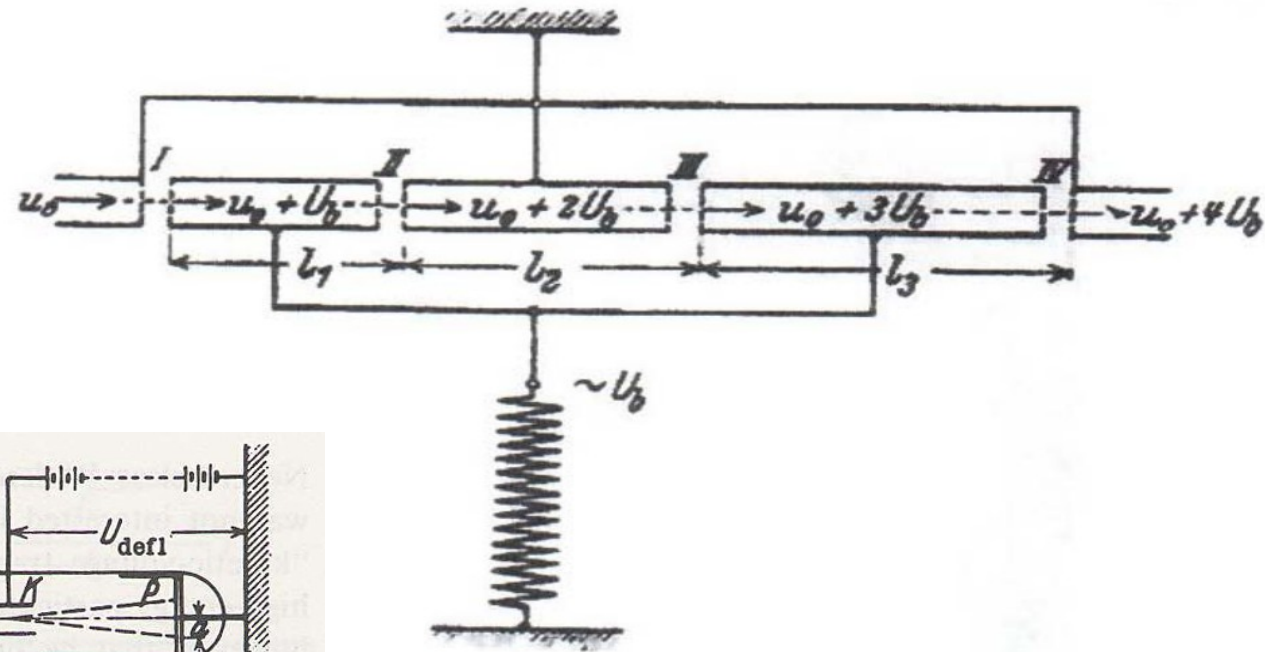


# Wideröe RF linac

Wideröe (1928):

Use RF instead of timed pulses!

RF changes  $180^\circ$  while particle reaches next gap

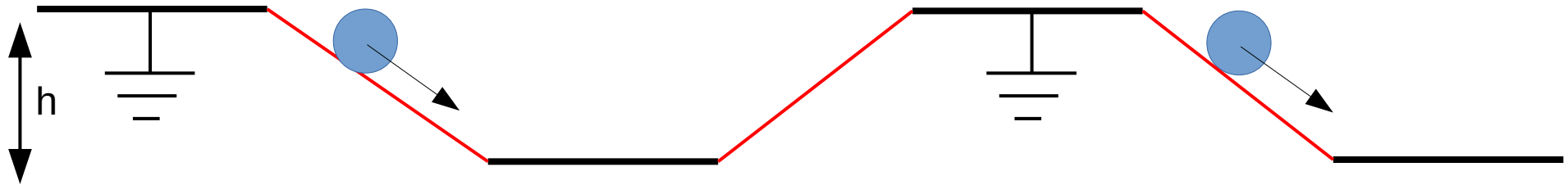


- PhD thesis: construction of a 3 tubes (2 gaps) accelerator  
2 x 25=50 keV

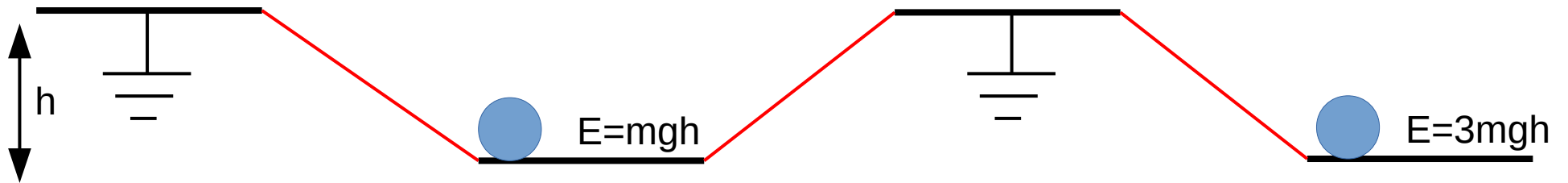
## • Limitations

- Before world war 2: only low RF frequency available → need long drift tubes ( $L = v/f_{RF}$ )
- WW2 radar R&D: high RF frequencies → open drift tubes radiate as antennas

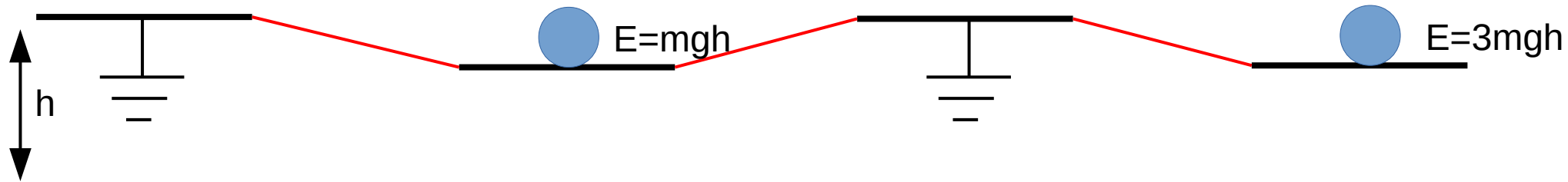
# RF linac



# RF linac

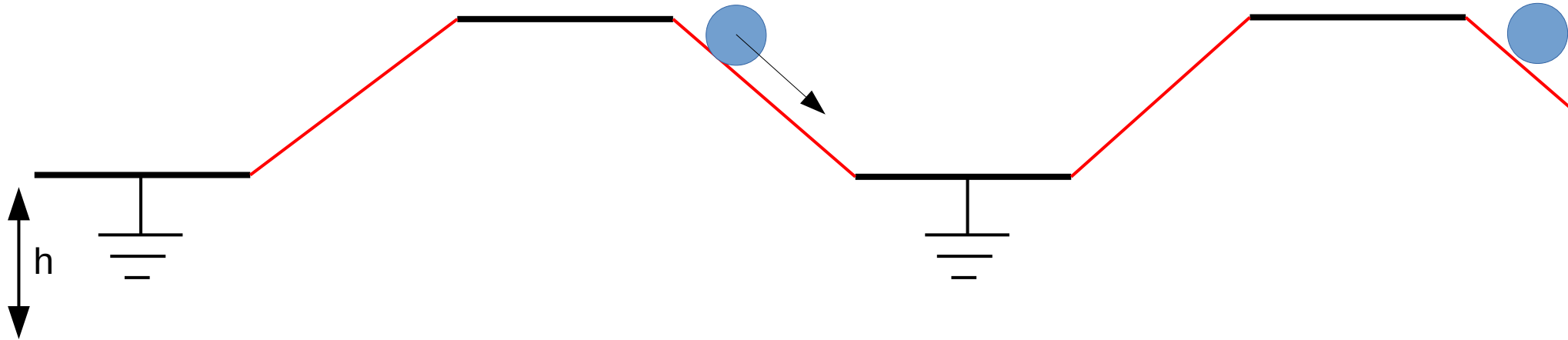


# RF linac



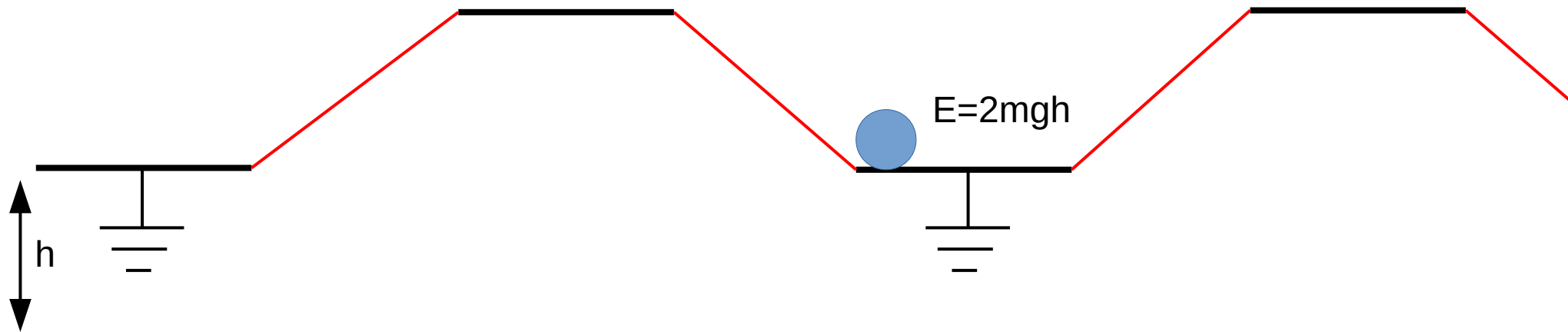


# RF linac



Standing wave!

# RF linac

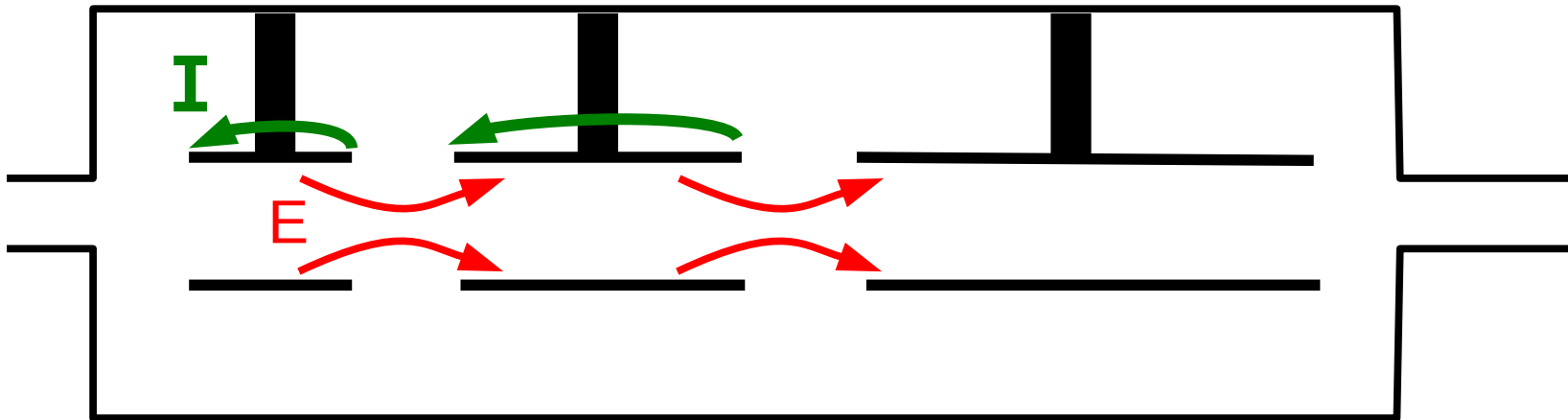


Standing wave!

<http://wigner.mta.hu/~barna/content/Lectures/Illustration of RF acceleration principle.webm>

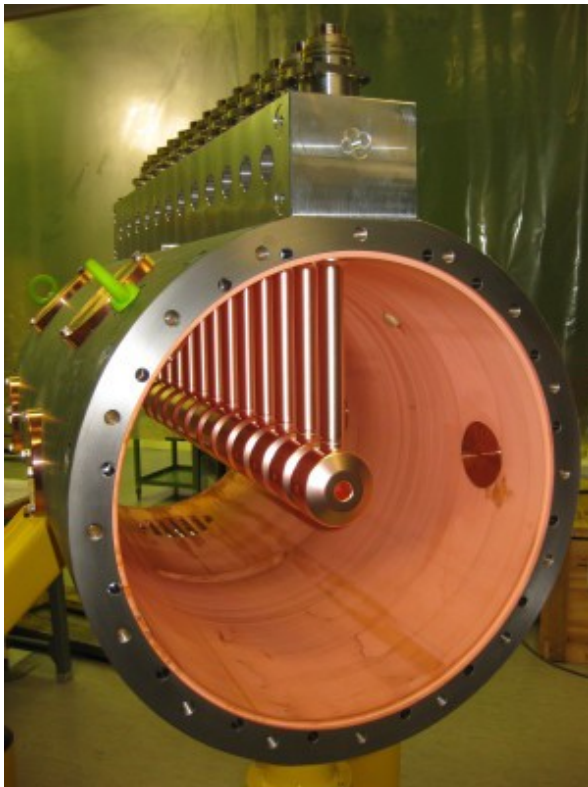
# Alvarez linac

- Alvarez (1946)
  - Grounded electrodes of Wideröe connected to other RF pole
  - Accelerating structure can be transformed into a closed resonator cavity
  - EM standing wave within a closed resonator
  - Resonator → no radiative losses



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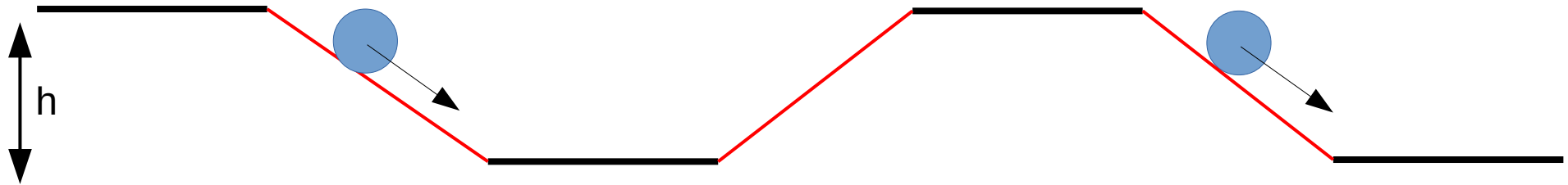
CERN Linac4 – 50 MeV



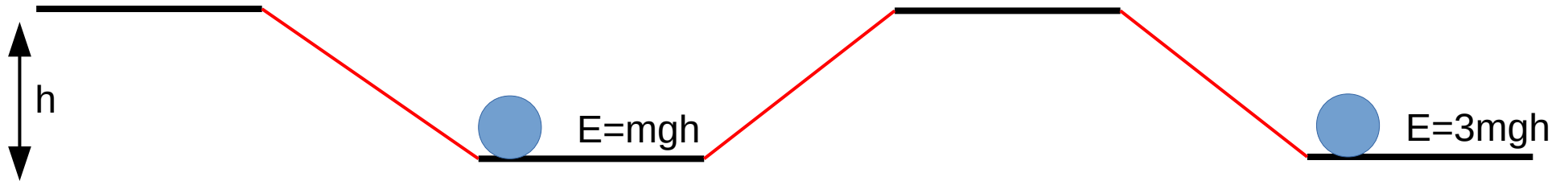
Lawrence Berkeley National Lab (LBNL), 1957

- Can be individual accelerators...
- ... or injectors into rings

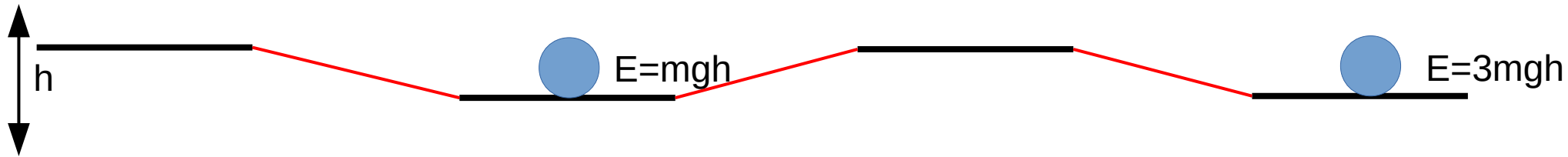
# Alvarez linac



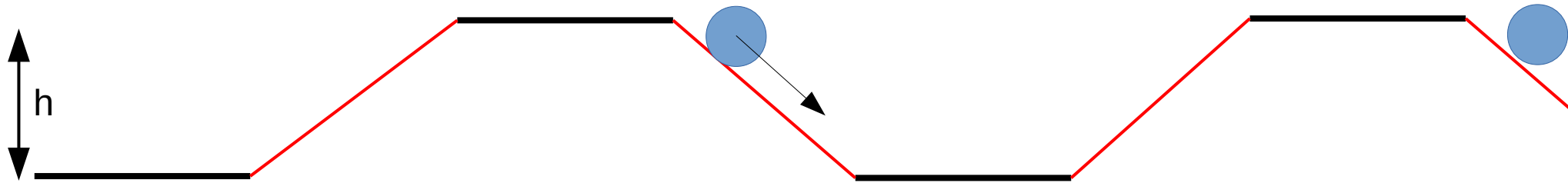
# Alvarez linac



# Alvarez linac



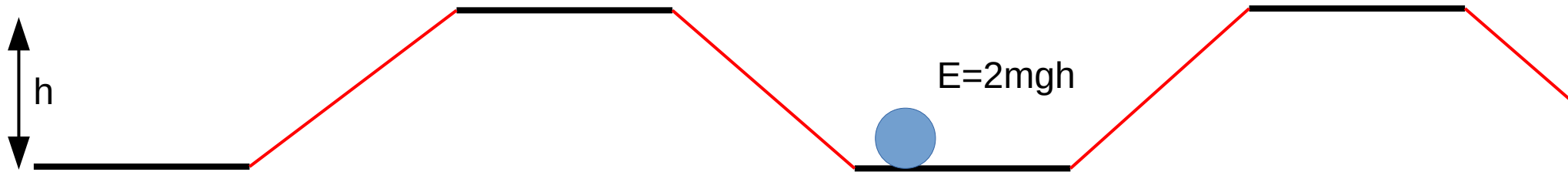
# Alvarez linac



Standing wave!



# Alvarez linac



Standing wave!

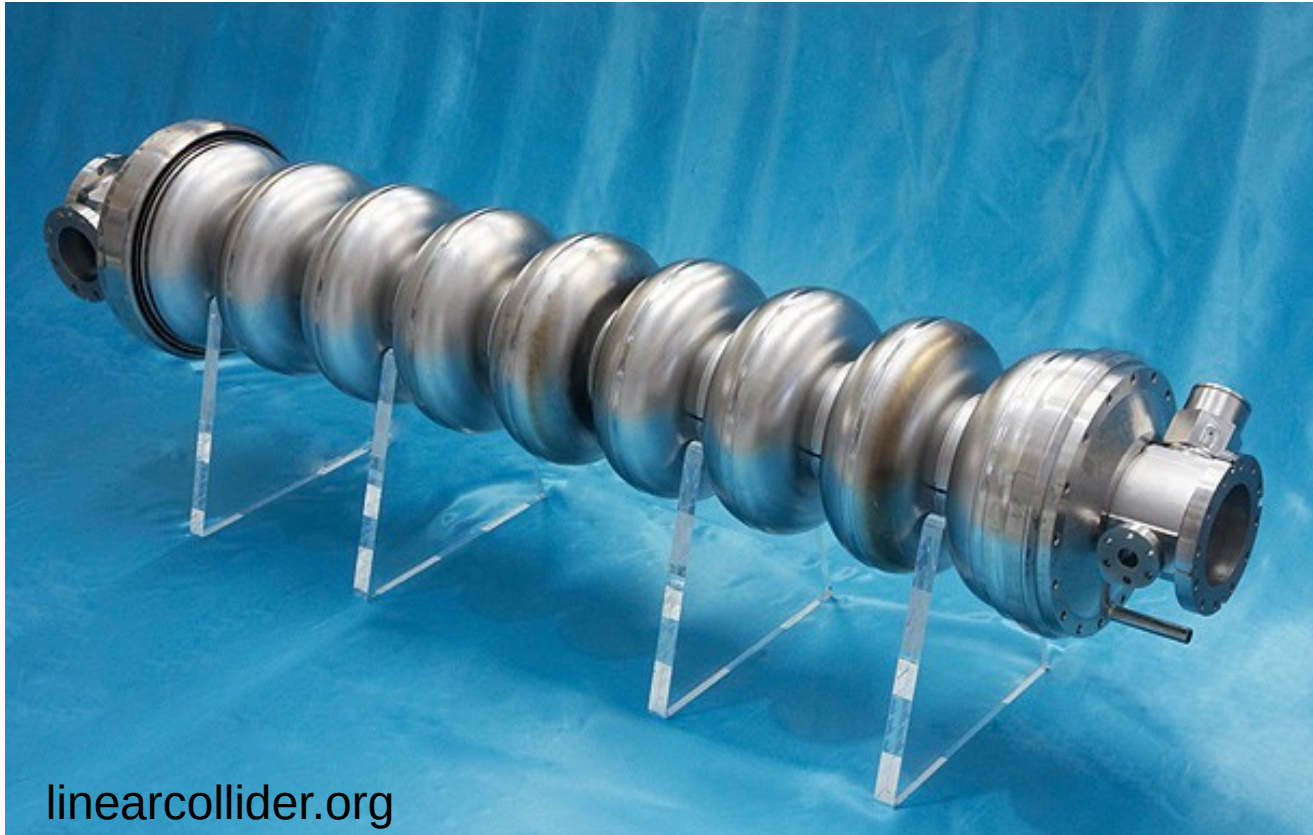
[http://wigner.mta.hu/~barna/content/Lectures/Illustration of RF acceleration principle.webm](http://wigner.mta.hu/~barna/content/Lectures/Illustration%20of%20RF%20acceleration%20principle.webm)

# Alvarez linac

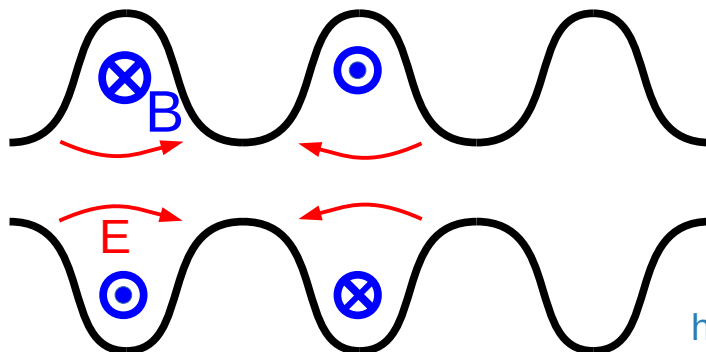


CERN Linac2 (protons, 50 MeV)

# Tesla cavity



- Normalconducting (e.g. LEP initially)
- Superconducting (LEP upgrade, LHC, etc)



$\pi$ -mode: (E-field with  $180^\circ$  phase diff. in neighbouring cells)

[https://wigner.mta.hu/~barna/content/Lectures/Tesla cavity illustration.webm](https://wigner.mta.hu/~barna/content/Lectures/Tesla%20cavity%20illustration.webm)

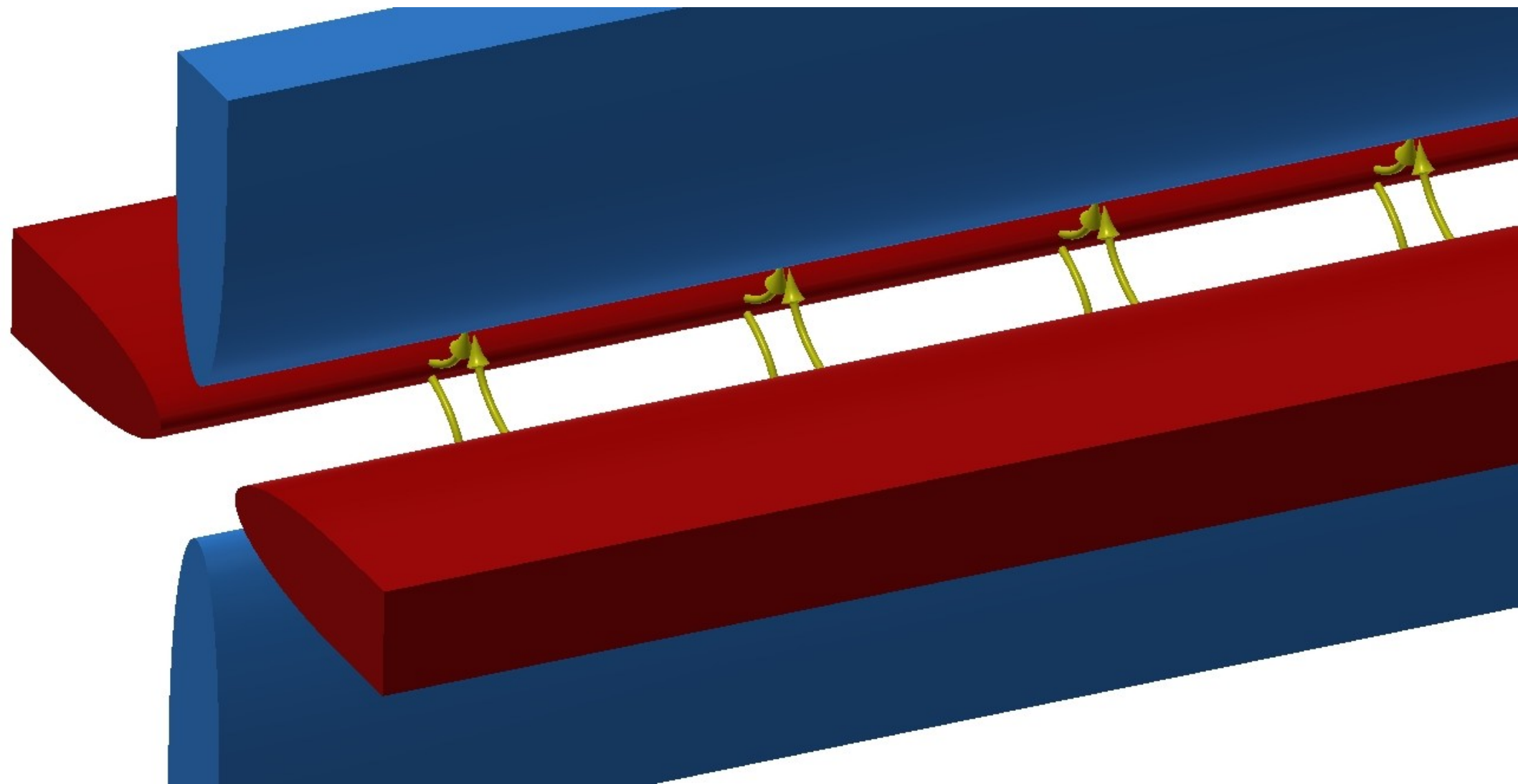
# RadioFrequency Quadrupole (RFQ)

- Kapchinskij, Teplyakov (1970)
- First operational RFQ: 1974, input: 100 keV output: 620 keV (50% eff)
- Western countries learn about it only in 1977(!) (cold war times...)  
1980: Los Alamos, 100 --> 640 keV, 90%
- Invented later than the other components reviewed so far, but it is used at an intermediate stage at lower energies:  
typical intermediate component **between ion source and drift-tube linac**.  
Increases transport/capture efficiency (adiabatic bunching – see later)
- Combined machine for 3 functions
  - 1) Focusing
  - 2) Acceleration
  - 3) Bunching
- Uses only E field for all functions
- Delivers bunched DC beam (i.e. continuous output with a microstructure = RF)

# RadioFrequency Quadrupole (RFQ)

## 1) Focusing (by the electric field!)

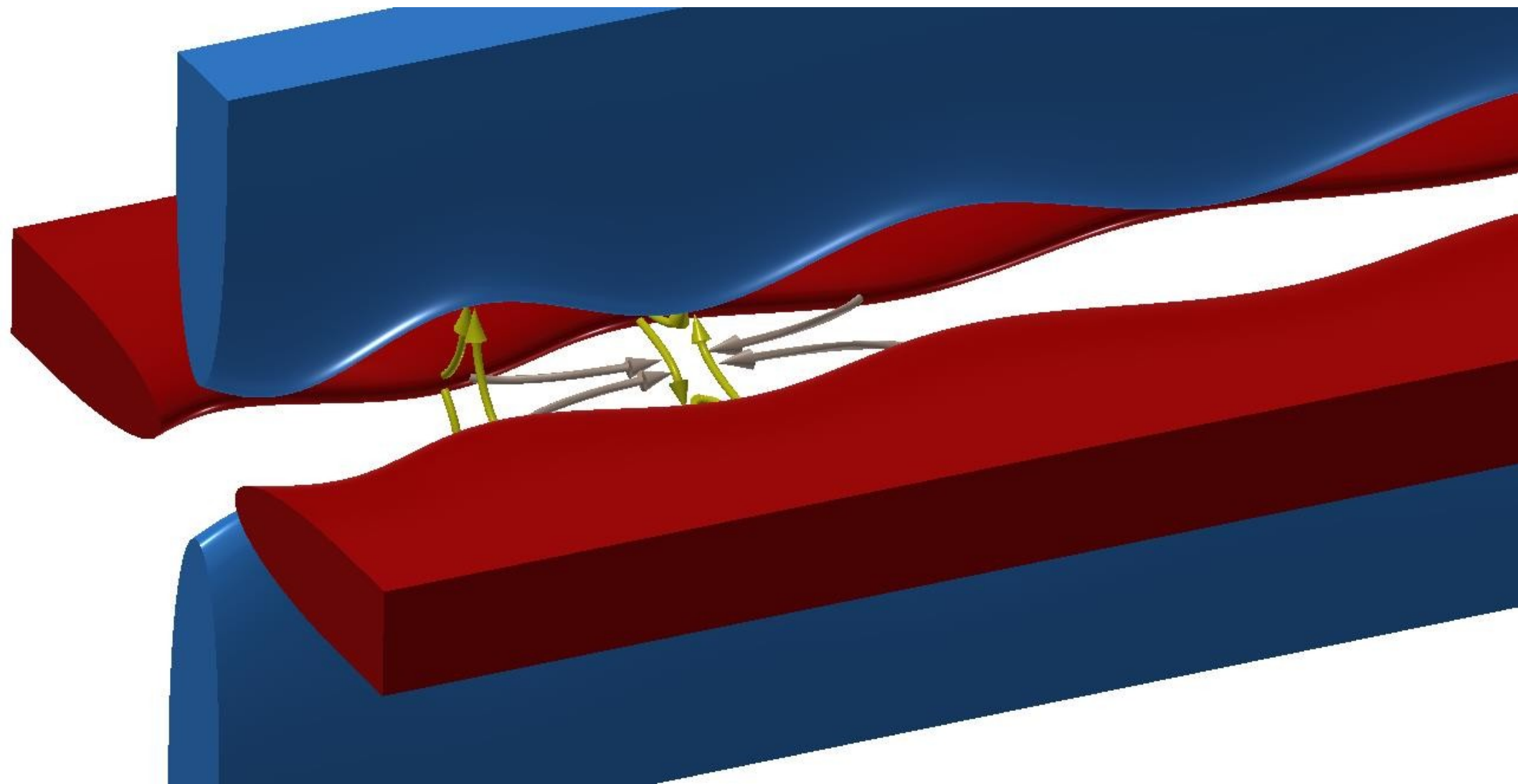
- Transverse quadrupole electric field focuses in one plane, defocuses in other
- If this alternates in time: net focusing in both planes ( $\leftarrow$  ponderomotive force) (cf. Paul trap, AGS/strong focusing) – ask now rather than at the exam!



# RadioFrequency Quadrupole (RFQ)

## 2) Acceleration

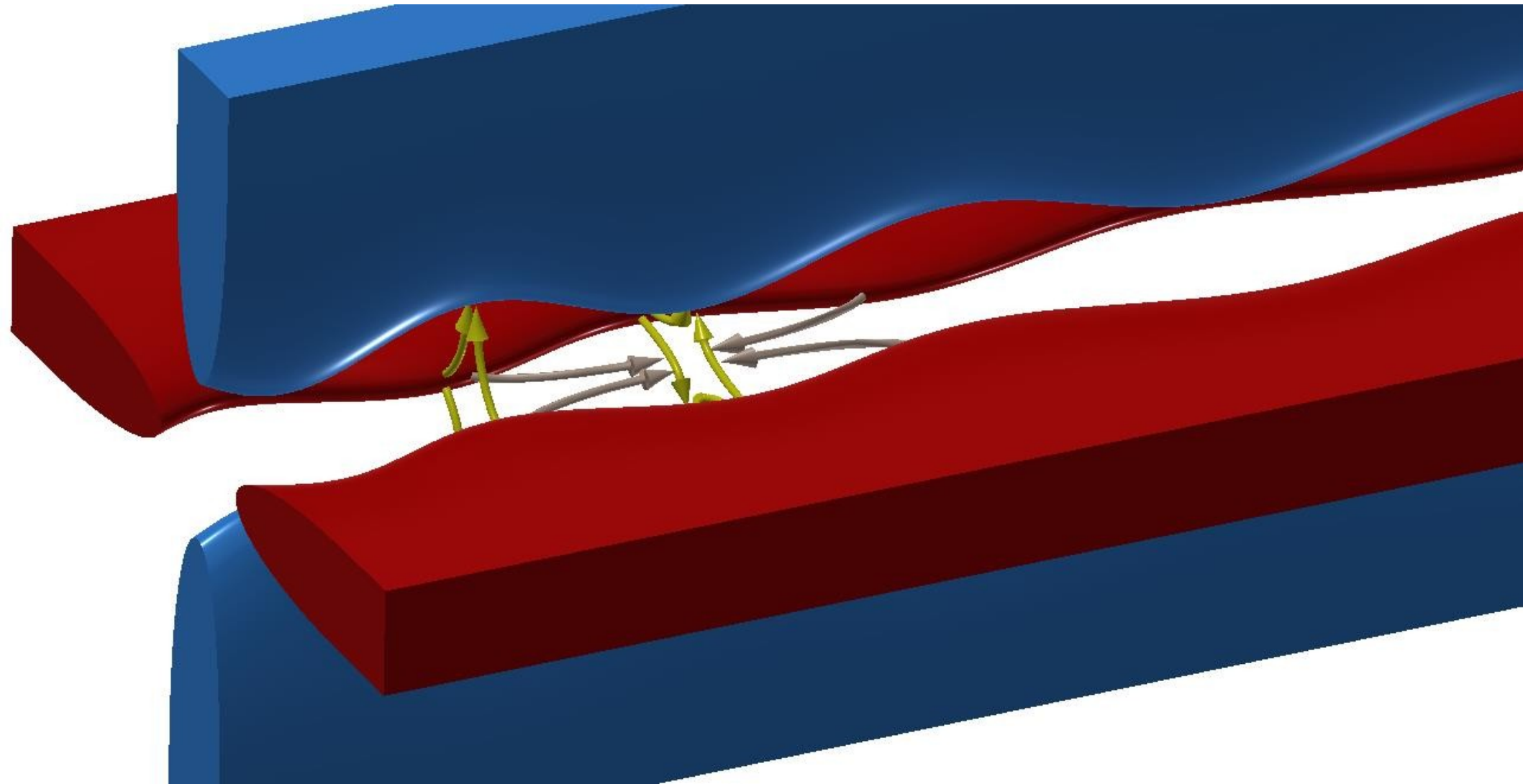
- Longitudinal electrode shape modulation (180° diff between x/y electrodes)
- Alternating longitudinal **electric** field component, accelerates only particles at correct phase



# RadioFrequency Quadrupole (RFQ)

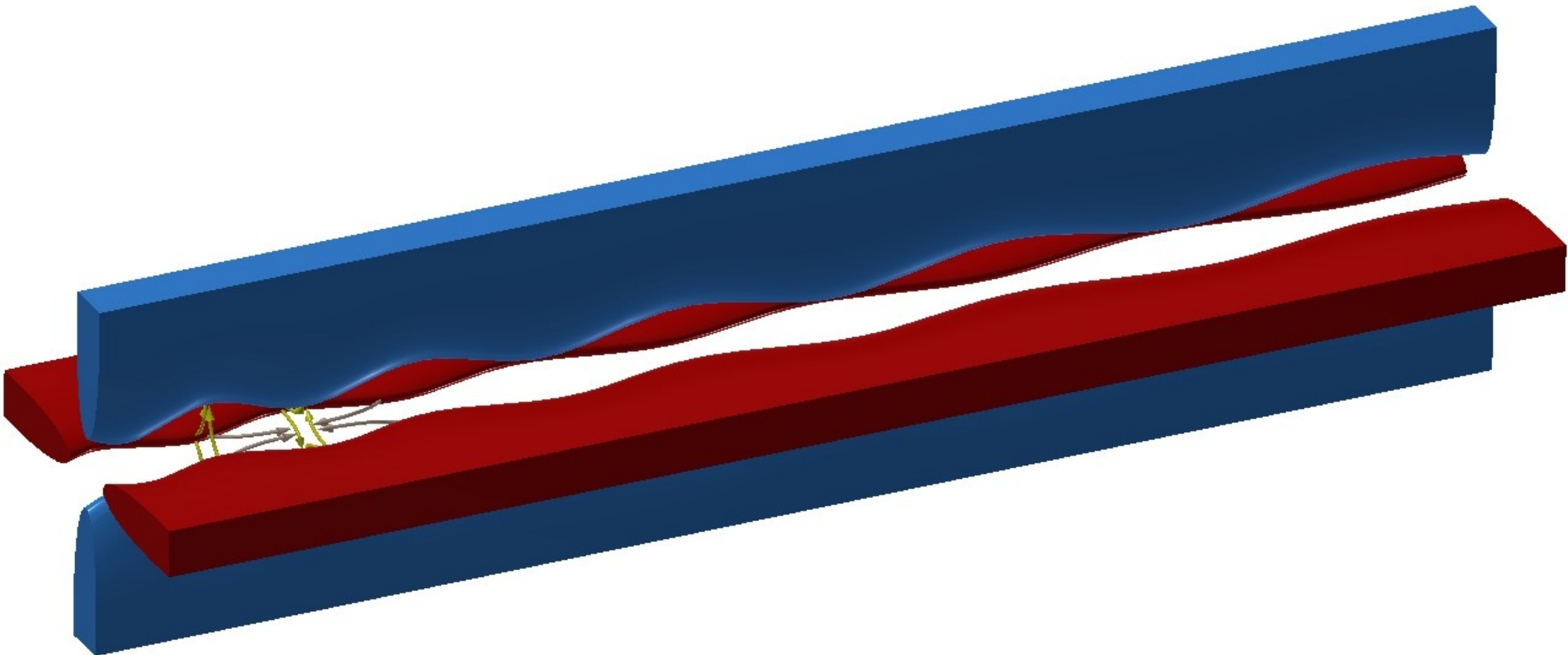
## 3) Bunching

- Accelerates only in correct phase
- Bunches the particles “adiabatically”:
- Electrode modulation “slowly” developing from input to output



# RadioFrequency Quadrupole (RFQ)

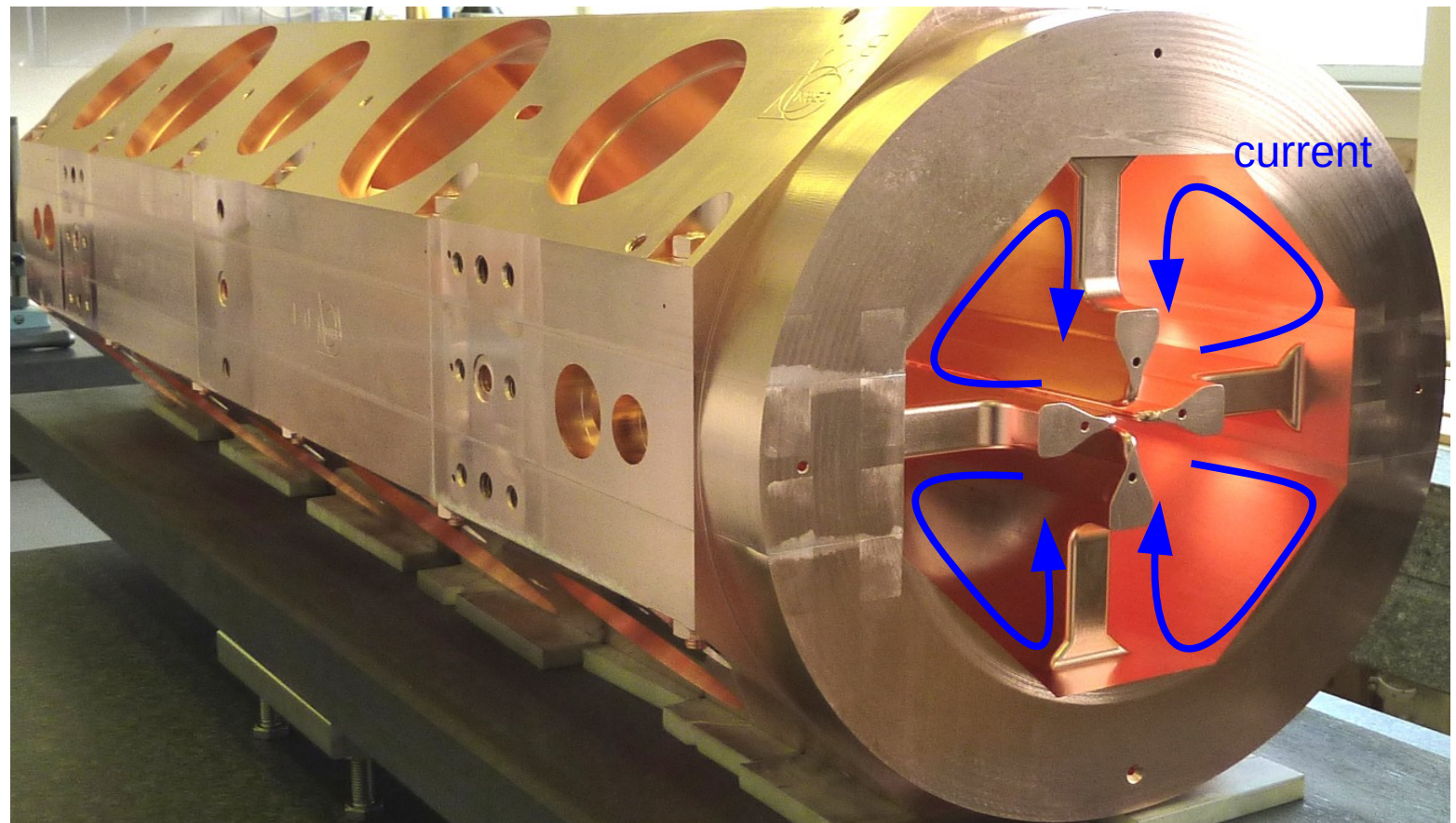
- Wavelength of electrode modulation changing in accordance with velocity of particles
- Manufactured by CNC (Computer Numerical Control) machines
- Electrode shape “adiabatically” changing from input to output (“slowly” captures the particles into bunches)





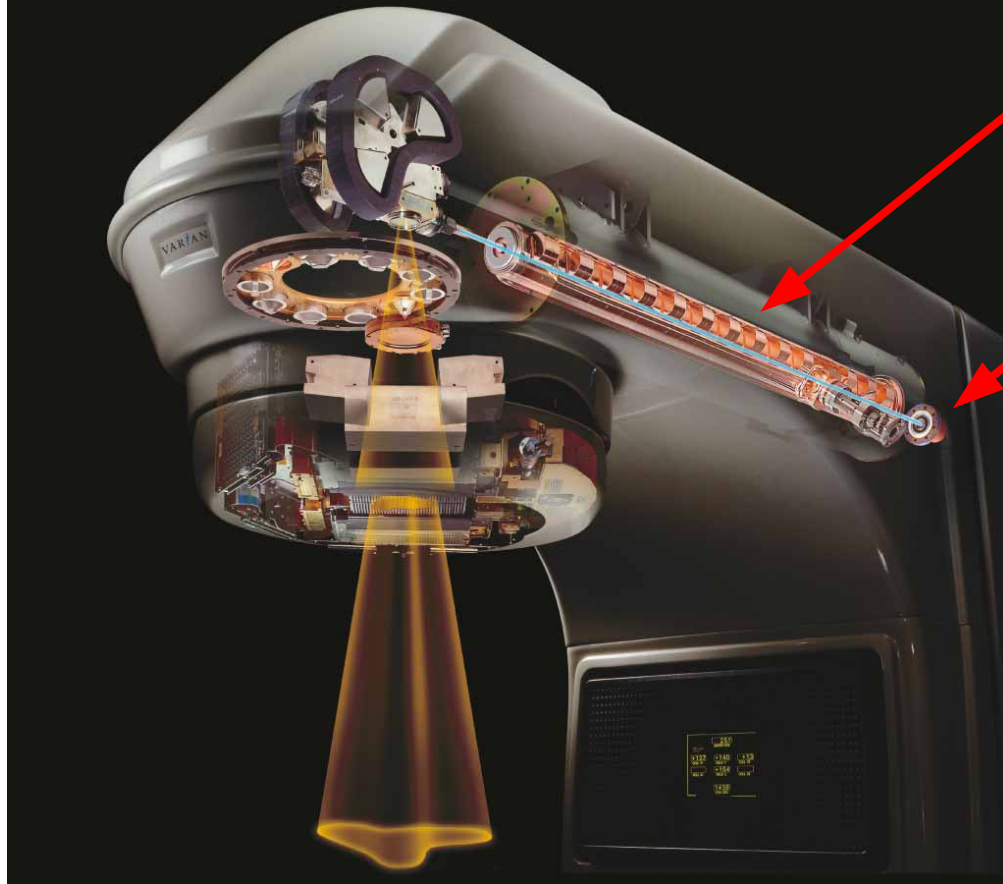
# RadioFrequency Quadrupole (RFQ)

- RFQ for LINAC4 (CERN – being commissioned):
  - protons
  - output energy: 3 MeV
  - 3 m length
  - Closed resonator
  - 78 kV between pole tips



# Linacs in our life

<http://www.cancercarelasvegas.com/wp-content/uploads/2017/05/linac1.jpg>



Linear electron accelerator

Electron gun



# Changing electromagnetic fields:

## 2) accelerator rings

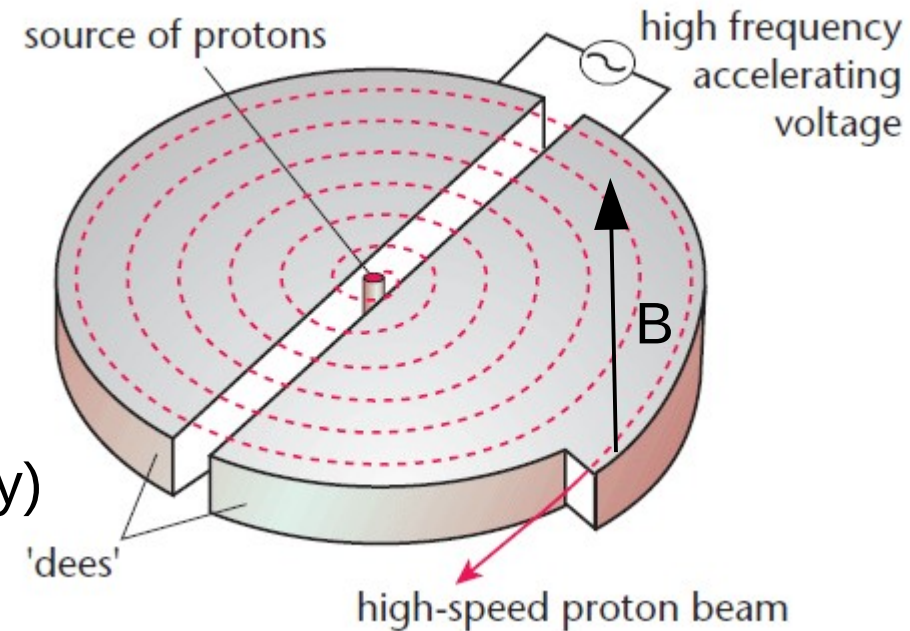
*“Let’s reuse the same accelerating structure several times by guiding the beam back to it using magnets”*

# Cyclotron

- Lawrence & Livingston (1931)
- Particle orbit is a circle in a constant field. Cyclotron radius increases proportionally to momentum:  $B \cdot R = p/q$
- In the **nonrelativistic** regime: revolution frequency (cyclotron frequency) is energy-independent:

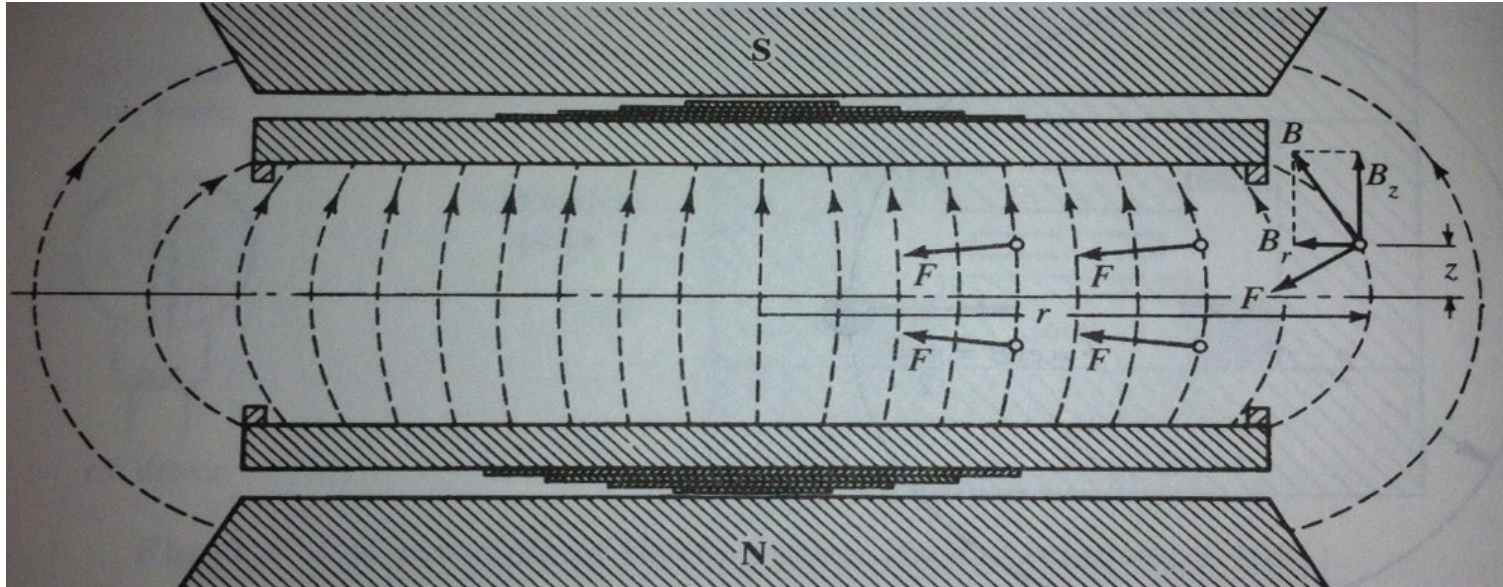
$$f_{cyc} = \frac{v}{2\pi R} = \frac{v}{2\pi} \cdot \frac{qB}{p} = \frac{qB}{2\pi} \frac{v}{p} = \frac{qB}{2\pi} \frac{1}{m}$$

- Cyclotron resonance: frequency of E-field between two D electrodes equals cyclotron frequency:  $f_{RF} = f_{cyc}$
- In this case: E accelerates at each passage through gap
- DC (continuous) beam, with a microstructure matching the RF



# Cyclotron

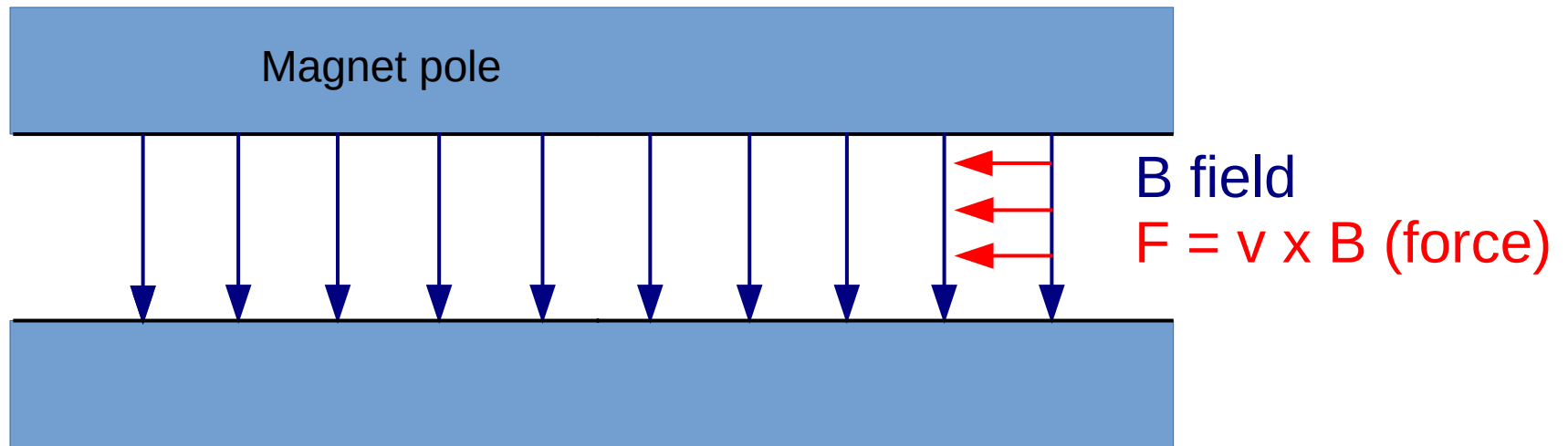
- How can it be that particles are not lost over a lot of cycles, even though they are not parallel?
- McMillan: played with the magnetic field (using pole shims) → suddenly the output current increased



(E. Wilson: An introduction to particle accelerators)

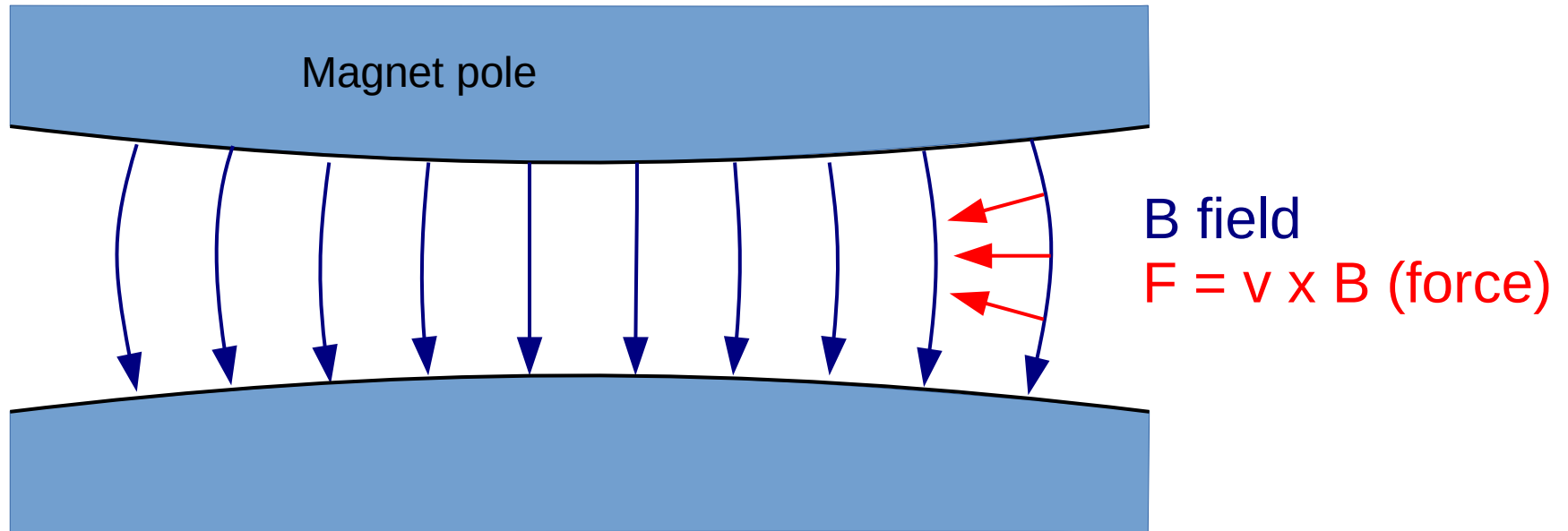
- Horizontal B component → vertical focusing or defocusing
- Focusing if B has the right curvature ↔ decreases outwards  
If B increases outwards → defocusing
- Horizontal focusing might get messed up if B decreases too fast outwards  
(see later: weak focusing)

# Weak focusing – preliminary



- At iron-air boundary, B field in air is perpendicular to iron surface (homework: why? hint:  $\mu_r \sim 3-4000$  for iron)
- The larger the gap between the poles, the weaker the field

# Weak focusing – preliminary



- At iron-air boundary, B field in air is perpendicular to iron surface (homework: why? hint:  $\mu_r \sim 3-4000$  for iron)
- The larger the gap between the poles, the weaker the field

**The “good field” (focusing in the vertical direction) must decrease with increasing radius!**

# Cyclotron: relativistic limit

$$f_{cyc} = \frac{v}{2\pi R} = \frac{qB}{2\pi} \cdot \frac{v}{p}$$

Substitute cyclotron radius:  $R = qB/p$



# Cyclotron: relativistic limit

$$f_{cyc} = \frac{v}{2\pi R} = \frac{qB}{2\pi} \cdot \frac{v}{p} = \frac{qB}{2\pi} \cdot \frac{1}{m}$$

Classic formula:  $p=mv$ , therefore  $v/p=1/m$   
and  $f_{cyc} = \text{const}$

# Cyclotron: relativistic limit

$$f_{cyc} = \frac{v}{2\pi R} = \frac{qB}{2\pi} \cdot \frac{v}{p} = \frac{qB}{2\pi} \cdot \frac{1}{m}$$

Classic formula:  $p=mv$ , therefore  $v/p=1/m$  and  $f_{cyc} = \text{const}$

- Relativistic formula (homework!): momentum (and proportionally R) increases, but velocity saturates to c

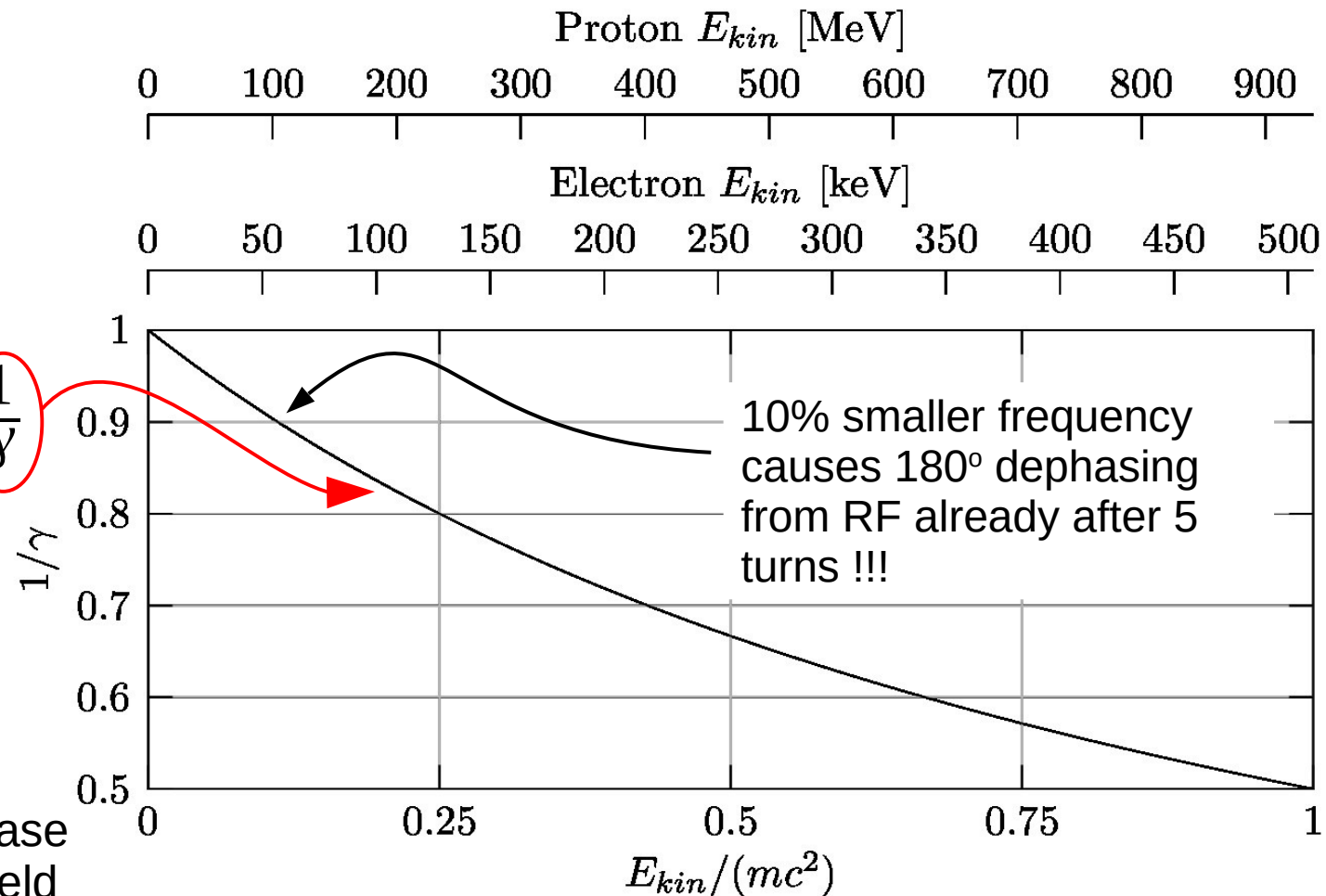
$$p = \frac{mv}{\sqrt{1-v^2/c^2}} = \gamma m v$$

$$\frac{v}{p} = \frac{1}{\gamma m}$$

$$f_{cyc} = \frac{qB}{2\pi m} \frac{1}{\gamma} = f_{cyc}^{class} \frac{1}{\gamma}$$

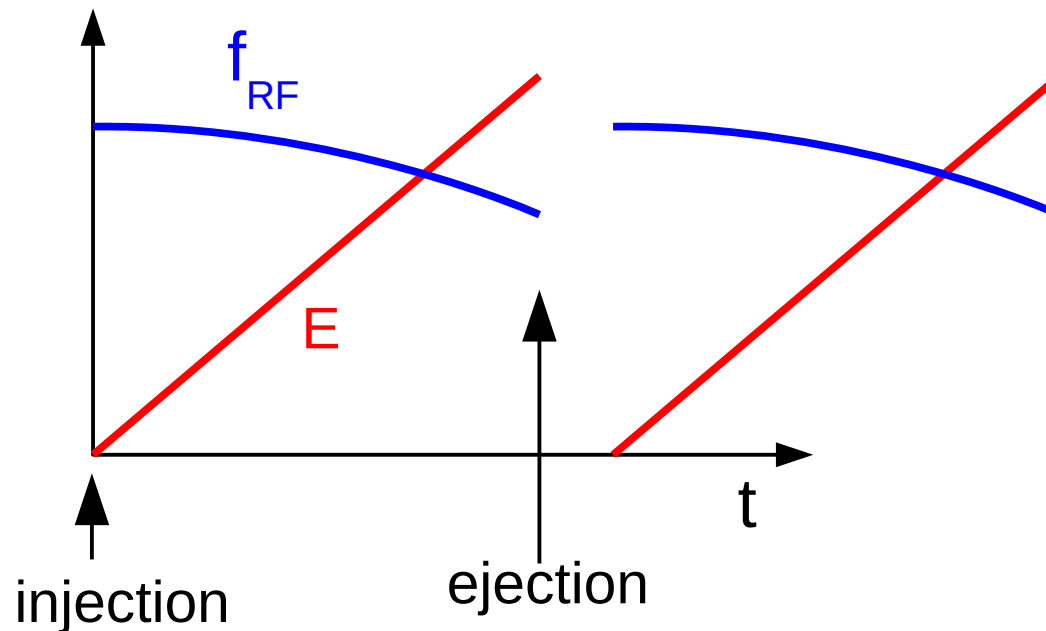
- Few% deviation already for few-10 MeV protons

- Particles get out-of-phase with accelerating RF field



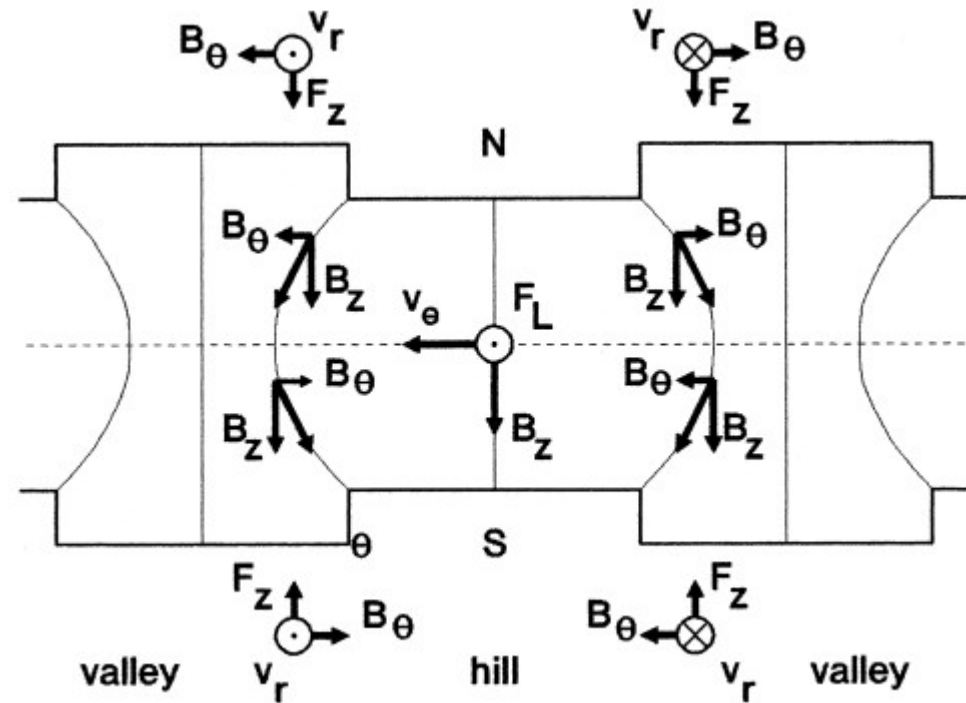
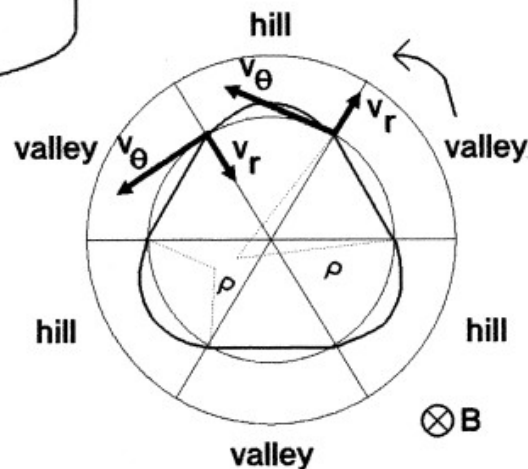
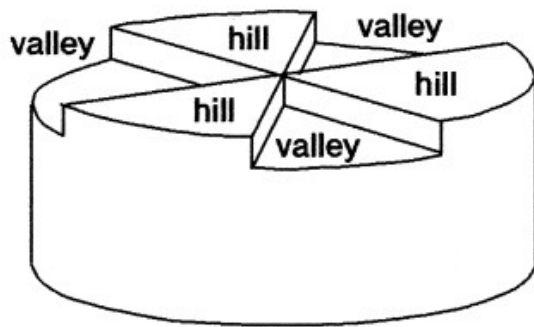
# Cyclotron: overcoming the relativistic limit #1

- **Synchro-cyclotron:** RF frequency ( $f_{RF}$ ) decreasing in sync. with increasing energy
- Cyclic (non-DC) operation. Delivers particle bunches



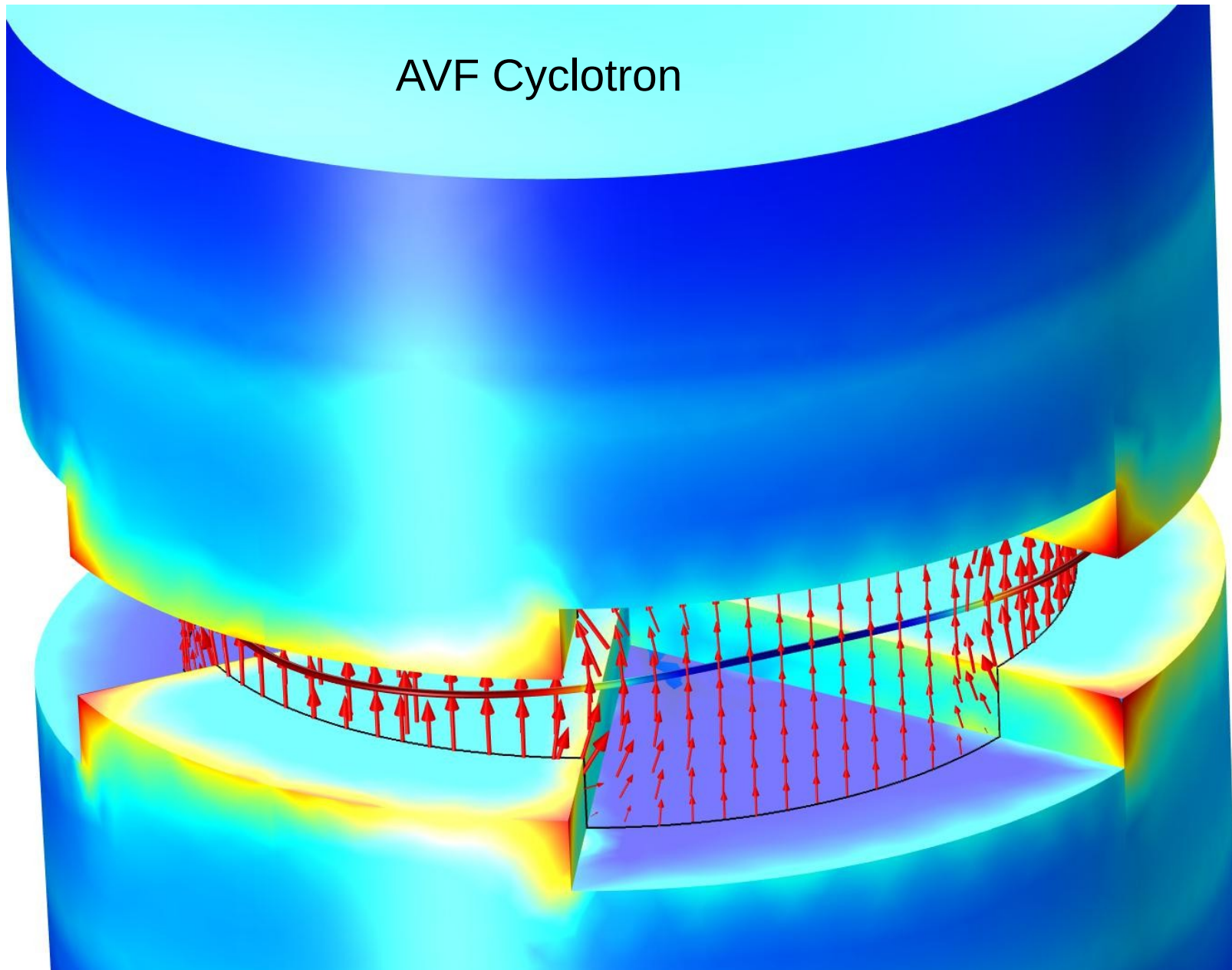
# Cyclotron: overcoming the relativistic limit #2

- **Isochronous cyclotron = azimuthally varying field (AVF) cyclotron**  $\approx$  sector-focused cyclotron
- **B increasing with R** (in order not to allow the orbit radius to grow proportionally to momentum  $\rightarrow$  to keep the revolution frequency constant).
- Problem: B increasing with R  $\rightarrow$  defocusing vertically
- Solution: ( $\sim$ edge focusing – orbit entering the magnet non-perpendicularly!)



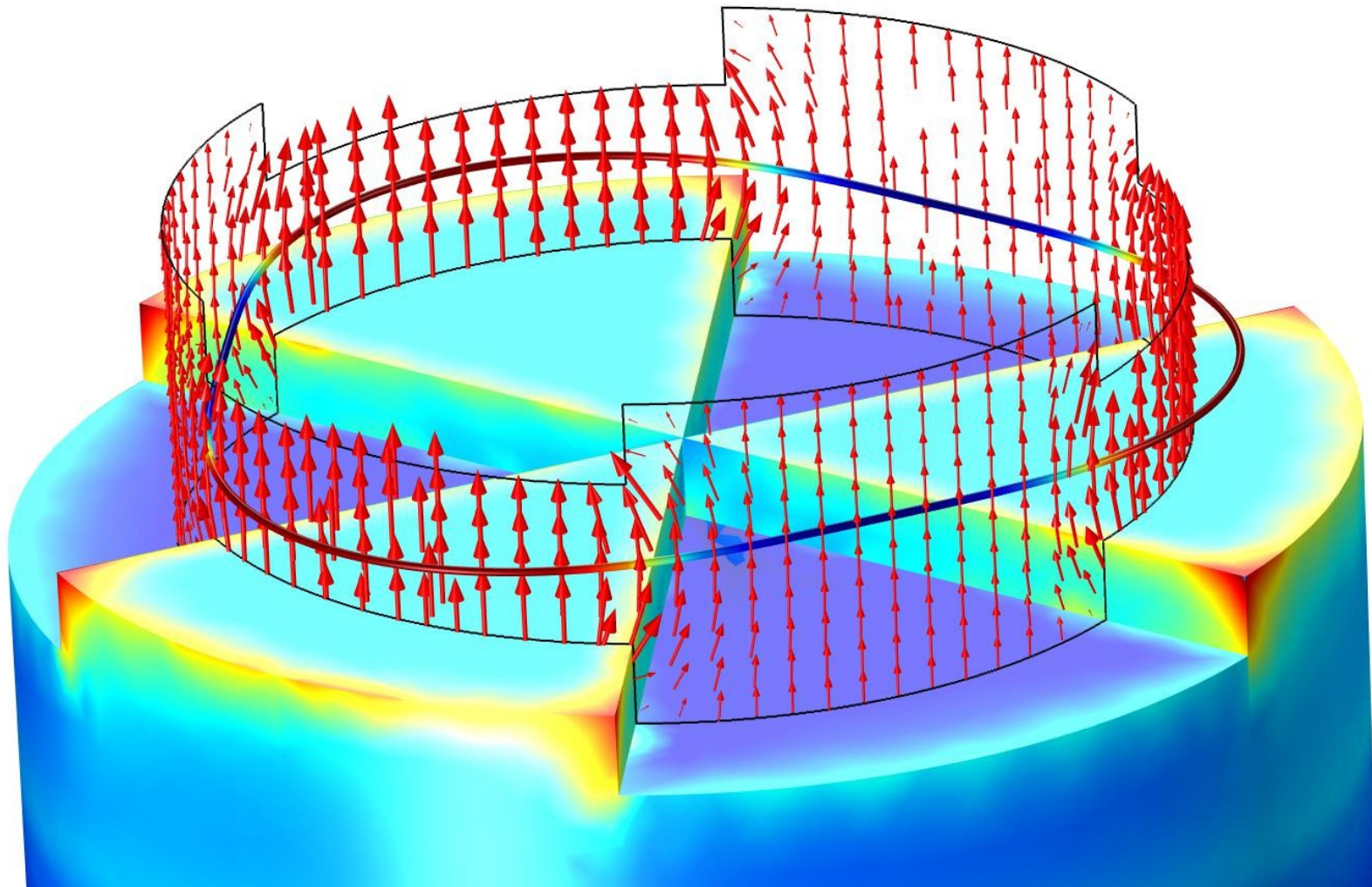
Illusztrációk: K. Strijckmans, Computerized Medical Imaging and Graphics 25 (2001) 69

# Cyclotron: overcoming the relativistic limit #2



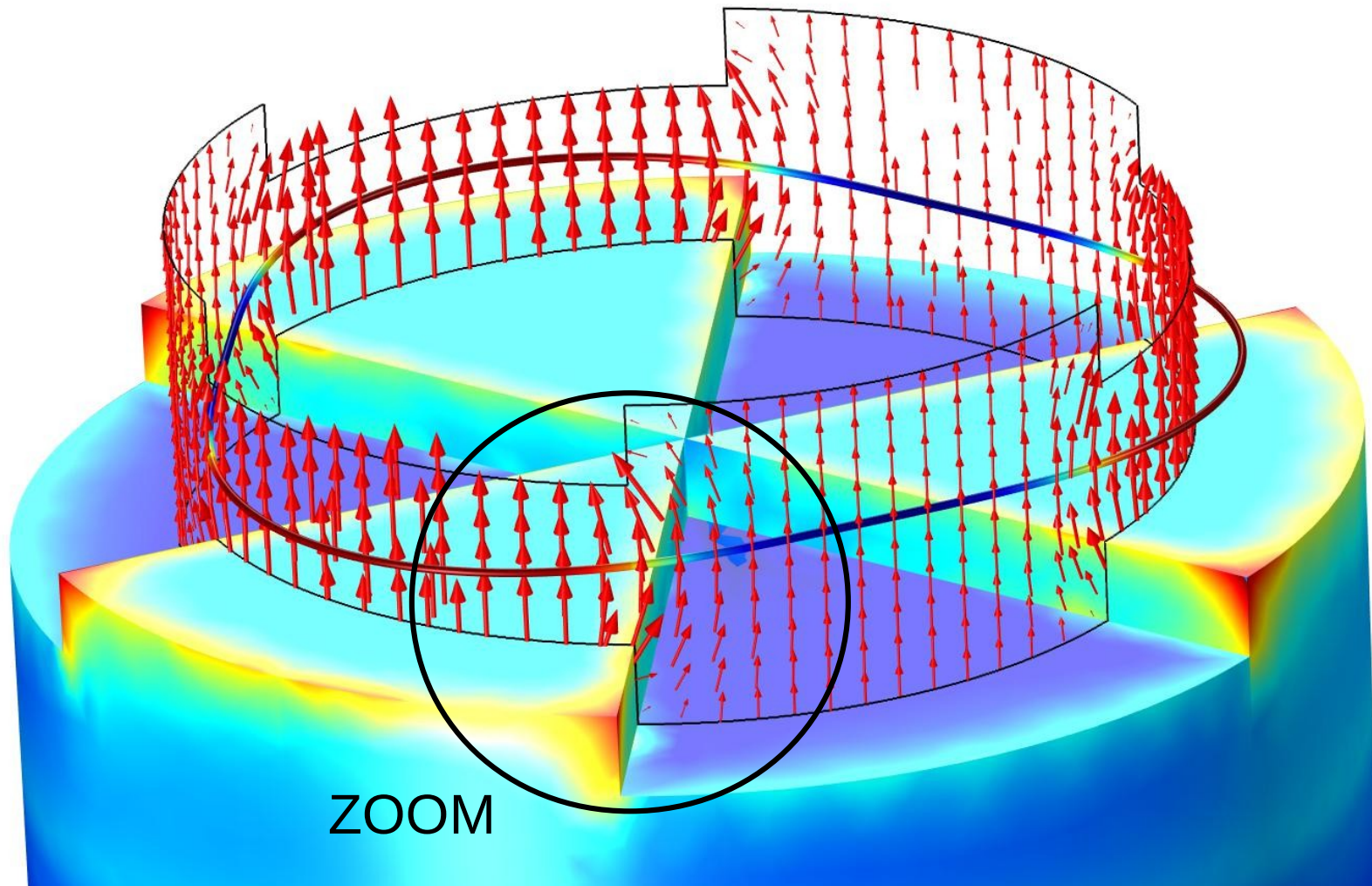
# Cyclotron: overcoming the relativistic limit #2

## AVF Cyclotron

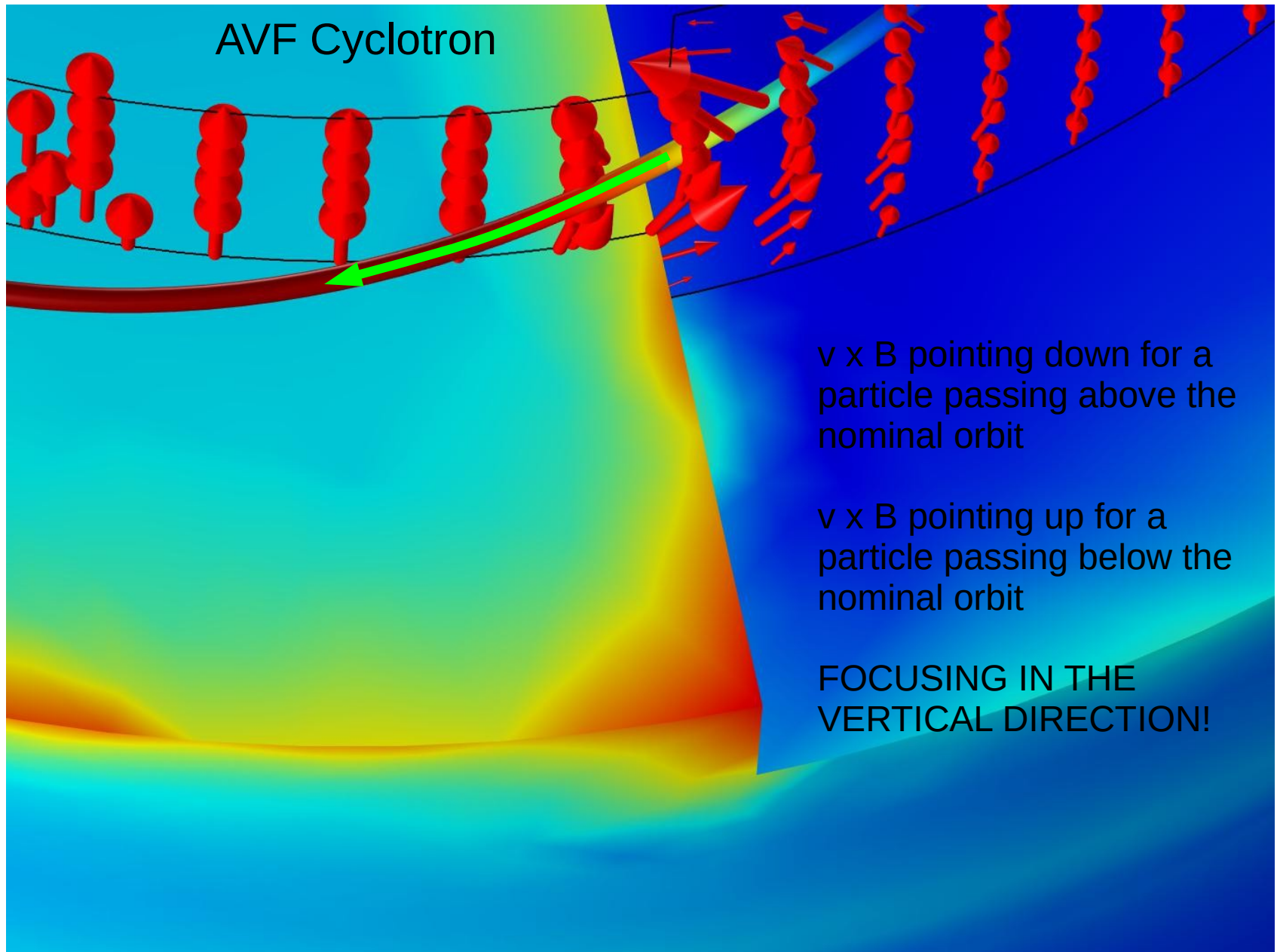


# Cyclotron: overcoming the relativistic limit #2

## AVF Cyclotron

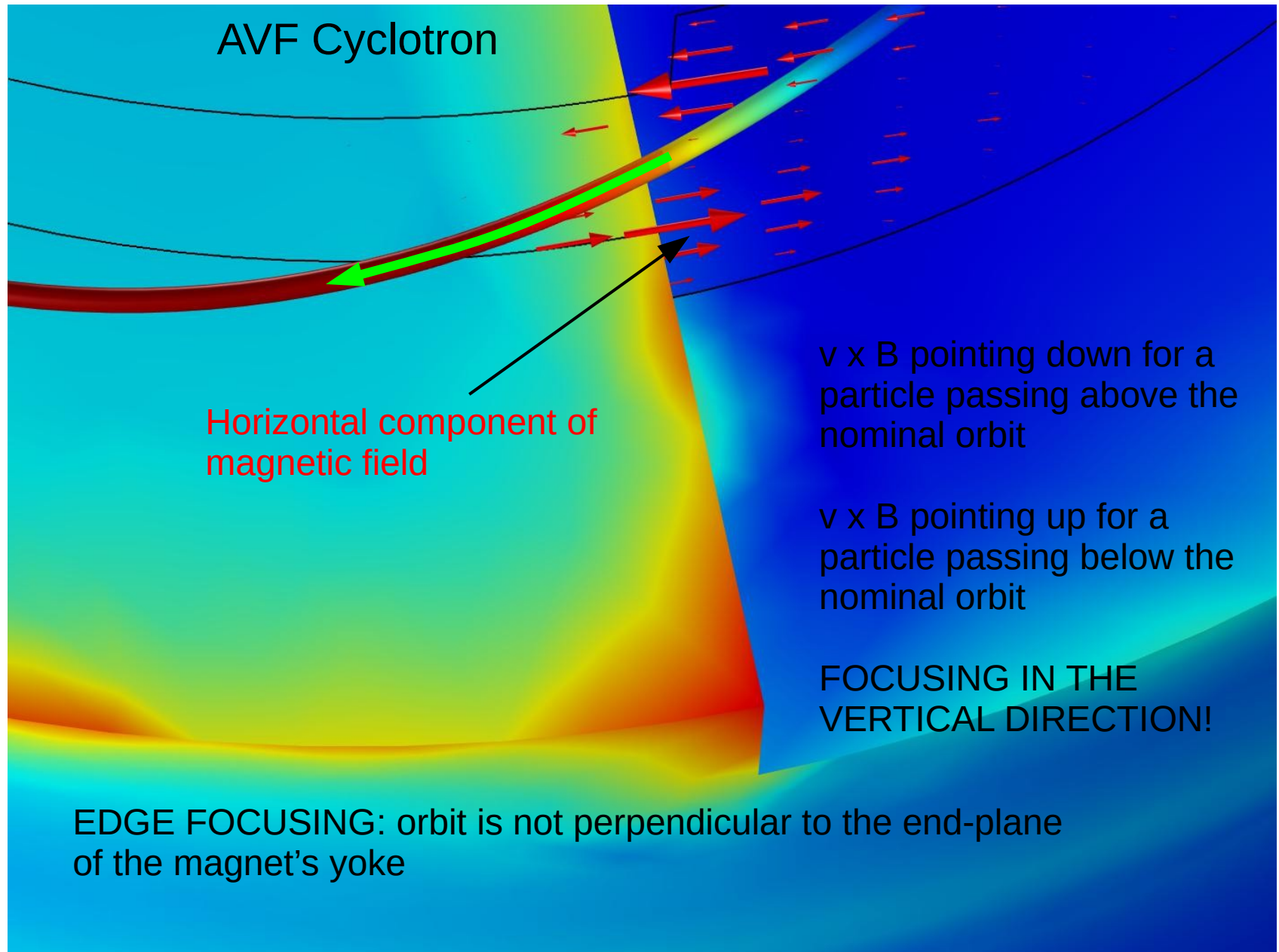


# Cyclotron: overcoming the relativistic limit #2





# Cyclotron: overcoming the relativistic limit #2

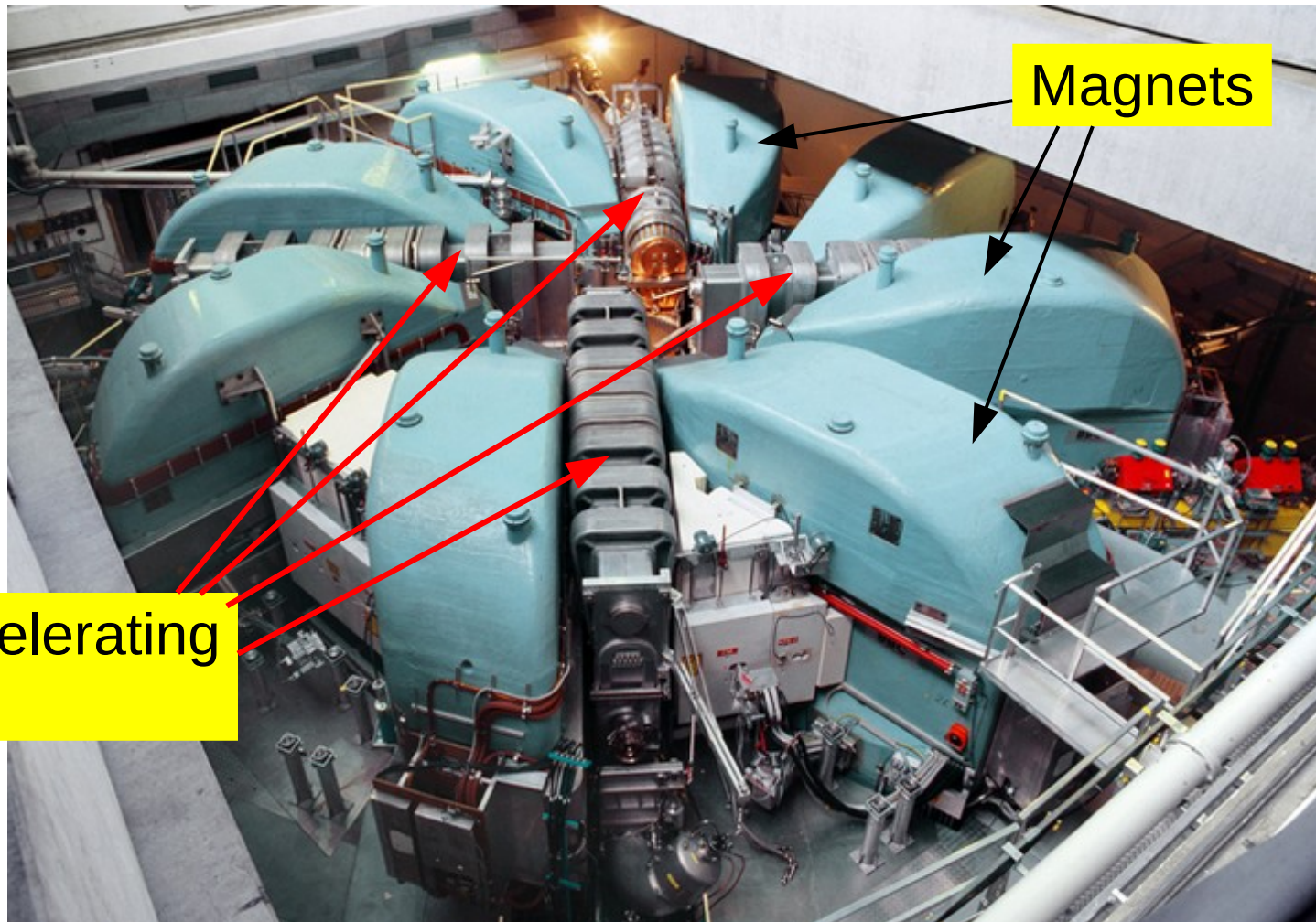


# Sector focused cyclotron (PSI)

Extreme case of AVF: Magnets in discrete sectors, with interleaving gps.

Advantages:

- Easier access to the vacuum system
- Accelerating cavities can be placed between the magnets



Huge accelerating  
cavities

Magnets

# Cyclotrons today

- ~650 cyclotrons in operation
- Production of radioisotopes
- Proton therapy
- Nuclear research

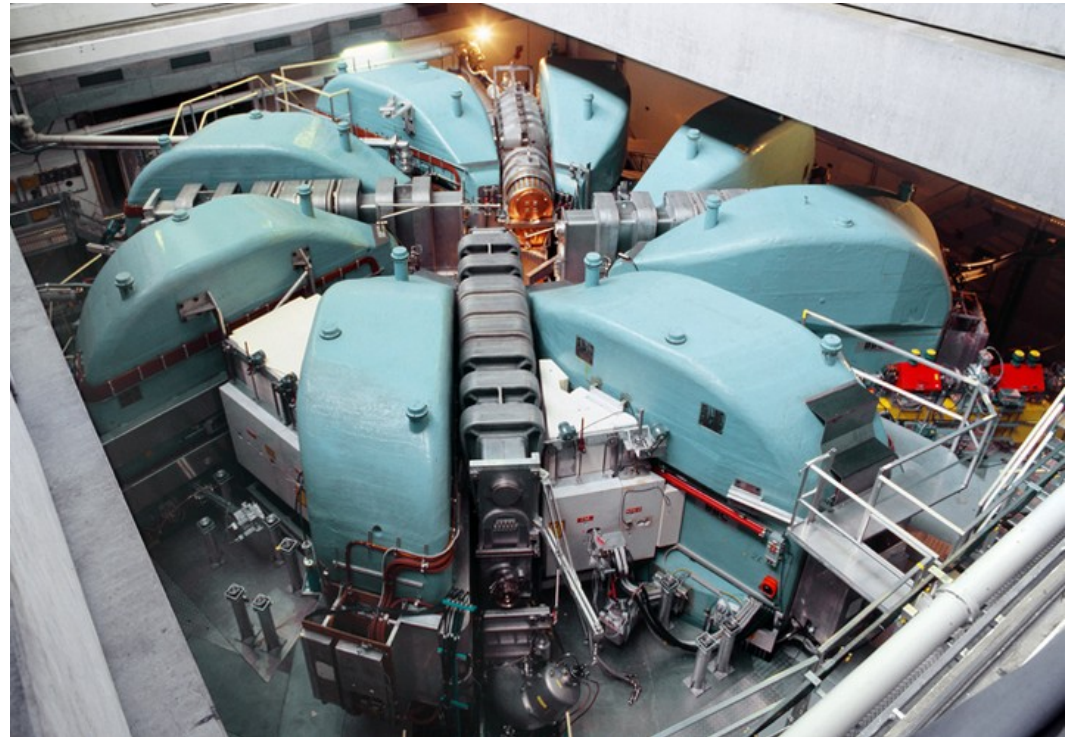
# Proton Therapy Center - Prague

Commercial,  
turn-key systems



# Cyclotrons today: PSI (Paul Scherrer Institute, Switzerland)

- Cockroft-Walton (870 keV) → small cyclotron (72 MeV) → large cyclotron (590 MeV)
- diameter: 15 m. Proton current: 2.2 mA (!!!)  
1g hydrogen in 1.5 years!  
most intense proton beam
- secondary  $\pi/\mu$  beams
- neutron spallation source



Also @ PSI:

- 250 MeV SC cyclotron (proton therapy)

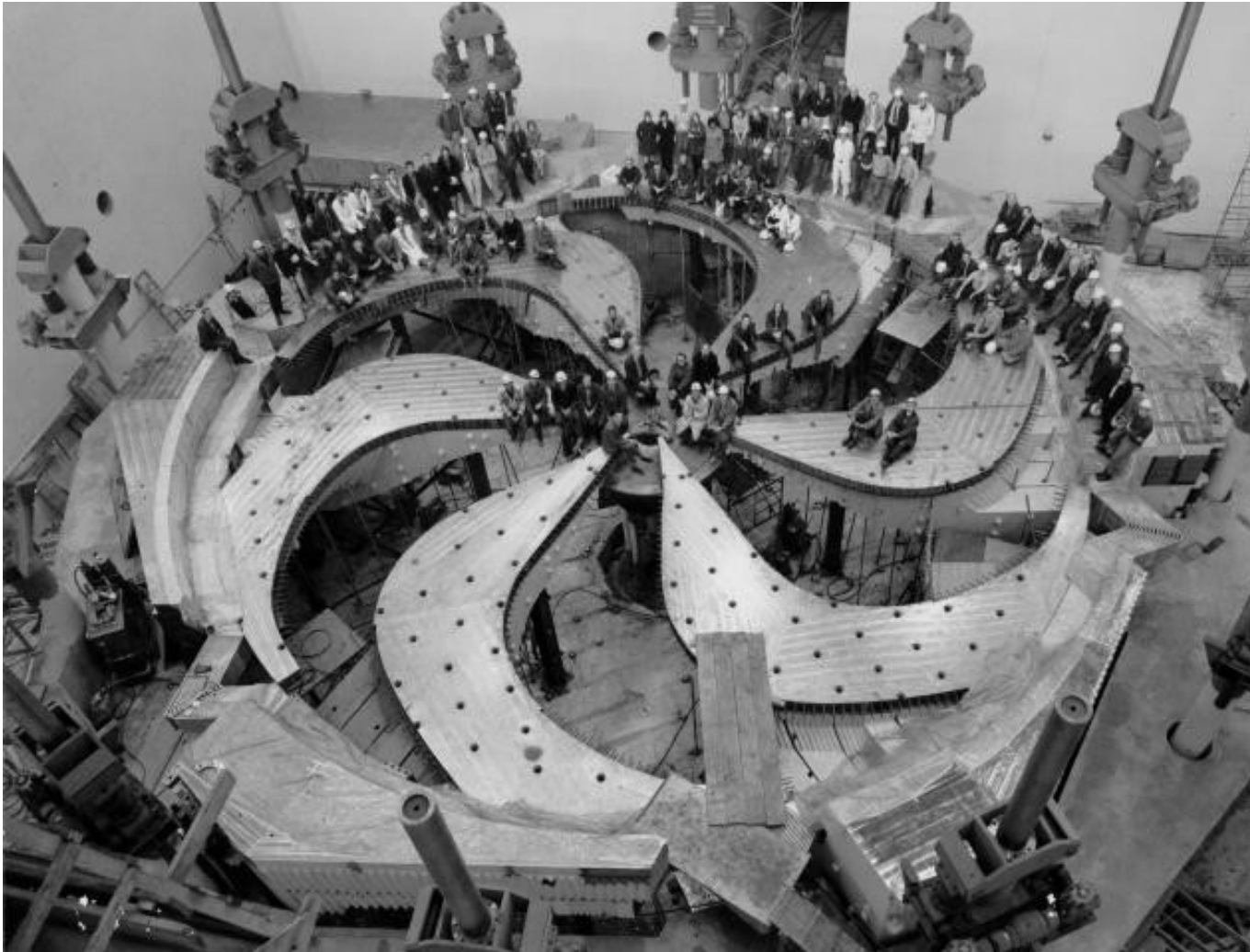
# Cyclotrons today: PSI (Paul Scherrer Institute, Switzerland)

- COMET
- proton therapy
- Superconducting → compact
- 250 MeV

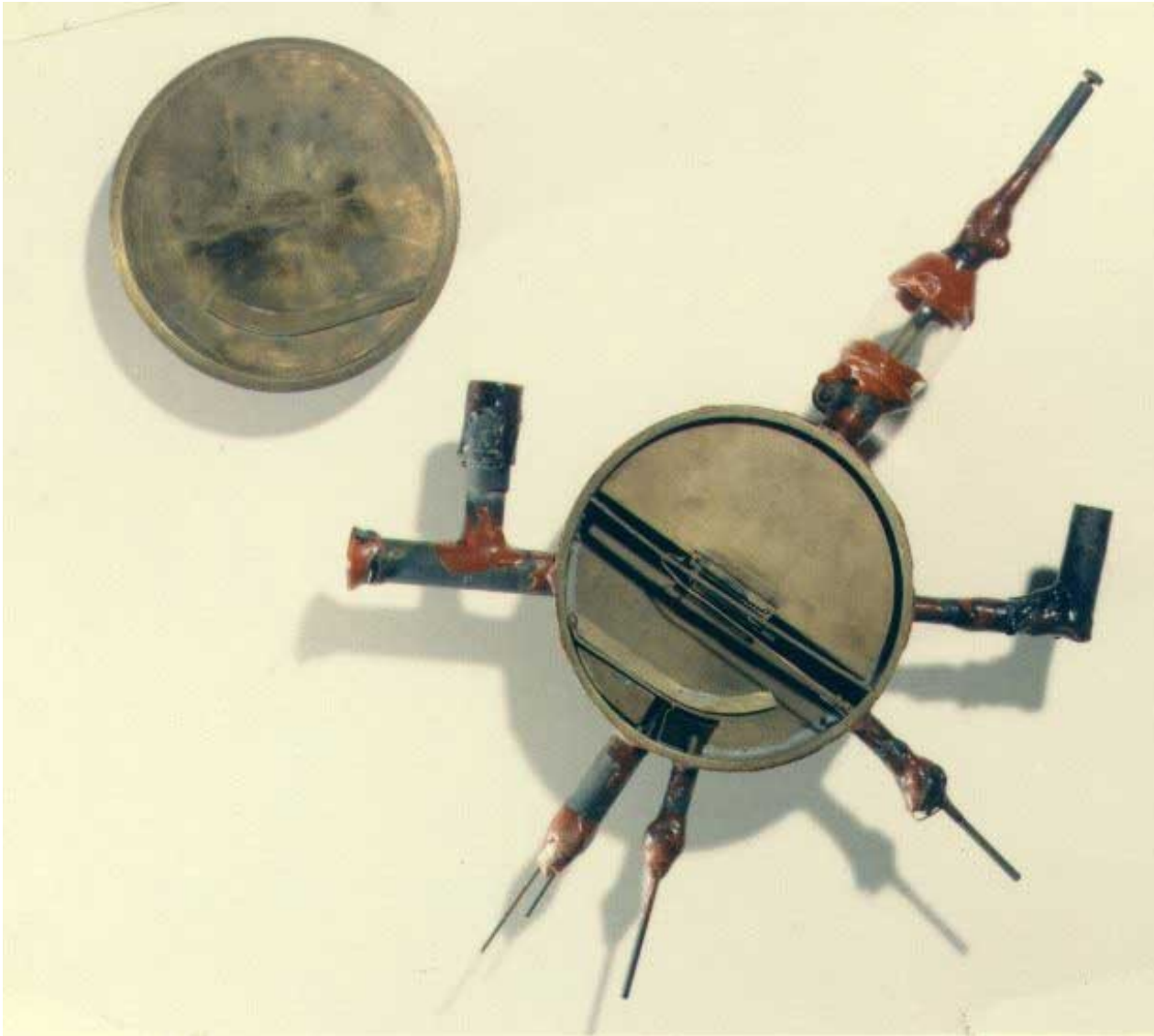


# Cyclotrons today: TRIUMF (Canada)

- Maximum energy: 520 MeV (proton). Intensity:  $<400 \mu\text{A}$  ( $\sim 140 \mu\text{A}$ )
- Diameter: 18 m. Weight of magnet: 4400 tons



# Cyclotron

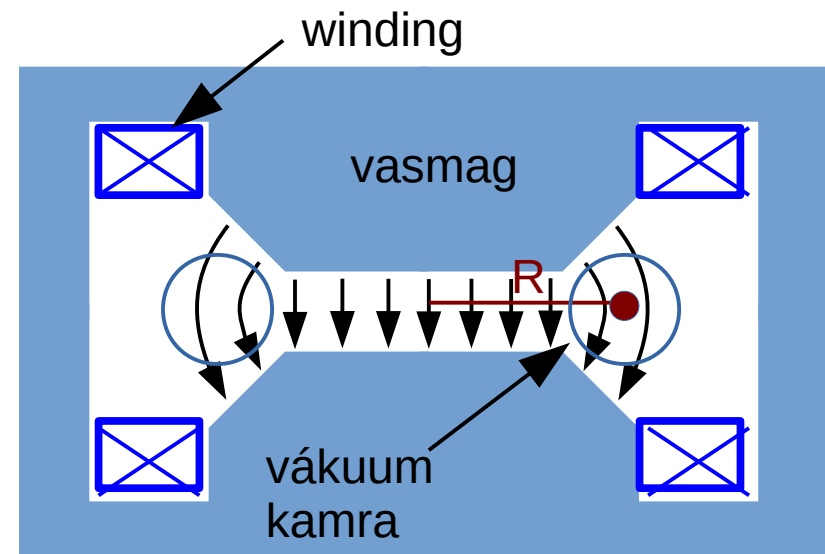


Lawrence ~1931.  
~12 cm diameter, 80 keV



# Betatron

- ~ transformer: primary: winding.  
secondary: electron beam
- Original idea: Rolf Widerøe  
Realization: Donald Kerst  
(1940, 2.3 MeV)
- Electrons move on a **fixed** orbit!
- Bending field  $B_{\text{guide}}$  is the same as the accelerating field

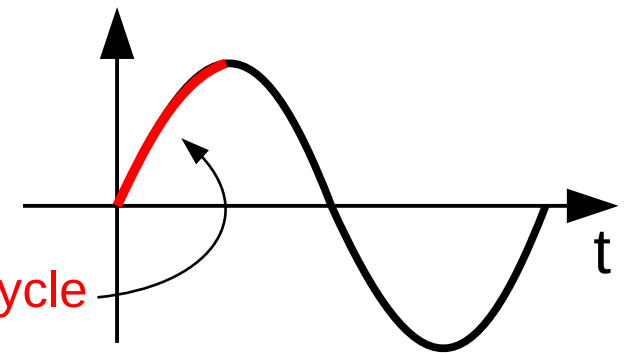


$$\oint E ds = 2 R \pi E = \int \frac{\partial B}{\partial t} dA = R^2 \pi \dot{B}_{av} \quad \rightarrow \quad E = \frac{1}{2} \dot{B}_{av} R$$

$$\dot{p} = eE = \frac{1}{2} e \dot{B}_{av} R \quad \rightarrow \quad p = \frac{1}{2} e B_{av} R = e B_{\text{guide}} R$$

$$B_{\text{guide}} = \frac{1}{2} B_{av} \quad \text{'betatron principle'}$$

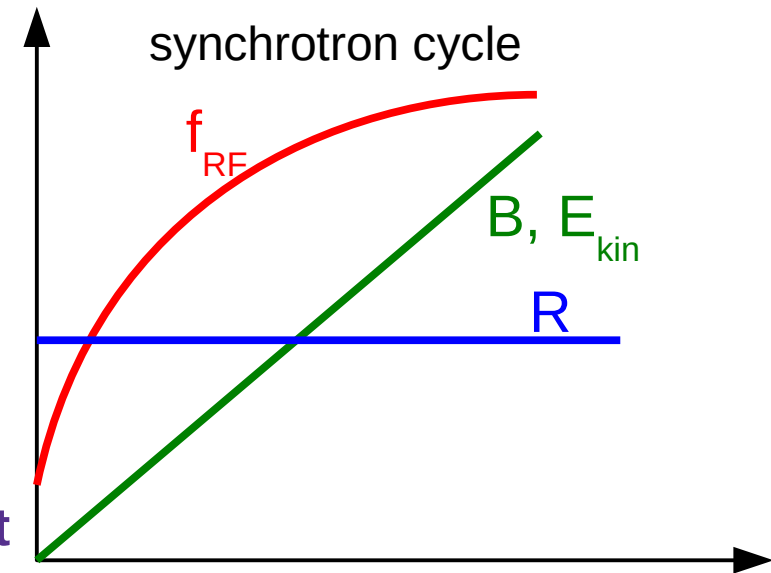
- Max energy: ~300 MeV (275 ton mgnet)
- Pulsed operation: AC current, accelerates during **1/4 cycle**
- **Weak focusing** (see later)



# Synchrotron – accelerator/storage ring

- 3 basic ideas:

- Acceleration in the gap of a resonator cavity (~gap, cyclotron)
- **Frequency changing with time –** (increases in this case, was decreasing for synchro-cyclotron)
- **Magnetic field increasing with time,** in order to keep the **radius of orbit constant** (~betatron)



- Orbit is constant! →

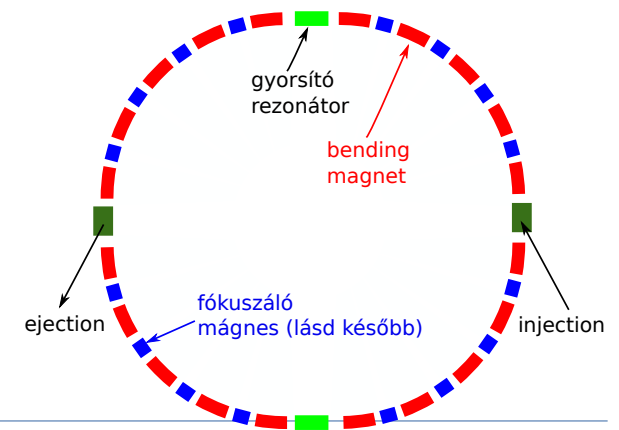
- We need B field only at the fixed orbit. Can build large accelerators, in contrast to previous principles where B had to cover huge area

- Cyclotrons: B must cover changing orbit

- Magnetron: need to cover area encircled by beam (induction):.

$$\oint \frac{\partial B}{\partial t} dA$$

- Cyclic operation (not DC):  
injection + acceleration + ejection



# Advantages of collider rings

- One accelerating cavity in the whole ring, “reused” at every turn
- Two beams colliding head-on: center-of-mass energy much larger than in fixed-target experiments
- Particles missing a collision get a second chance in the next turn.

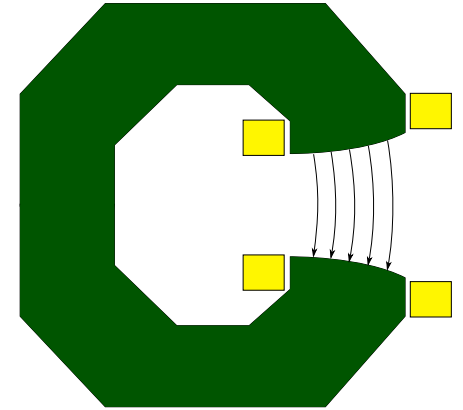
# Synchrotrons – the beginning

- First proposal: Mark Oliphant, 1943 Oakridge (US). Memo to the Directorate of Atomic Energy (UK, classified document)  
A key principle (phase stability) is now known yet.
- Phase stability – even though particles have a finite velocity spread, they remain in sync with the accelerating RF field even after a looooot of turns.  
V.I. Veksler (Moszkva, 1944), E.M. McMillan (Berkeley, 1945) – see later
- McMillan proposed the construction of a synchrotron
- First working synchrotron: General Electric Co. 1946; 70 MeV electrons  
Glass vacuum tube – the first machine to produce visible synchrotron radiation
- First proton synchrotron:  
Cosmotron, 3 GeV  
(Brookhaven Nat. Lab, 1952)  
**weak focusing** – see later
- Weak focusing → **large beamsize, large aperture, large and expensive vacuum pipes and magnets**  
Cosmotron: 20x30 cm; Bevatron (6.2 GeV): 30 cm x 1.2 m (!)

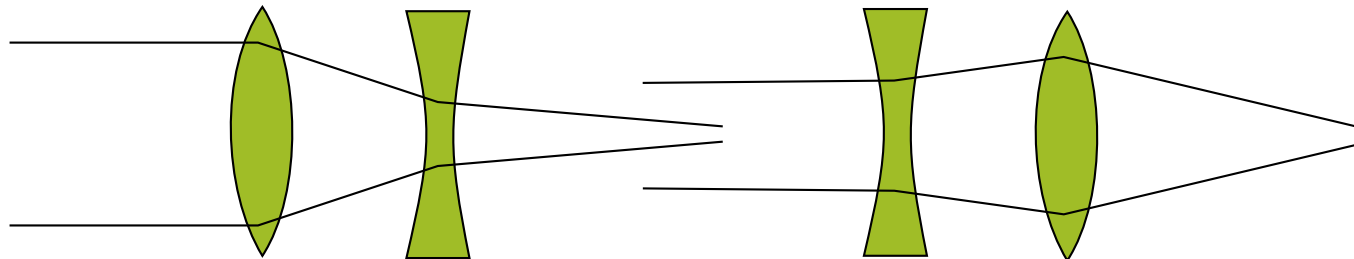


# Synchrotrons – strong focusing

- Cosmotron: iron yoke saturated at large fields → distortion of the field pattern. This could lead to the **destruction of the conditions for weak focusing** ( $n$  became  $> 1$ ).
- E.D.Courant, S. Livingston, H.S.Snyder: compensate this by turning some magnets  $180^\circ$ , giving negative  $n$ -values, bringing the average back to  $0 < n < 1$

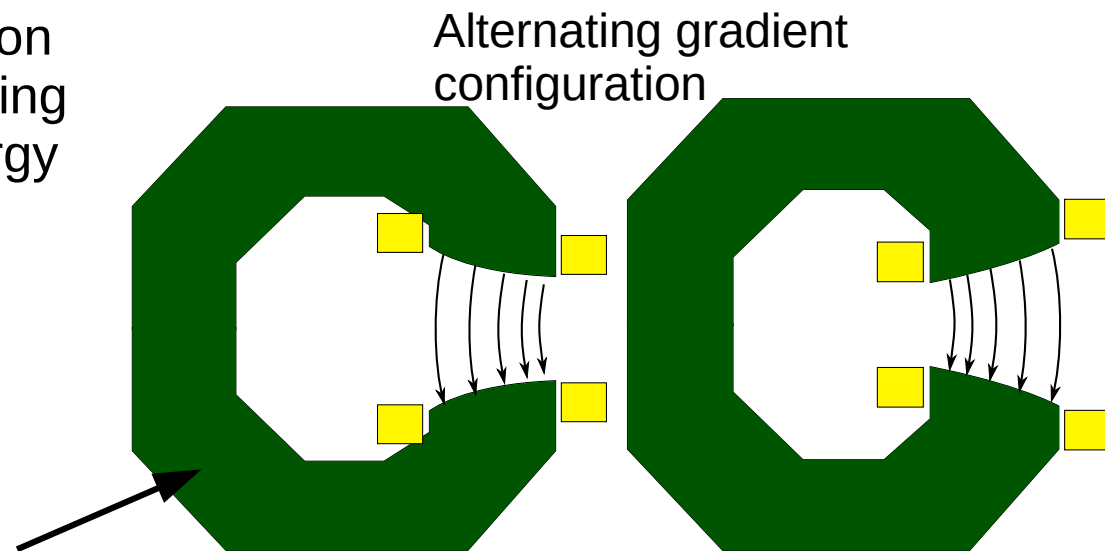


- Discovery: **alternating pattern can lead to much stronger net focusing in both planes simultaneously!!**
- Individual magnets do not need to focus in both planes simultaneously! **They focus in one plane, and defocus in the other plane**
- Optical analogy: net focusing with proper conditions



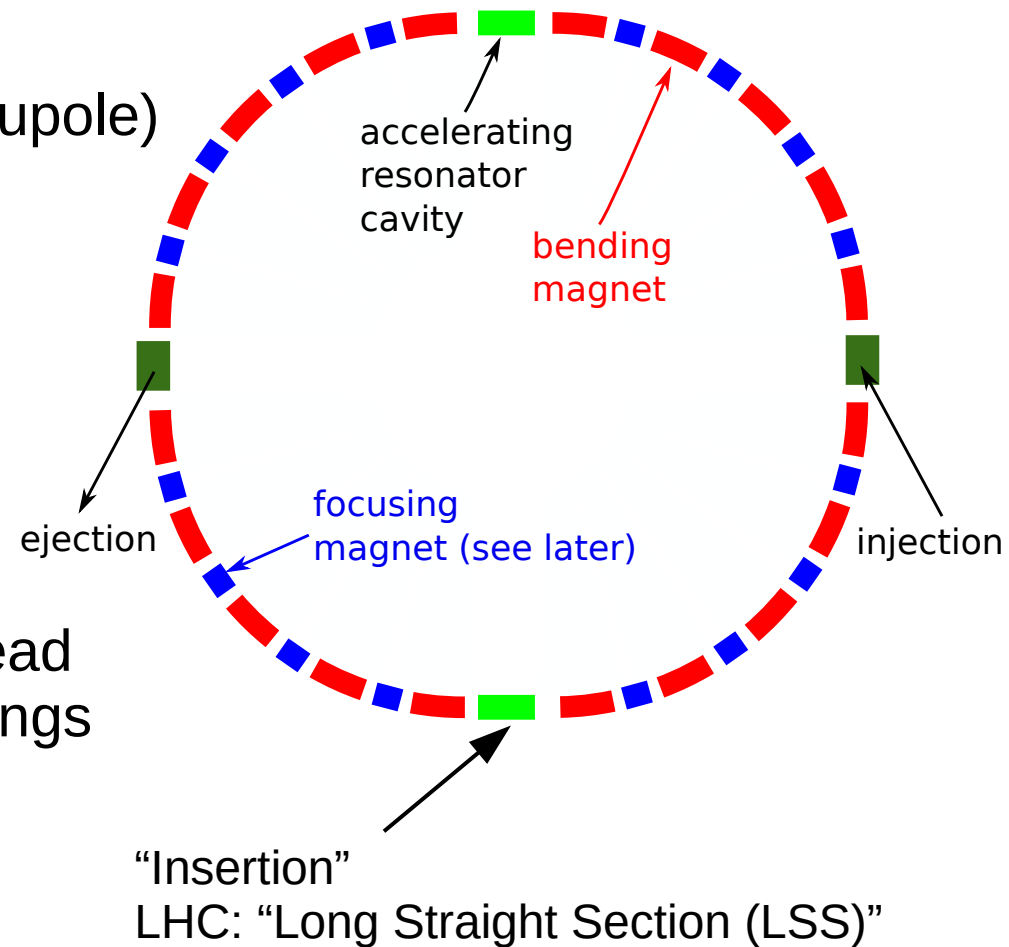
# Synchrotrons – strong focusing

- Strong focusing gives **much smaller beamsizes!**
- No need for huge vacuum pipes and magnets
- Beam can be focused to a smaller spot (higher luminosity!)
- 10 GeV proton synchrotron being planned @ CERN. Visit to BNL at the time of discovering AG (strong) focusing – old idea dropped:
  - 1959: CERN Proton Synchrotron (PS) 25 GeV, first strong focusing synchrotron, world record energy for a short time
  - 1960: BNL AGS (Alternating Gradient Synchrotron) 33 GeV
  - Both used **combined function magnets** (the same magnet creating the bending dipole and focusing quadrupole field)
  - Very similar: cooperation & competition

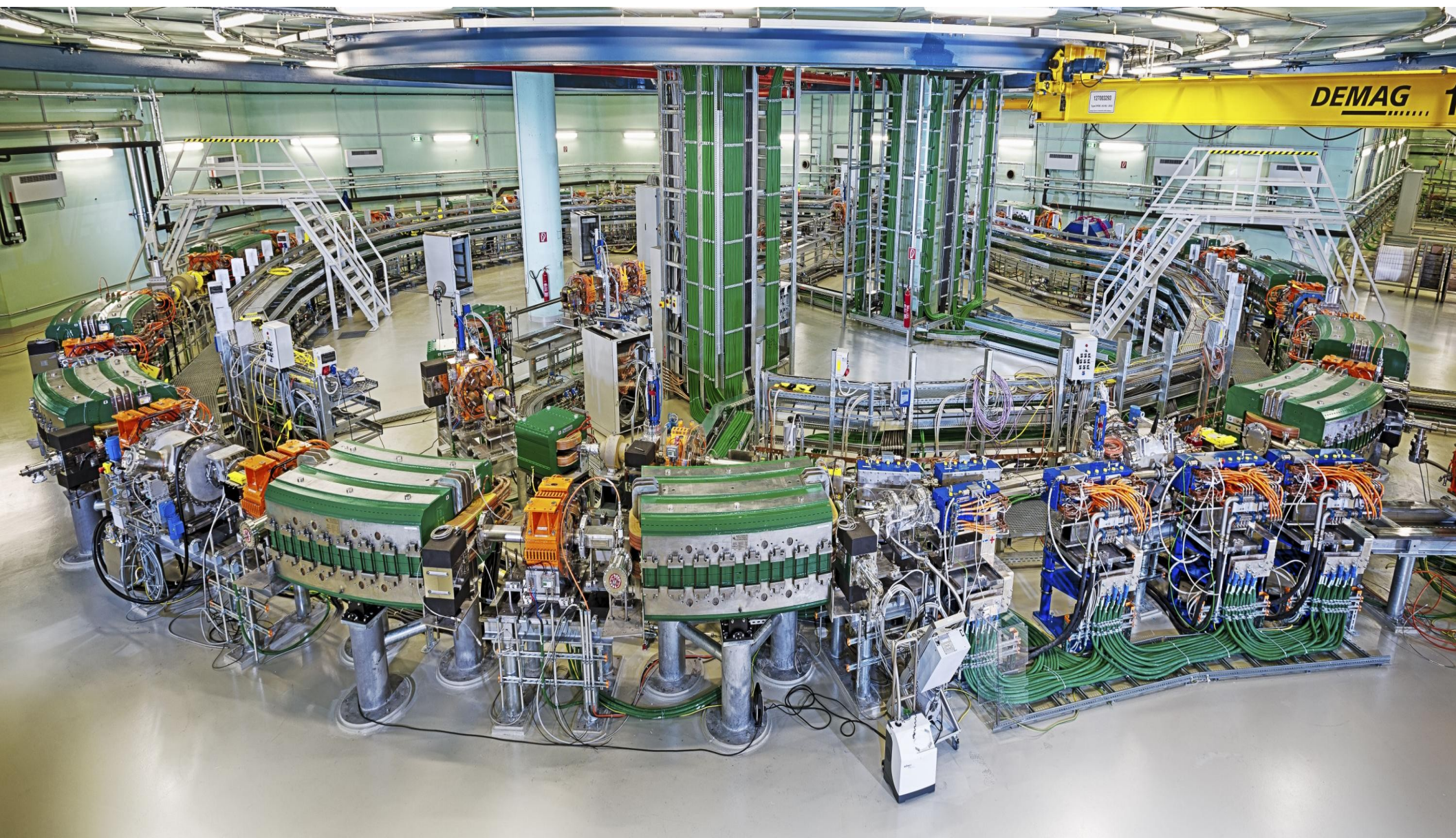


# Synchrotron

- Modern synchrotrons: bending (dipole) and focusing (quadrupole) by separate magnets
- Straight (focusing, quads) and bent (dipoles) sections alternating
- + extra corrector magnets (e.g. sextupole)
- Periodic structure:
  - Largest period: the full ring
  - Repeating sectors (4 in the figure)
  - Periodic structure within a section: (FODO = focus-drift-defocus-drift)
- Synchrotrons are the most widespread for high energy physics (all CERN rings for example)



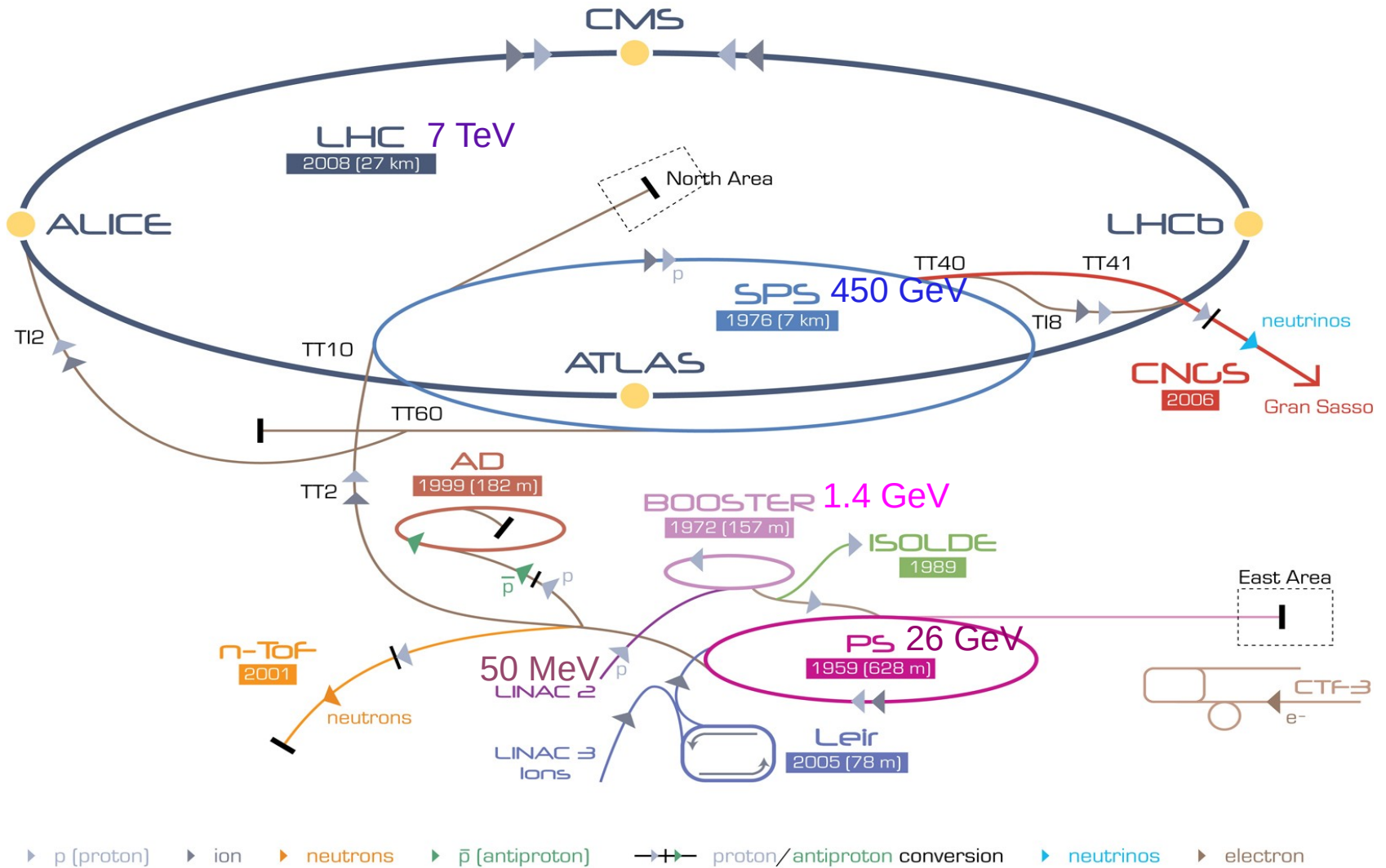
# A medical synchrotron: MedAustron, Wiener Neustadt, Austria





# Synchrotron – the accelerator of the present

- Synchrotrons have a finite energy span → hierarchy of rings with increasing energy



LHC Large Hadron Collider SPS Super Proton Synchrotron PS Proton Synchrotron

AD Antiproton Decelerator CTF-3 Clic Test Facility CNGS Cern Neutrinos to Gran Sasso ISOLDE Isotope Separator OnLine DEvice  
 Acc... LEIR Low Energy Ion Ring LINAC LINear ACcelerator n-ToF Neutrons Time Of Flight

# CERN proton-accelerator hierarchy (near past)

- Duoplasmatron ion forrás: 92 keV - electrostatic acceleration
  - RFQ: 750 keV
  - Alvarez drift-tube linac: 50 MeV
  - PS Booster: 1.4 GeV
  - PS: 26 GeV
  - SPS: 450 GeV
  - LHC: 7 TeV
- 
- LINAC2
- Synchrotrons

# CERN proton-accelerator hierarchy (near future)

- H- ion source: 45 keV - electrostatic acceleration
  - RFQ: 3 MeV
  - Alvarez drift-tube linac: 50 MeV
  - Cell-coupled drift tube linac: 102 MeV
  - Pi-mode structure: 160 MeV
  - PS Booster: 2 GeV (LIU: LHC Injector Upgrade)
  - PS: 26 GeV
  - SPS: 450 GeV
  - LHC: 7 TeV
- 
- LINAC4
- Synchrotrons

# The future (at least towards high energies)

- HL-LHC (High-luminosity LHC) – first priority @ CERN, goal: reach 10x luminosity in LHC by 2020 (serious hardware upgrade)
- FCC (Future Circular Collider) study: develop a conceptual design for the next generation collider ring @ CERN
  - 1) >350+350 GeV e+e- collider (FCC-ee)
  - 2) 50+50 TeV pp collider (FCC-hh)
  - CERN's current accelerators as injector chain
  - 80-100 km ring
- CLIC – Compact Linear Collider (CERN). 3 TeV center-of-mass energy, e+e- collider. Energy transfer: “Drive beam” → Normalconducting RF cavity → colliding beams
- ILC – International Linear Collider. Superconducting resonator technology, 500+500 GeV e+e-. (Japan?)
- China (?) - Higgs factory, 52 km 250+250 GeV electron-positron collider, and later proton-proton collider